A novel classifier model for mass classification using BI-RADS category in ultrasound images based on Type-2 fuzzy inference system

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Abstract. Ultrasound imaging is an imaging technique for early detection of breast cancer. Breast Imaging Reporting and Data System (BI-RADS) lexicon, developed by The American College of Radiology, provides a standard for expert doctors to interpret the ultrasound images of breast cancer. This standard describes the features to classify the tumour as benign or malignant and it also categorizes the biopsy requirement as a percentage. Biopsy is an invasive method that doctors use for diagnosis of breast cancer. Computer-aided detection (CAD)/diagnosis systems that are designed to include the feature standards used in benign/malignant classification help the doctors in diagnosis but they do not provide enough information about the BI-RADS category of the mass. These systems classify the benign tumours with 90% biopsy possibility (BI-RADS-4) and with 2% biopsy possibility (BI-RADS-2) in the same category. There are some studies in the literature that make category classification via commonly used classifier methods but their success rates are low. In this study, a two-layer, high-success-rate classifier model based on Type-2 fuzzy inference is developed, which classifies the tumour as benign or malignant with its BI-RADS category by incorporating the opinions of the expert doctors. A 99.34% success rate in benign/malignant classification and a 92% success rate in category classification (BI-RADS 2, 3, 4, 5) were obtained in the accuracy tests. These results indicate that the CAD system is valuable as a means of providing a second diagnostic opinion when radiologists carry out mass diagnosis.

Keywords. Ultrasound; CAD; Type-2 fuzzy.

1. Introduction

According to recent research, 14.79% of deaths caused by cancer are due to breast cancer [1]. Breast cancer is defined as the abnormal cell growth around the breast and it is classified into two classes as benign or malignant [2]. Mammography and ultrasound imaging are the most principal imaging techniques [3, 4]. With respect to the ultrasound imaging, mammograms cause the doctors to make much more incorrect detections, meaning a more false-positive detection rate [5]. Breast Imaging Reporting and Data System (BI-RADS) lexicon, which is developed by The American College of Radiology for the diagnosis of sonographic lesions, includes the description of mass features such as shape, margin and orientation. Predictive values of these features were examined by a study by Hong in 2005. According to this study, predictive values for malignant masses are spiculated margins 86% and irregular shape 62%, while the predictive values for benign masses are circumscribed margins 90% and shape 84% [6, 7]. BI-RADS categorizes the lesions with respect to the probability of biopsy

requirement. These categories are Category 2 0%, Category 3 is below 2%, Category 4 is 3%–94% and Category 5 is 95% [8]. The most basic standard to determine whether the tumour is malignant or not is through biopsy. But more than 70% of the results obtained via biopsy (which is an invasive method) are benign [9]. Redundant biopsies both increase the cost and cause emotional pressure on the patient [10]. In the case of lesion characterization, complex anatomy, variation in the presentation of benign and malignant states and the varying abilities of the physicians may result in interpretation errors. Computer-aided detection (CAD) systems have more space in modern medicine, providing specialists with a second source of information and increasing the diagnostic success rates. These systems have been implemented to support the detection and characterization of breast lesions from digital mammography and ultrasound images, to assist the diagnosis of lung cancer using chest radiographs and Computed Tomography images, to distinguish Tourette's syndrome from chronic tic disorder based on Single Photon Emission Computed Tomography brain imaging and to support the diagnosis of functional brain disorders using Positron Emission Tomography images. CAD systems that help the doctor in the interpretation of

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Table 1. Survey of CAD systems.

Reference no.	Size of data set	Classifier type	Accuracy (%)	Features	nof	Feature selection
[13]	49 (32 B/17 M)	DA function	87.80	Tx. & Mh.	5	No
[20]	250 (215 B/35 M)	SVM	94.40	Tx.	2	No
[28]	112 (54 B/58 M)	SVM	91.10	Tx. & Mh.	85	PCA
[29]	210 (120 B/90 M)	SVM	90.95	Mh.	6	No
[30]	78 (26 B/52 M)	SVM	95.70	Tx. & Mh.	10	PCA
[31]	148 (119 B/29 M)	SVM	85.14	Tx. & Mh.	14	GA
[32]	200 (102 B/98 M)	Biclustering + BPNN	94.00	Mh.	19	Variance metric
[33]	178 (88 B/90 M)	FCM	95.86	Tx. & Mh.	457	Filter
[33]	178 (88 B/90 M)	BPNN	94.14	Tx. & Mh.	19	Filter
[34]	118 (84 B/34 M)	SVM	82.20	Mh.	19	PCA
[35]	210 (120 B/90 M)	SVM + GA	95.24	Tx. & Mh.	6	GA
[36]	321 (113 B/208 M)	SVM	86.92	Tx. & Mh.	36	By radiologists
[36]	321 (113 B/208 M)	ANN	86.60	Tx. & Mh.	36	By radiologists
[36]	321 (113 B/208 M)	KNN	83.80	Tx. & Mh.	36	By radiologists
[84]	65 (31 B/34 M)	FCMNN	92.00	Tx.	49	No
[38]	178 (88 B/90 M)	SVM	94.40	Tx. & Mh.	457	Filter
[38]	178 (88 B/90 M)	BPNN	96.60	Tx. & Mh.	19	Filter
[72]	244 (166 B/78 M)	Decision tree	89.00	Tx. & Mh.	6	Statistical method

Abbreviations: Tx. – texture, Mh. – morphologic, B – benign, M – malignant, GA – genetic algorithm, DA – discriminant analysis, FCMNN – Fuzzy Cerebellar Model Neural Networks, BPNN – Back-Propagation Neural Network, FCM – fuzzy C-Mean clustering, ANN – Artificial Neural Network, PCA – principal component analysis, nof – total number of features

radiologic images also decrease the detection time [11, 12]. A typical CAD system architecture consists of four main modules, namely image pre-processing, definition of region of interest (ROI), feature extraction/selection from ROI and classification of ROI [11, 13]. In this work, the mass areas in 153 breast ultrasound images that belong to the women patients were marked by an expert radiologist. The smallest rectangular area covering the tumour was cut off from the image to be used as the ROI. The speckle noise in the sub-images was reduced by filtering and image enhancement. Medical information that the expert doctor uses while determining the BI-RADS category and the type of mass were noted during the interpretation of each image. A CAD model based on the Type-2 fuzzy inference was designed using this information and the feature values were obtained using the ROI. Depending also on the expert opinion, the proposed model is based on a novel two-layer Type-2 fuzzy inference system that classifies the tumour area as benign or malignant with its BI-RADS category. The rest of the paper is as follows. In section 2, there is a literature review. In section 3, the fuzzy inference system is examined. In section 4, the details of the proposed CAD model are provided. In section 5, the classification success-rate tests of the proposed model are presented. Finally, in section 6, the results and the future work are discussed.

2. Literature review

In recent years, classification of breast tumours in ultrasound images is a hot research point. Many CAD systems have been proposed to distinguish the benign mass from the

malignant mass in these studies. A survey on the research work done on such CAD systems is summarized in table 1. Columns of table 1 present the size of the data set used in the study, type of the classifier, the success rate of the classifier, the type of the features used in the study, the size of the total features used in the study and feature selection methods if there are any. The used abbreviations are summarized in the last row of table 1.

2.1 Image preprocessing

The most severe disadvantage of the ultrasound is the low quality of the image. It affects the precision of the diagnosis negatively [14]. The sound wave used in ultrasound imaging has to pass through the heterogeneous tissue with different acoustic properties before it reaches the converter. This situation causes distortion in the image called the speckle noise [15]. Many filtering architectures have been proposed to remove the speckle noise [16, 17].

2.2 Obtaining ROI

ROI is the area that includes the mass and is used to extract the features [9]. There are two methods to obtain the ROI. One of these is obtaining automatically by segmentation methods [9, 18, 19] and the other is manually by expert radiologist marking [20, 21]. Using the ROI, various feature sets grouped as texture, morphological, model-based and descriptor are obtained, which can be used to distinguish the breast cancer lesions as benign and malignant [10, 22].

2.3 Texture features extraction

Texture features that are very commonly used in literature can be obtained using first-order or second-order statistical calculations such as grey-level co-occurrence matrix (GLCM) [21, 23]. GLCM matrices are obtained by calculating the joint probability density functions of the pixel pairs at a specific orientation and distance in the image matrix [24]. Let i, j ($i, j = 0, 1, 2, \dots, N-1$) represent the grey levels of two pixels and let μ be the relationship of the position between two pixels as orientation and distance. Then $P_\mu(i, j)$ represents the GLCM [25]. Texture features can be extracted from a grey-scale image using GLCM [26]. Texture features are given in Eqs. (1)–(4):

$$energy = \sum_{i=0}^{N-1} \sum_{j=0}^{N-1} P_\mu^2(i, j) \quad (1)$$

$$contrast = \sum_{i=0}^{N-1} i^2 \left\{ \sum_{j=0}^{N-1} \sum_{j=0}^{N-1} P_\mu(i, j) \right\} \quad (2)$$

$$correlation = \frac{\sum_{i=0}^{N-1} \sum_{j=0}^{N-1} P_\mu(i, j) ij - m_1 m_2}{\sigma_1^2 \sigma_2^2} \quad (3)$$

$$homogeneity = \frac{\sum_{i=0}^{N-1} \sum_{j=0}^{N-1} P_\mu(i, j)}{1 + (i + j)^2} \quad (4)$$

m_1, m_2, σ_1 and σ_2 are defined, respectively, by Eqs. (5), (6), (7) and (8):

$$m_1 = \sum_{i=0}^{N-1} i \sum_{j=0}^{N-1} P_\mu(i, j), \quad (5)$$

$$m_2 = \sum_{j=0}^{N-1} j \sum_{i=0}^{N-1} P_\mu(i, j), \quad (6)$$

$$\sigma_1^2 = \sum_{i=0}^{N-1} (1 - \mu_1)^2 \sum_{j=0}^{N-1} P_\mu(i, j), \quad (7)$$

$$\sigma_2^2 = \sum_{j=0}^{N-1} (1 - \mu_2)^2 \sum_{i=0}^{N-1} P_\mu(i, j). \quad (8)$$

The histogram of the grey levels is an abstract of the statistical information that is present in the image [27]. A grey-scale image, represented as a two-dimensional matrix mathematically, can be defined as a function $f(x, y)$ where $x = 1, \dots, N-1$ represents the row index and $y = 1, \dots, M-1$ represents the column index. Let G be the total number of grey-scale numbers; then the function $f(x, y)$ can take $i = 1, \dots, G-1$ discrete values. Grey-scale histogram shows the number of the pixels that have the same intensity value in the image and given by Eq. (9):

$$h(i) = \sum_{x=0}^{N-1} \sum_{y=0}^{M-1} \delta(f(x, y), i). \quad (9)$$

Here $\delta(j, i)$ is the Kronecker delta function and given by Eq. (10):

$$\delta(j, i) = \begin{cases} 1 & \text{if } j = i \\ 0 & \text{if } j \neq i \end{cases} \quad (10)$$

In Eq. (11) the probability density of the recurrence of grey level can be obtained by dividing $h(i)$ by the number of pixels in the image:

$$p(i) = h(i)/NM, \quad i = 0, \dots, G-1. \quad (11)$$

Equations (12)–(15) show that first-order texture features can be obtained using $p(i)$:

$$mean \mu = \sum_{i=0}^{G-1} iP(i), \quad (12)$$

$$variance \sigma^2 = \sum_{i=0}^{G-1} (i - \mu)^2 P(i), \quad (13)$$

$$standard deviation \sigma = \sqrt{\sum_{i=0}^{G-1} (i - \mu)^2 P(i)}, \quad (14)$$

$$kurtosis k = \sigma^{-4} \sum_{i=0}^{G-1} (i - \mu)^4 P(i) - 3. \quad (15)$$

Other than the texture features obtained conventionally from the smallest area covering the tumour (ROI), Cheng *et al* [10] have obtained texture-based features that also include a morphological feature (size) besides the texture information using together the number of lateral/depth pixels and grey-level values of ROI. Amin *et al* [28] divided the smallest rectangular area enclosing the tumour into 9 images and gathered the first-order texture features obtained from each sub-image into the sets called vertical, horizontal and central orientation. They also obtained a new texture-based feature set by dividing the texture feature values obtained from the whole ROI by the values obtained from these sets [28].

2.4 Morphological (shape, margin) features extraction

In lots of CAD systems, texture and morphological features [29] have been used together to increase the classification success rate [13, 28, 30–37]. Morphological features are independent of various ultrasound systems or machines in the diagnosis of breast cancer masses. Therefore, it is more advantageous to use morphological features in CAD systems [38] where they can also define the margin and shape

of the mass [39, 40]. The most common morphological features used in CAD systems are roundness, perimeter, area, area perimeter ratio, long-axis–short-axis ratio and most importantly the spiculation [34, 40–42]. *Roundness* is defined as the shape feature that represents the roundness of the mass shape in BI-RADS lexicon and is given by Eq. (16) [34]. A high value of roundness increases the possibility of malignancy [43]:

$$\text{roundness} = 4(\text{area})/\pi(\text{max_diameter}^2). \quad (16)$$

Here, the *max_diameter* is the length of the long axis of the equivalent ellipsis that covers the mass. *Area* is the area in pixels bounded by the contour of the shape that forms the mass. Malignant masses usually have a larger area than the benign ones [28, 42]. *Perimeter* is the measure of the mass periphery. Malignant masses have irregular shape and a higher perimeter value [44, 45]. *Ap_ratio* feature is calculated by dividing the mass area by the perimeter of the tumour and is given by Eq. (17):

$$\text{Ap_ratio} = \text{area}/\text{perimeter}. \quad (17)$$

Las_ratio is the ratio of the long axis (in pixels) to the short axis (in pixels) of the shape that forms the tumour and is given in Eq. (18). The ratio of the long axis to the short axis is an important parameter in segregation of the malignant and benign tumours. The elliptic shape of a mass is a significant feature for the mass to be classified as benign [46].

$$\text{Las_ratio} = \text{long-axis length}/\text{short-axis length}. \quad (18)$$

Spiculations are spiked contour gaps and lines out of the mass (arrows). Spiculations are the highest BI-RADS predictive value morphological features for the classification of malignancy [43, 47]. Different methods have been proposed for the calculation of spiculation. Among these methods, SI value has been calculated for every curved part of each of the mass border as the ratio of the length of the contour to the width of the floor [48]. One of the most promising methods for the description of spiculation depends on the Fourier descriptors of the image contour [49]. Here, the polar coordinates and the mass centre of the contour pixels of the mass were obtained and the radial distance was calculated. Fourier transform of the radial distance was obtained and the sum of the high-frequency components with respect to the cut-off frequency $\pi/4$ was divided by the sum of the low-frequency components; then this ratio was used as a feature [50]. In another study, the skew angle from each pixel, at the contour of the mass to the convenient pixels, was used to specify the spiculation feature. Spiculated regions have a lower skew angle (45° – 60°) [43]. In another method, the average distance between a virtual circular contour (with its centre overlapping the centre of the mass and having the same area as that of the mass) and the pixels of N tumour contours outside this circular contour was calculated and a feature was obtained to measure the spiculation [39].

2.5 Feature selection

Many features can be extracted from ultrasound images. To correctly classify and diagnose the benign and malignant masses in the breast cancer data set, it is very important to select the features in an optimal way [51]. There are many feature selection systems in the literature. They are principal component analysis (PCA) [30, 44], artificial intelligence algorithms [31], bidirectional search [29], *t*-test for selecting class-descriptor features and statistical significance tests such as Wilcoxon–Mann–Whitney (WMW) test [52] and backward feature elimination method [53].

2.6 Classification

The most common classifiers used in the classification of tumours in the ultrasound images as benign or malignant are summarized in table 1. Besides, machine learning methods such as artificial neural networks (with different topologies: multilayer perceptron, probabilistic neural network) [45, 52], fuzzy SVM [5] and *C* means (to cluster the data to *C* clusters using the least squares method) [54], statistical analysis methods (chi-square and Mann–Whitney *U* test, logistic regression classifier, Fisher’s exact test, *t* test) [3, 55], *k*-nearest neighbourhood (KNN) algorithm (classifies the test samples based on the *k* nearest training samples in the feature space) and citation KNN [56], which is an enhanced KNN algorithm, were also used as classifiers.

3. Fuzzy inference systems

Fuzzy set theory, which was proposed by Zadeh in 1965, deals with the vagueness of the information. It is less restrictive than the classical set theory and more convenient for the processing of data provided by humans. The membership or non-membership (0 or 1) in the classical set theory is mapped onto the continuous domain (0, 1) [57]. Fuzzy inference is the mapping of the given inputs to the outputs via an inference mechanism using if–then rules, membership functions and fuzzy logic. Among the fuzzy inference models, the well-known Mamdani model uses the semantic rules, union and intersection operators (max–min) [58]. This model consists of fuzzification, if–then linguistic rules and defuzzification steps. The fuzzification maps the crisp input values to the corresponding membership values using the triangular, Gaussian and trapezoidal membership functions. The histogram of the given data set is one of the methods to choose the membership function [59]. If–then rules of Mamdani algorithm are given in Eq. (19):

$$R_i : \text{if } x_i \text{ is } A_{i1} \text{ and...then } y_i \text{ is } B_i \text{ (for } i = 1, 2, 3, \dots, k). \quad (19)$$

Here *k* is the number of rules, *x* is input variable (antecedent value) and *y* is output value (consequent value).

The basic form of a fuzzy composition processing is $B = A \circ R$. Here A is the antecedent defined in the X universe. B is the consequent defined in the Y universe. R is the fuzzy relation between X and Y . The first step in Mamdani-type fuzzy inference system is the calculation of the degree of fulfilment α for each rule (i) using the membership degrees μ . It is given by Eq. (20) [60]:

$$\alpha_i = \mu_{A_{i1}}(X_1) \wedge \mu_{A_{i2}}(X_2) \wedge \dots \wedge \mu_{A_{in}}(X_n). \quad (20)$$

In the second step, the fuzzy output set B_i is derived for each rule using the t -norm. It is given by Eq. (21):

$$\mu_{B_i}(y) = \alpha_i \wedge \mu_{B_i}(y). \quad (21)$$

In the third step the output fuzzy sets are aggregated using the maximum. It is given by Eq. (22):

$$\mu_B = \max(\mu_{B_i}(y)), \quad i = 1, 2, \dots, k. \quad (22)$$

In the final step the output fuzzy set is converted to the crisp value via defuzzification. One of the methods for defuzzification is the centre of gravity (COG). It is given by Eq. (23):

$$y = \int B(y)ydy / \int B(y)dy. \quad (23)$$

3.1 Type-2 fuzzy inference system

Zadeh proposed the Type-2 fuzzy sets in 1975. Therefore, the fuzzy set that he proposed earlier was called Type 1 [61]. A fuzzy logic system (FLS) using at least one Type-2 fuzzy set is called a Type-2 FLS. The structure of the Type-2 fuzzy rules is the same as that of the Type-1 fuzzy rules except for the structure of the membership functions. Unlike Type 1, in the output process where the crisp value is calculated, it also includes the type reduction unit [62]. The membership value of each element in the Type-1 fuzzy set is described with crisp values in $[0, 1]$ while the membership value of each element in the Type-2 fuzzy set is described as fuzzy sets. Type-1 fuzzy set with n elements is defined with n fuzzy sets with a membership value of $[0, 1]$, where n fuzzy sets generate the footprint of vagueness (FOU) [59]. The recent studies on Type-2 fuzzy sets depend on the definition by Mendel [63–65]. According to this definition, instead of using the n fuzzy sets that constitute the FOU, using only the lower and upper membership functions (LMF, UMF) simplifies in obtaining the result. Therefore, the union of lower and upper membership functions is described as FOU [66]. There are various artificial intelligence optimization algorithms in the literature such as genetic algorithms [67]. The equation of FOU is given in Eq. (24), while the membership functions are shown in figure 1:

$$FOU(\hat{A}) = \cup [\bar{\mu}_{\hat{A}}(x), \underline{\mu}_{\hat{A}}(x)] / x \quad \forall x \in X. \quad (24)$$

Figure 1. Type-2 triangular membership function (UMF – upper membership function, LMF – lower membership function, FOU – footprint of uncertainty).

4. Proposed method

In this study, a total of 153 ultrasound images containing 64 benign and 89 malignant masses were used (CMSDH K, SSKM Hospital Kolkata and the webpage: <http://www.ultrasoundcases.info/About-Us.aspx> by Dr T S A Geertsma, The Netherlands). The proposed CAD system for the classification of ultrasound images consists of the following steps.

4.1 Selection of ROI

A software has been developed for an expert radiologist to mark the area containing the mass. The software also provides the pixel-based coordinate information of the marked mass contour. Using the coordinate information, the smallest rectangular area is cut off and the ROI image to extract the features has been obtained. As an example, figures 2 and 3 show, respectively, the marked area and the ROI image.

4.2 Speckle noise reduction and image enhancement

One of the most common methods to reduce the speckle noise is filtering. In this study, Gaussian filter has been used for the reduction of speckle noise reduction [16, 17]. Histogram equalization, which is used for enhancing the low visibility of an image, makes the output histogram to a uniform distribution. Contrast limited adaptive histogram equalization is another version of histogram equalization which has different equalization values for each region [68]. In this study, image enhancement has been realized using

Figure 2. Area marked by a physician.

Figure 3. ROI image of malignant case segmented from BUS image.

Figure 4. Enhanced ROI image.

Figure 5. Binary form of ROI image.

contrast limited adaptive histogram equalization. Figures 4 and 5 give the filtered enhanced image and binary image.

4.3 A novel texture-based feature set

In this study, a total of eight statistical texture features (first-order mean obtained by the whole of the ROI (TF1), kurtosis (TF2), variance (TF3) and standard deviation (TF4) obtained via the approach mentioned in section 2.3 [10] and also the contrast (HF1), homogeneity (HF2), energy (HF3) and correlation (HF4) obtained via the second-order GLCM matrix) were divided to the tumour area in pixels, which is a morphological feature. Thus a novel texture-based feature set is obtained.

4.4 Morphological features

Five morphological features, namely roundness based on the BI-RADS lexicon and the expert doctor opinion (MF1), area (MF2), area/perimeter rate (MF3), long-/short-axis rate (MF4) and most importantly spiculation (MF5), were extracted. To get these features, first, the image was converted to black and white by applying Otsu global thresholding [69] to the filtered and enhanced image. Second, the shape of the mass in the ultrasound image was tried to better expose via the morphological open-close processes [70]. The binary image is shown in figure 5. The area in white colour represents the mass while the area in black colour represents the image background. The method based on the Fourier descriptors mentioned in section 2.4 was applied with an enhancement to calculate the spiculation feature. With this enhancement, an array is constructed by calculating the distances from two adjacent pixels of the mass edge to the centre pixel. Then the Fourier transform of this array is taken and the first value of the transformed data array is chosen as a feature.

Figure 6. Proposed CAD architecture.

4.5 Feature selection

Five morphological features mentioned in BI-RADS lexicon (section 2.4) and in section 4.4 by the expert doctor [71, 72] were directly used. In the selection of texture features, the statistical method explained in section 2.5 was applied. First, the distribution over data set was investigated by applying Kolmogorov–Smirnov test via SPSS. Student’s *t*-test was applied to the data set with normal distribution while Mann–Whitney *U* test was applied to the data set without normal distribution. Subsequently, based on the *p*-value, the mean (TF1) and the contrast (HF1) were chosen as texture features [73, 74].

4.6 Classification

It is advisable to use BI-RADS lexicon in the decision process because it follows a natural language structure. The ‘If the mass is rounded and less dense, then it is more probable to be classified as benign’ rule can be conveniently modelled with fuzzy sets [75]. Adaptive neural fuzzy inference system (ANFIS) is a first-order, network-based, multi-layer and adaptive Takagi–Sugeno fuzzy inference system proposed by Jang in 1993 [76, 77]. In a study the system architecture was designed, as each ANFIS output is an input to the next ANFIS layer [78]. In this model, a multi-layer classifier architecture based on Type-2 fuzzy inference system for the CAD system is proposed. Layer 1 classifies the mass as benign or malignant. The class at the output of Layer 1 enters the category classifier at Layer 2 where the BI-RADS category of the mass is determined. The architecture of Type-2 fuzzy inference system was initially designed as Type 1 for testing purposes using the MATLAB fuzzy logic toolbox. Then the *FOU* sizes were determined using ABC optimization algorithm and the system was converted to Type-2 structure using type reduction module with the Karnik–Mendel algorithm [79, 80]. A software has been developed in Matlab for every step. The block schema of the proposed architecture is shown in figure 6. Here, $X = X_1, X_2, X_3, X_4, X_5, \text{textit{X6}}$ is the Layer 1 input feature vector, X_7 is the Layer 2 input feature vector, B/M is the benign/malignant output of Layer 1 and 2–5 are BI-RADS category output of Layer 2. Histograms were used in the design of each membership function [81]. The histograms of each feature data set in the

benign and malignant classes were extracted and the most similar fuzzy set was determined as a triangular fuzzy set. For the consequent part (or output), again triangular fuzzy sets were preferred and they were scaled as 1–3 for benign and 3–5 for malignant for the discrimination of classes. The histograms of benign and malignant data sets for *Ap_ratio* feature are given as examples in figures 7 and 8. The parameters used in the design of triangular membership functions were obtained by calculating the minimum, average and maximum values of feature data sets in each class and are given in table 2.

Mamdani-type rules were created via max–min approach by noting the medical information that the expert doctor uses during the interpretation of the ultrasound images [75]. The rules of the designed system are shown in table 3.

The BI-RADS categories were determined as 2, 3, 4 for the benign tumour and 3, 4, 5 for the malignant tumour by the expert doctor. In this study, MF4 feature was used to classify the BI-RADS categories. The method used in Layer 1 was applied to the BI-RADS categories of each class and the input/output membership functions were designed. The parameter values of benign and malignant class input membership functions are given in tables 4 and 5, respectively. The parameter values of output membership functions are given in table 6. The rules [82] of Layer 2 for

Figure 7. Histogram of benign data sets for *Ap_ratio* feature.

Figure 8. Histogram of malignant data sets for Ap_ratio feature.

Table 2. Minimum, mean and maximum values of the features.

Feature	Min	Mean	Max
MF5 B LOW	143.120	451.430	568.830
MF5 M HIGH	572.750	613.470	685.840
MF2 B LOW	721	5439	9761
MF2 M HIGH	10022	15608	31927
MF1 B LOW	0.361	2.125	3.737
MF1 M HIGH	3.563	5.360	10.316
MF3 B LOW	7.240	16.270	25.620
MF3 M HIGH	14.780	37.250	83.230
HF1 B HIGH	15.330	84.610	706
HF1 M LOW	6.950	19.240	36
TF1 B HIGH	61.177	223.600	1206
TF1 M LOW	20.076	61.990	102.910

Table 3. Layer 1 fuzzy rules of the CAD system.

Fuzzy rules	Class B/M
If MF5 is high and MF2 is low	M
If MF5 is low and MF2 is high	B
If MF2 is high and HF1 is low	M
If MF2 is low and HF1 is high	B
If MF5 is high and MF3 is high	M
If MF5 is low and MF3 is low	B
If MF5 is high and HF1 is low	M
If MF5 is low and HF1 is high	B
If MF1 is high and TF1 is low	M
If MF1 is low and TF1 is high	B

the BI-RADS classification are given in table 7. The membership functions that were initially designed as Type 1 constitute the upper membership functions in the conversion to Type 2. The optimum *FOU* for each membership function was obtained using the ABC algorithm [83]. Thus,

Table 4. Parameter values for the benign class triangular membership function (min – minimum, max – maximum).

Feature	Min	Mean	Max
MF4 - BIRADS 2 - High	1.16	2.50	3.38
MF4 - BIRADS 3 - Middle	1.23	1.74	2.20
MF4 - BIRADS 4 - Low	1.15	1.46	1.81

Table 5. Parameter values for the malignant class triangular membership function (min – minimum, max – maximum).

Feature	Min	Mean	Max
MF4 - BIRADS 3 - High	1.38	1.76	2.45
MF4 - BIRADS 4 - Middle	1.23	1.74	2.39
MF4 - BIRADS 5 - Low	1.02	1.31	1.86

Table 6. Parameter values of output membership functions (X_1, X_3, X_5 from figure 1).

BI-RADS class	X_1	X_3	X_5
Malignant BI-RADS 3	1	1.5	2
Malignant BI-RADS 4	2	2.5	3
Malignant BI-RADS 5	3	3.5	4
Benign BI-RADS 2	1	1.5	2
Benign BI-RADS 3	2	2.5	3
Benign BI-RADS 4	3	3.5	4

Table 7. Layer 2 fuzzy rules for benign/malignant class.

fuzzy rules	BI-RADS category
If MF4 is high	BI-RADS 2 - Benign
If MF4 is middle	BI-RADS 3 - Benign
If MF4 is low	BI-RADS 4 - Benign
If MF4 is high	BI-RADS 3 - Malignant
If MF4 is middle	BI-RADS 4 - Malignant
If MF4 is low	BI-RADS 5 - Malignant

the parameter values of the lower membership function were calculated. The triangular membership function is given in figure 1. Here, X_1 , X_3 and X_5 correspond to the minimum, mean and maximum values, respectively, for the given feature data set, $X_2 = X_1 + FOU$ and $X_4 = X_5 - FOU$. Optimal *FOU* sizes are given in table 8.

5. Success test

Success test was realized by a comparison of the proposed method with the common classifiers such as SVM, ANN, KNN and Type-1 FIS on correctness, sensitivity and specificity measures. The result is given in table 9. The

Table 8. FOU sizes of the input and output membership functions.

MF1	MF2	MF3	MF5	TF1	HF1	Output
5	50	5	10	2	6	0.8

Table 9. Comparison between the proposed method and other methods in terms of the success test parameters.

Classifier	Acc (%)	Sens (%)	Spec (%)
SVM	97	98	95
ANN(MLP)	98	100	97
KNN (k=8)	92	98	84
C-MEAN	72	50	100
FC-MEAN	73	54	100
LDA	89	84	97
TYPE 1 FUZZY	96	97	95
PROPOSED METHOD	99.34	100	98.44

correctness, specificity and sensitivity equations are as follows.

In Eqs. (25)–(27), TP stands for malignant classification in the case of malignant tumour, FN stands for benign classification in the case of malignant tumour, TN stands for benign classification in the case of benign tumour and FP stands for malignant classification in the case of benign tumour. In another CAD system that uses the same ultrasound image database with this study, benign/malignant classification was realized using an SVM classifier and a correctness of 95.7%, sensitivity of 87.5% and specificity of 100% were gained [30]. In another study where the BI-RADS category classification was realized using logistic regression, a correctness rate of 81% was acquired [3]. In this study, a correctness of 92% was obtained. It is observed that the proposed method is more successful when compared with these studies. The radiologists generally perform visual inspection followed by an invasive and painful procedure called biopsy for accurate diagnosis. However, the subjective way of classifying abnormal tissues in breast is an ineffective, tiresome and time-consuming job. Therefore, the proposed system provides an efficient and objective method of classifying breast tumours in ultrasound images. This system can improve the decision making and can be helpful in reducing the number of false diagnoses and biopsies. Medical costs will be reduced as well.

$$\text{Accuracy}(acc) = (TP + TN) / (TP + TN + FP + FN), \quad (25)$$

$$\text{specificity}(spec) = TN / (TN + FP), \quad (26)$$

$$\text{sensitivity}(sens) = TP / (TP + FN). \quad (27)$$

6. Conclusion and related work

There are many studies in the literature that utilize CAD systems with various architectures to help the expert doctors in diagnosis stage. They include the artificial intelligence techniques that are benefited by the superior calculation ability of the computers. The proposed design is a high-success-rate, novel CAD architecture that combines the expert doctor knowledge with the superior calculation ability of the computers and it provides more accurate information to the doctor, including the BI-RADS category of the breast cancer. In the future, conversion of the designed CAD system to a web application is planned. In the future, the researchers who study in the field of this area can save verbal expressions that contain the knowledge and experiences of doctors' diagnosis to a database with a software module that is added to web-based application. Through the analysis of the verbal expression, it is possible to improve the rule structure of fuzzy system. Through this web-based application, doctors who are even far away from each other procure the chance of sharing the interpretations on patients while analysing images of patients in real time. By this way, the accuracy of diagnosis with a CAD system is increased. Since the application provides for sharing information and experiences, the application software, which is improved by the continuous studies, can be additionally used for educational purposes. One of the advantage of web-based CAD system is that all doctors who work in this field can easily have an access to this system via internet. Furthermore, monitoring the patient by the doctor is provided for without the limitations of time and location.

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