

Size effect in self consolidating concrete beams with and without notches

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Abstract. The aim of this study is to obtain the fracture characteristics of low and medium compressive strength self consolidating concrete (SCC) for notched and un-notched plain concrete beams by using work of fracture G_F and size effect model G_f methods and comparing them with those of normal concrete and high performance concrete. The results show that; (i) with an increase in compressive strength, G_F increases and G_f decreases; (ii) with an increase in depth of beam, the decrease in nominal stress of notched beam is more when compared with that of a notchless beam.

Keywords. Size effect model; self consolidating concrete; notched beam.

1. Introduction

Self-consolidating concrete (SCC) is the hot topic of current research area today. Many intrinsic properties of the concrete are yet to be understood clearly. Concrete is prepared by proportioning materials and adding admixtures to suit the specific requirements. Large amount of mineral admixture also called cement replacement material is used for high performance concrete (HPC) and SCC to make concrete dense and economical (Albiero 2001; Mata 2004). The differences between HPC and SCC is essentially in the use of special admixture (Kishi *et al* 2000) i.e. high range water reducing admixture (HRWR). The use of HRWR and viscosity-modifying admixture (VMA) can provide a high degree of fluidity and segregation resistance to SCC, a distinct advantage over HPC (Bury & Christensen 2002). Polyacrylate-based super plasticizers are more efficient to reduce the porosity of matrix (Biolzi *et al* 1997). Due to the use of chemical and mineral admixtures, the micro cracks studies are essential in SCC than in normal concrete (NC) (Druta 2003; Wittmann 2002).

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The improved pore structure and better densification of matrix have bearing on the fracture characteristics like fracture energy G_F and critical stress intensity factor K_{Ic} . It has been reported that increased density will increase the compressive and tensile strengths of concrete as well as fracture energy (Giaccio *et al* 1993). It will decrease the characteristic length (Haidar & Cabor 2002). Many investigators have evaluated the mechanical characteristics and durability of SCC mixes. SCC is more porous and has lesser density compared to HPC.

Fracture behaviour of plain concrete is the basis for all the studies on behaviour of reinforced concrete and pre-stressed concrete structures via fracture mechanics. Experimental studies conducted by many researchers show that, with increase in the size of aggregate, there is a decrease in the brittleness of hardened concrete and increase in both the fracture energy as well as the fracture toughness of concrete (Amparano *et al* 2000; Appa Rao & Raghu Prasad 2002; Strange & Bryant 1979).

As pointed out by Bazant & Pfeiffer (1987); Bazant & Kazemi (1990), the fracture energies G_F and G_f are two different material characteristics. The fracture energy G_F is obtained by the area under the complete load-deflection curve, and the fracture energy G_f is represented by the area under the initial tangent of the softening curve. It has been shown that the fracture energy G_f (Bazant & Giraudon 2002; Ta-Peng & Mei-Miao 1996; Perdikaris & Romeo 1995) increases with increasing in compressive strength. Notchless beams have not been tested sufficiently in the past. A very few experimental results are available (Karihaloo & Xiao 2002; Kim & Eo 1990) on notchless beams. Determination of fracture characteristics of geometrically similar beams with and without notches are of particular interest for SCC.

2. Research significance

There are many studies on fracture characteristics of notched beams and only a few on notchless beams in literature. The present study is aimed at documenting effects of size both in notch and notchless beams in SCC using size effect model. The objectives of the present work are listed below:

- (i) The influence of notch on fracture characteristics such as fracture energies G_F , G_f , K_{Ic} , critical energy release rate (G_{Ic}) and characteristic length (l_{ch}) in SCC beams under three point bend condition.
- (ii) Size effect model (SEM) for notched and notchless beams.
- (iii) Influence of compressive strength on fracture energies G_F and G_f .
- (iv) Effect of notch on brittleness of concrete structure.

3. Evaluation of fracture characteristics

3.1 Size effect model (SEM)

In the method proposed by Bazant & Pfeiffer (1987), the fracture energy is determined from the size effect model. If geometrically similar beams are used and loaded up to rupture and extrapolated to a beam of infinite dimensions, the fracture energy must have one single value, regardless of the type, size or shape of the specimen. Bazant and Pfeiffer suggested the following relationship:

$$\sigma_N = \frac{Bf_t}{(1 + b/b_o)^{1/2}}, \quad (1)$$

where $\sigma_N = C_n \frac{P_u}{bd}$ is the nominal stress at failure, f_t is the tensile strength, P_u is the ultimate load and C_n is a coefficient introduced for convenience.

The coefficients B and b_o are determined by linear regression. For this purpose, equation (1) applicable to geometrically similar specimens of different sizes, can be algebraically rearranged to a linear regression form $Y = AX + C$, in which:

$$Y = (1/\sigma_N)^2; X = d; b_o = C/A; B = 1/\sqrt{C}. \tag{2}$$

The concrete fracture process zone size is small in an infinite size specimen. In this case, the fracture energy G_f and fracture process zone c_f respectively for infinitely large specimens are calculated as:

$$G_f = \frac{g(\alpha)}{AE}, \tag{3}$$

$$c_f = \frac{g(\alpha) C}{g'(\alpha) A}, \tag{4}$$

$$g(\alpha) = (S/b)^2 \pi \alpha [1.5g_1(\alpha)]^2 \text{ and } g'(\alpha) = dg(\alpha)/da, \tag{5}$$

where $g_1(\alpha)$ is shown in equation (8) for $S/b = 4$, E is the Young’s modulus of elasticity of the concrete, A is the angular coefficient of the linear regression plot, $g(\alpha)$ is the non-dimensional energy release rate calculated according to LEFM and α is the relative notch to depth ratio (a/b).

3.2 Fracture energy from work-of-fracture (G_F)

Many methods have been recommended to determine the fracture energy and characteristic length, using simple three point bending test (Mindess 1984; Petersson 1980a; Petersson 1980b; Tang *et al* 1996; Belhamei *et al* 2002; Elices *et al* 1997; NT Build 491,1999; Guinea *et al* 1992; Elices *et al* 1992). One can apply the recommendation of the Technical Committee RILEM (RILEM FMC-50, 1985) to perform three-point bend tests in notched beams. The Fracture energy is defined as the amount of energy necessary to create a crack of unit surface area projected in a plane parallel to the crack direction. As the beam is split into two halves, the fracture energy can be determined by dividing the total dissipated energy by the total surface area of the crack. According to the RILEM (RILEM FMT 89, 1990) fracture energy can be calculated as

$$G_F = \frac{W_0 + 2mg\delta_0}{t(b - a)}, \tag{6}$$

where G_F = fracture energy (N/m), W_0 = area under the force-deflection curve (Nm), m = weight of the beam between supports (kg), t = thickness; b = depth; δ_0 = Displacement corresponding to $P = 0$ in the post peak region and a = initial notch of the beam.

3.3 Fracture toughness

The fracture toughness K_{Ic} is calculated according to the RILEM (RILEM TC89-FMT, 1991) using the equation

$$K_{Ic} = 3(P_0) \frac{S\sqrt{\pi}ag_1(\alpha)}{2b^2t} \quad [\text{MPa}\sqrt{m}] \tag{7}$$

in which

$$g_1(\alpha) = \frac{1.99 - \alpha(1 - \alpha)(2.15 - 3.93\alpha + 2.7\alpha^2)}{\sqrt{\pi}(1 + 2\alpha)(1 - \alpha)^{3/2}}, \quad (8)$$

where $\alpha = a/b$, $P_0 =$ the measured maximum load [N] + self weight of the beam [N]. The result correspond to the mean values of three tests. The critical energy release rate G_{Ic} is related to K_{Ic} as:

$$G_{Ic} = (K_{Ic})^2/E. \quad (9)$$

3.4 Intrinsic brittleness

It is well known that the brittleness of concrete is characterized not only by the fracture toughness but also by a measure of the length of the fracture process zone. The smaller the length, more brittle is the material. According to the fictitious crack model (FCM) (Hillerborg *et al* 1976), the brittleness can be expressed:

$$l_{ch}(\text{mm}) = EG_F/f_t^2, \quad (10)$$

where f_t is the tensile strength (MPa).

3.5 Brittleness of concrete structure

The brittle response of a concrete structure should not be confused with the intrinsic brittleness of concrete. The brittleness of concrete structural elements depends on their size. Small sized elements fail in ductile or plastic manner, while large sized elements of the same material fail in brittle and often in catastrophic manner. Bazant & Pfeiffer (1987) and Bazant & Kazemi (1990) proposed the structural brittleness number $1/\beta$, which reflects the geometry and initial notch depth of the specimen, besides intrinsic brittleness of concrete and structural size. It is expressed by the following equation:

$$\beta = \frac{b}{b_o}, \quad (11)$$

where b is the characteristic dimension of the structure (the specimen height in this study) and b_o is a coefficient determined experimentally.

4. Experimental study

4.1 Material properties and mix proportions

The cement used was 53 grade, having 3, 7 and 28 days strength as 263.50, 33.20, and 53.40 MPa, respectively. Crushed granite aggregates having maximum size of 16 mm were used. The specific gravity, dry-rodded unit weight, and water absorption of the coarse aggregate were 2.71, 1, 550 kg/m³ and 0.5 by weight of the aggregate, respectively. River sand passing 4.75 mm sieve was used. The specific gravity of the sand was 2.62 and the fineness modulus was 2.48. Class F fly ash from the thermal power plant near Raichur, India, was used. The quantities of materials for various mixes of SCC (SCC1, SCC2 and SCC3) are listed in table 1.

Table 1. Quantities of material for SCC kg/m³.

Materials	SCC1	SCC2	SCC3
Cement (kg)	240	400	360
Water (kg)	220	180	190
Fine Agg. (kg)	900	900	900
Coarse Agg. (kg)	830	830	830
Fly ash (kg)	184	200	196
Silica fume (kg)	12	36	29
HRWR (liter)	2.00	4.00	3.50
AEA (liter)	0.20	0.24	0.40
VMA (liter)	0.50	1.50	1.25

5. Analysis of results

5.1 Fresh and mechanical properties of SCC

The fresh and hardened properties of SCC were obtained by conducting tests and the results are listed in tables 2 and 3.

Table 2. Fresh properties of SCC.

Tests	SCC1	SCC2	SCC3
Slump Flow (mm)	750	700	670
T50 cm Slump Flow	3	4	5
J-ring (mm)	3.2	3	8
V-funnel (Sec)	4	6	7
V-funnel at T5	2	3	3
L-box (H2/H1)	0.8	1	0.95
U-box (H2-H1)	5	3	5
Fill-box(%)	95	95	95

Table 3. Mechanical properties of SCC.

Mix	Density kg/m ³	f_c MPa	E GPa	f_t MPa	f_r MPa
SCC1	2044	17.1	17	1.5	2.6
	2074	16.8	17	1.8	2.7
	2074	16.1	16.5	1.7	3.0
SCC2	2006	29.8	21	2.7	4.2
	1956	30.4	22	2.7	4.2
	2010	31.4	22	2.7	4.2
SCC3	2163	45	28	3.4	6.2
	2133	46	28.2	3.4	6.3
	2104	43	27	3.4	5.9

5.2 Fracture energies G_F, G_f

Geometrically similar specimens with three different sizes were used in order to allow the fracture energy evaluation through the SEM besides the work-of fracture method. To study the size effect, the beam specimens were loaded under three point bend condition. The beam specimens were geometrically similar in two-dimensions; viz. (i) the ratio of the span to the depth of the beam (S/b) was 4 for all the specimens; (ii) the ratio of the notch/depth (a_0/b) equal to 0.33 and 0.01 for the (B1, B2, B4) and B3 respectively. The depth (b) of specimens were 50 mm, 100 mm, and 200 mm, with the lengths equal to $4 \cdot 2b$, and span equal to $4b$. The thickness of all beams was 50 mm, which was determined by considering the maximum aggregate size (16 mm) to make sure that the thickness of the beams is larger than three times the maximum aggregate size. A total of 36 specimens, divided in three series of concrete batches (SCC1 to SCC3) were cast. Each series contained three specimens for each of the batches.

The equipment used to test the beam specimens was with three channels for data acquisition and a load cell of 50 kN capacity. All the tests were conducted under the CMOD control. The notch was made at the time of casting using an acrylic plate with a thickness of 2 mm.

From figure 1 in a typical force-deflection and force-CMOD curve for the specimens B2. Due to the CMOD control it is evident that, the pre-peak stiffness of force-displacement curve is more than that of force-CMOD.

Table 4 shows the corrected maximum loads for all the tested beams, which were obtained by adding half the beam self weight to the measured peak load, in order to consider the effect of the self weight of the specimen for fracture energy calculations (RILEM FMT 89, 1990).

The fracture energy, G_f , can be calculated by using equation (3) together with the values of B, b_0 , and E of each group of specimens with a specific f_c . The non-dimensional energy release rate $g(\alpha)$ is obtained from equation (5) for $g(0.33)$ and $g(0.01)$. The numerical value of $g'(\alpha)$ in equation (4) is calculated using Matlab.

From the geometrically similar specimens in two-dimensions, fracture energies G_f and G_F are obtained by the work of fracture method and size effect model. It was seen that the values obtained for the fracture energy G_F are greatly affected by the size of the specimen. The values of fracture energies G_F, G_f according to the work of fracture and size effect model methods are listed in table 5. The standard requirements concerning the limiting values of the coefficient of variation of the slope of the regression line (w_A) and the relative width of scatter-band (m) and the values of w_A and m should not exceed 0.10 and 0.20 respectively.

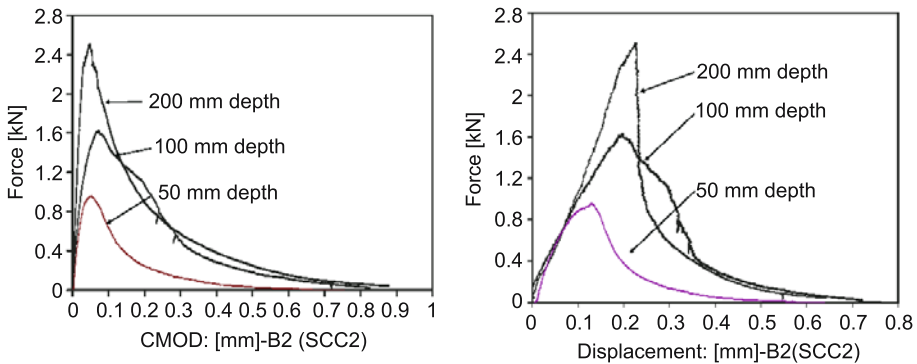


Figure 1. Typical force vs CMOD/displacement for mixes B2(SCC2).

Table 4. Corrected maximum load for series B1 to B4, $S = 4b$.

Series B, Concrete	f_c	a/b	Corrected maximum load $P_0(N)$ Beam Depth b (mm)								
			50			100			200		
			1	2	3	1	2	3	1	2	3
B1(SCC1)	15	0.33	745	707	726	1341	1431	1377	2286	2346	2386
B2(SCC2)	30	0.33	877	836	900	1560	1620	1540	2536	2636	2606
B3(SCC2)	30	0	1973	2121	2065	3421	3441	3541	6200	6100	6050
B4(SCC3)	45	0.33	1072	1030	1017	1951	1881	1921	2786	2936	2836

The following conclusions could be drawn from the table 5 for beams with and without notches under three point bend condition to investigate size effects: (i) values of K_{Ic} varies from 0.6 to 0.75 MPa \sqrt{m} , which is similar to previous investigations for light weight concrete on geometrically similar beams (Ta-peng & Mei-Miao 1996). With an increase in compressive strength of SCC, there is an increase in the fracture toughness for notched and notchless beams. There is a significant difference between K_{Ic} of notched and notchless beams. It may be stated that in practice the beams are notchless and hence the value of K_{Ic} is over estimated which is also mentioned by Barr *et al* (1985); (ii) it is observed that the G_{Ic} normally varies between 17 and 40 N/m for geometrically similar specimens (Bharatkumar *et al* 2005), while G_{Ic} varies between 10 and 25 N/m for notched beam and between 2 and 5 N/m for notchless beam. The variation of K_{Ic} is also reflected in the corresponding toughness value G_{Ic} , since K_{Ic} , and G_{Ic} are directly related as per equation (9); (iii) it is confirmed that, the fracture energy G_F increases with an increase in the depth of beam as well as an increase in compressive strength and (iv) fracture energy G_f and fracture process zone length c_f are increased with decrease in compressive strength as pointed out by Bazant & Pfeiffer (1987).

The size effect plot is shown in figure 2 for SCC beams with various compressive strengths, clearly show that, the present test results fall into the range of the transition zone between the fracture mechanics size effect and the horizontal line representing the strength criterion (Bazant & Kazemi 1990). When fracture process zone is small, the failure pattern is more brittle and falls in the region of linear elastic fracture mechanics (LEFM). This means that SCC 45 MPa is more brittle than SCC 15 MPa.

The test results of SCC are compared with the results from HPC and plotted in figure 2, for beams with depths (b) equal to 50 mm, 100 mm and 200 mm and compressive strength of 47 MPa. High performance concrete (Bharatkumar 2003) of 47 MPa is relatively more brittle than SCC of 45 MPa as can be seen clearly from figure 2. The point pertaining to HPC is to the right of SCC. It can be interpreted that, the SCC is less size dependent than HPC.

It can be seen that the test data lie close to the predictions of the size effect model. Figure 3 shows the best fits through the results obtained experimentally in a plot of $\log(\sigma_N)$ vs. $\log(b)$. The curve of HPC tends to be asymptotic to LEFM behaviour much faster i.e. for smaller value of $\log(b)$ compared to that of SCC. The curve of SCC is flatter, with their tangents tending to become asymptotic to the LEFM line at larger values of $\log(b)$.

5.3 Notchless SCC beams

Notchless beams have not been tested sufficiently in the past. A very few data are available (Karihaloo & Xiao 2002; Kim & Eo 1990) for notchless beams. In the present work notchless

Table 5. Fracture characterize obtained from the size effect model, $S = 4b$.

Series	b		a	f_c MPa	E GPa	a/b	P_0 N	K_{Ic} MPa \sqrt{m}	G_{Ic}	G_F	G_f	A mm $^{-1}$ MPa $^{-2}$	w_A	m
	mm	mm												
B1	50	16.50	15	17.4	0.33	720	0.42	10.3	67	39	0.044	0.086	0.102	
B1	100	33.00	15	17.4	0.33	1360	0.57	18.3	82	39	0.044	0.086	0.102	
B1	200	66.00	15	17.4	0.33	2250	0.66	25.1	90	39	0.044	0.086	0.102	
B2	50	16.50	30	24.6	0.33	880	0.52	10.9	88	34	0.045	0.0595	0.095	
B2	100	33.00	30	24.6	0.33	1590	0.66	17.7	95	34	0.045	0.0595	0.095	
B2	200	66.00	30	24.6	0.33	2580	0.76	23.3	103	34	0.045	0.0595	0.095	
B4	50	16.50	45	30.2	0.33	1035	0.61	12.3	93	32	0.045	0.0727	0.153	
B4	100	33.00	45	30.2	0.33	1920	0.80	21.1	105	32	0.045	0.0727	0.153	
B4	200	66.00	45	30.2	0.33	2800	0.82	22.4	108	32	0.045	0.0727	0.153	
B3	50	0.50	30	24.6	0.01	2070	0.22	1.9	N/A	11	0.0044	0.197	0.11	
B3	100	1.00	30	24.6	0.01	3480	0.26	2.7	N/A	11	0.0044	0.197	0.11	
B3	200	2.00	30	24.6	0.01	6600	0.35	4.9	N/A	11	0.0044	0.197	0.11	

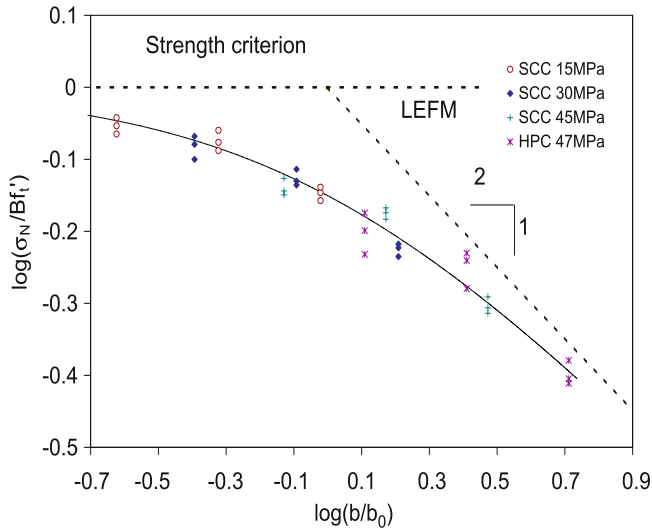


Figure 2. Comparisons of size effect plot for SCC and HPC (Raghu Prasad *et al* 2005).

SCC beams were tested and the results corresponding to compressive strength of 30 MPa are presented in figures 4 and 5. The G_f has been obtained using the peak loads. It can be seen that the test data lie close to the predictions of the size effect law. From figure 5 it is seen that with increase in depth of beam, the decrease in nominal stress of notched beam is more when compared to that of a notchless beam. It could be due to the fact that notched beam in SEM is more brittle compared with a notchless beam. Results on SCC specimens show that the trend follow findings of (Karihaloo & Xiao 2002) on high strength concrete (HSC), we observe from figure 5 that the curve is asymptotically touching the size effect plot of a notchless beam from below, while it reaches from above for a notched beam. Further, an interpretation from the laws of physics would be more appropriate to analyse the size effect plot. The interpretation

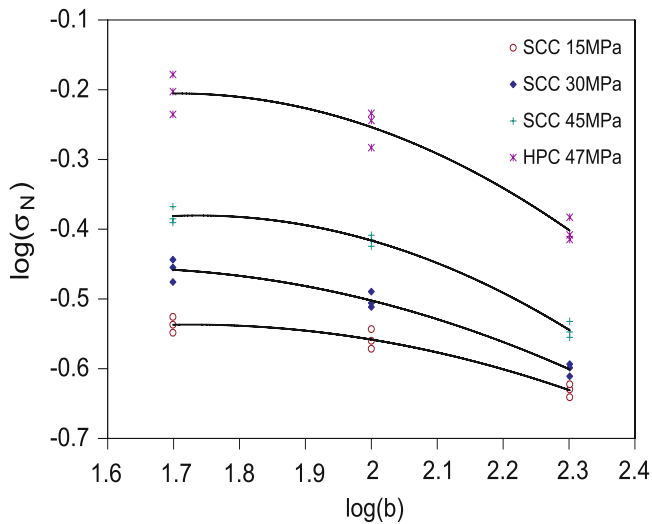


Figure 3. Comparative response of SCC and HPC for the size variation.

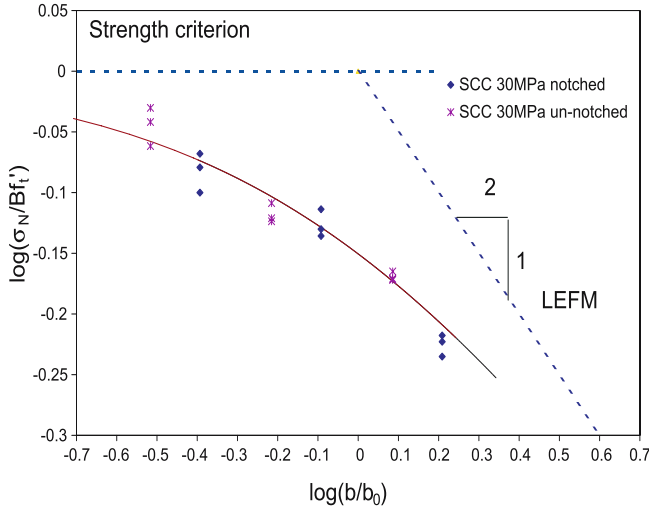


Figure 4. Size effect plot of notched and notchless beams for SCC.

could be the following; the curve asymptotically touches plot for SCC from below means that it is more ductile, because it tries to reach the LEFM behaviour at very large sizes. Such behaviour is not seen for HSC, which means that HSC is relatively more brittle.

5.4 Intrinsic brittleness and brittleness of structure

The intrinsic brittleness numbers based on FCM as per equation (10) and size effect model equation (4), were calculated accordingly and presented in table 6. The l_{ch} is found to vary between 266 mm to 446 mm, which is in the range reported in literature (i.e. 200–500 for NC, 150–300 for HSC (Karihaloo 1995) and for HPC is 120–450 mm (Bharatkumar et al 2005)). It is seen that as the concrete strength increases l_{ch} value decreases which indicates a trend towards brittle behaviour. The l_{ch} also seems to depend on the size of the specimen and it increases with increase in size.

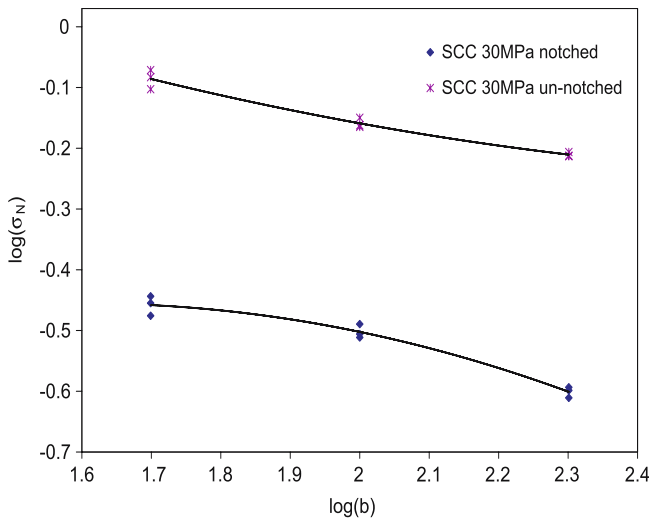


Figure 5. Comparative response of notched and notchless beams for SCC for the size variation.

Table 6. Intrinsic brittleness values of SCC and brittleness of structure (B1, B2 and B4, S = 4b).

Series	<i>b</i>	<i>a</i>	<i>f_c</i>	<i>l_{ch}</i>	<i>c_f</i>	<i>β</i>
B1	50	16.50	15	332.7	41.2	0.24
B1	100	33.00	15	407.2	41.2	0.48
B1	200	66.00	15	446.9	41.2	0.95
B2	50	16.50	30	309.0	24.25	0.40
B2	100	33.00	30	333.5	24.25	0.81
B2	200	66.00	30	361.6	24.25	1.62
B4	50	16.50	45	266.6	13.21	0.74
B4	100	33.00	45	301.0	13.21	1.48
B4	200	66.00	45	309.6	13.21	2.97

The relationship between the intrinsic brittleness of SCC for various depths of beams and the compressive strengths is derived from figure 6 and the following relationship between *l_{ch}* and *f_c* are obtained:

$$l_{ch} = 800\alpha_F(f_c)^{-0.3}, \tag{12}$$

where empirical constant, $\alpha_F = 1, 1.5$ and 1.3 for various depth of beam 50 mm, 100 mm and 200 mm, respectively.

This relationship is similar to equation (13) which was proposed for HPC (Bharatkumar *et al* 2005)

$$l_{ch} = 780(f_c)^{-0.3}. \tag{13}$$

The comparison of *l_{ch}* from SCC and HPC indicates that brittleness increases with increase in compressive strength, depth of beam and size of aggregate. It is also seen that the empirical

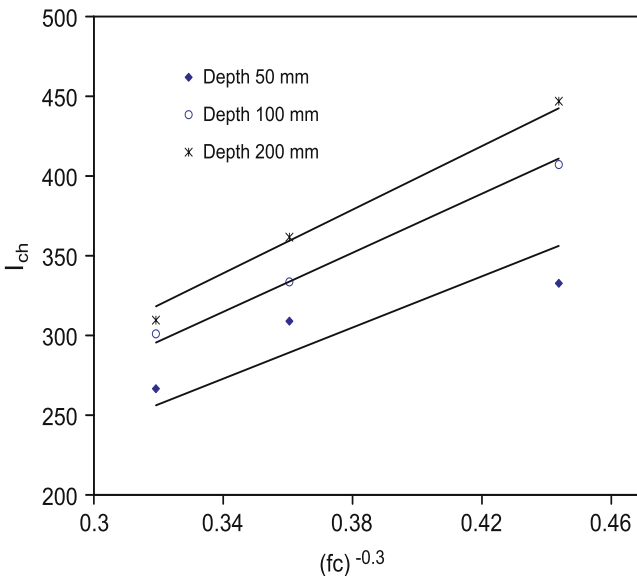


Figure 6. Intrinsic brittleness of concrete beam of SCC for the size variation.

Table 7. Values of β corresponding to the structural design (Bazant & Pfeiffer 1987; Bazant & Kazemi 1990).

Values of β	Structural design
$\beta = 1$	strength and the LEFM approach
$\beta \leq 0.1$	plastic limit analysis
$\beta \geq 10$	LEFM
$0.1 < \beta < 10$	nonlinear fracture mechanics

constant for SCC is more than that for HPC, which indicates the intrinsic brittleness, as per FCM is more in SCC compared to HPC.

Intrinsic brittleness of SCC as per size effect model is found to be varying from 13 mm to 41 mm, The range reported in literature (Bazant & Kazemi 1990; Gettu *et al* 1990; Bharatkumar *et al* 2005), show that the c_f ranges between 6 and 15 for mortar, 10–25 for NC, 3–6 for HSC and 5–15 for HPC. The values obtained for SCC fall in this range. It is evident from table 6 that the fracture process zone reduces as the strength increases due to increase in density of concrete. The c_f is found to be higher for SCC compared to HPC. This could be due to either SCC is more ductile or the length of fracture process zone is larger. As can be seen from literature, the values of G_f and c_f both together will increase or decrease. It can be seen from table 5 that the c_f and G_f both decrease with an increase in the compressive strength of SCC.

The brittleness of concrete structure based on equation (11) are given in table 6, which show that value $1/\beta$ is decreasing with increase in the characteristic size (in present case the depth of beam). The values of β for various design approaches are given in table 7.

It is pointed out by (Bazant & Pfeiffer 1987) that β is capable of characterizing the type of failure (brittle or ductile) regardless of structural geometry. It quantifies the proximity of the behaviour of a structure to LEFM and therefore $1/\beta$ is convenient tool to measure the brittleness of structure or specimen.

6. Conclusions

Experiments were conducted to determine fracture properties of SCC notched and notchless beams under three-point bend condition. The main conclusions could be drawn from this study are:

- (i) The results obtained by the work-of-fracture method show that fracture energy increases as the compressive strength of the concrete increases. Nevertheless, the results on fracture energy obtained by the SEM show a slight trend to decrease with increasing compressive strength.
- (ii) On the size effect plot, the nominal strength of SCC beams shift from left to the right with increasing compressive strength of SCC, which means that an increasing compressive strength of SCC the failure mechanisms shift to brittle region of linear elastic fracture mechanics.
- (iii) The asymptotic curve of SCC touching the plot from below means that it is more ductile, because it tries to reach the LEFM behaviour at larger sizes. Such behaviour is not seen for HSC, which means that HSC is relatively larger brittle.

- (iv) The values of characteristic length of SCC l_{ch} and c_f are more when compared with HPC, NC and HSC. It may be concluded that SCC is more ductile compared to other aforementioned concretes.

Notation

SCC	Self consolidating concrete
G_F	Fracture energy from work-of-fracture (N/m)
G_f	Fracture energy from size effect model (N/m)
HPC	High performance concrete
HRWR	High range water reducing
VMA	Viscosity modifying agent
NC	Normal concrete
K_{Ic}	Critical stress intensity factor for mode I fracture (LEFM)
l_{ch}	Characteristic length (mm)
G_{Ic}	Critical energy release rate
SEM	Size effect model
b	Depth (mm)
σ_N	Nominal stress at failure
P_u	Ultimate load
d	Length from bottom face of a specimen to roller axis (mm)
c_f	Length of fracture process zone (mm)
$g(\alpha)$	Crack opening profile function
α	Relative notch depth ratio
A	Slope of regression plot
$1/\beta$	Structural brittleness number
a	initial notch of the beam (mm)
LEFM	Linear elastic fracture mechanics
W_0	Area under the force-deflection curve (Nm)
m	Weight of the beam between supports (kg), Scatter-band
t	Thickness (mm)
δ_0	Displacement corresponding to $P = 0$ in the post peak region
P_0	Maximum load [N] + self weight of the beam [N]
FCM	Fictitious crack model
$1/\beta$	Structural brittleness number
f_c	Compressive strength of concrete (MPa)
f_r	Modulus of rupture (MPa)
f_t	Splitting Tensile Strength (MPa)
E	Young's modulus of elasticity (GPa)
CMOD	Crack mouth opening displacement
S	Span
AEA	Air entraining admixture
HSC	High strength concrete
MPa	Mega Pascal
W_A	Coefficient of variation of the slope of the regression line
(m)	Width of scatter-band

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