

THINK IT OVER

The 'Then' in (2) is equivalent to

$$a^3y^3 - 3a^2y^2x + 3axyx^2 = \frac{bz}{x}, \text{ and therefore to}$$

$$3ax^2 - 3a^2xy + a^3y^2 = \frac{bz}{xy}.$$

The two conditions in (2) are therefore equivalent iff

$$\frac{1}{3a} = \frac{3}{3a^2} = \frac{3}{a^3} = \frac{1}{b}.$$

These lead to $a = 3$ and $b = 9$, as claimed.

We can deduce an analogous result for quadratics, by arguing in the same way. The result is:

$$\text{If } (x + y)^2 = \frac{z}{y} + y^2, \text{ then } (4y + x)^2 = \frac{8z}{x} + x^2.$$

This may be stated using radicals as:

$$\text{If } x = -y + \left(\frac{z}{y} + y^2\right)^{1/2}, \text{ then } 4y = -x + \left(\frac{8z}{x} + x^2\right)^{1/23}.$$

We leave the proof to the reader.

A Problem in Graph Theory

A conference of ' n ' leaders is proposed to be held (where ' n ' is an odd number). Suppose that the organisers decide to conduct it in such a way that the leaders will have their dinner together at a circular table and each leader will have different neighbours on each day. Then

- 1) For how many days will the leaders have to meet to have all combinations and arrangements?
- 2) How can the leaders be arranged in their position each day?

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