

## Anomalous top magnetic couplings

G GONZÁLEZ-SPRINBERG<sup>1</sup>, R MARTINEZ<sup>2,\*</sup> and JORGE VIDAL<sup>3</sup>

<sup>1</sup>Instituto de Física, Facultad de Ciencias, Universidad de la República, Montevideo, Uruguay

<sup>2</sup>Departamento de Física, Universidad Nacional, Bogotá, Colombia

<sup>3</sup>Departament de Física Teòrica Universitat de València, Burjassot, València, Spain

\*Corresponding author. E-mail: remartinezm@unal.edu.co

**Abstract.** The real and imaginary parts of the one-loop electroweak contributions to the left and right tensorial anomalous couplings of the  $tbW$  vertex in the Standard Model (SM) are computed.

**Keywords.** Top; anomalous.

**PACS Nos** 14.65.Ha; 12.15.Lk

Top quark physics at the Large Hadron Collider (LHC) is an important scenario for testing physics above the electroweak scale [1,2]. Some effects related to the top anomalous couplings, both in the  $t \rightarrow bW^+$  polarized branching fractions and in single top production at the Tevatron and at the LHC, have already been studied in recent years. One-loop QCD and electroweak contributions to the  $tbW$  vertex have been studied in the frame of the Standard Model (SM) [3]. The explicit dependence of the polarized branching fractions on the anomalous couplings have been computed in refs [4,5].

We compute the electroweak SM contribution to the left and right ‘magnetic’ tensorial couplings of the  $tbW$  vertex. We found that the electroweak contribution is also at the level of 10% with respect to the leading gluon exchange. For on-shell particles, the amplitude  $\mathcal{M}_{tbW}$  can be written in the following way:

$$\mathcal{M}_{tbW^+} = -\frac{e}{\sin\theta_W\sqrt{2}} \epsilon^{\mu*} \bar{u}_b \left[ \frac{i\sigma_{\mu\nu}q^\nu}{m_W} (g_L P_L + g_R P_R) \right] u_t. \quad (1)$$

One-loop QCD gluon exchange contribution to  $g_R$  was computed in ref. [6],  $g_R^{\text{QCD}} = -6.61 \times 10^{-3}$ . The sensitivity to  $g_R$  will be accessible to the LHC experiments [2,5]. The left tensorial term couples a right  $b$ -quark and thus it is proportional to  $m_b$ . Then, constraints on  $g_L$  are stronger than  $g_R$  due to the chiral  $m_t/m_b$  factor.

Indirect limits on  $g_L$  and  $g_R$  can be obtained from  $b \rightarrow s\gamma$  [7]. The results from the analysis given in refs [8] and [9] are given in the first line of table 1; the second and third lines show  $g_L$  and  $g_R$  limits predicted for the future LHC data [5]. The LHC will improve the sensitivity to  $g_R$  by an order of magnitude compared to bounds from  $b \rightarrow s\gamma$ . In the same way as it is done in Tau physics [10], new asymmetry observables derived from

**Table 1.** Bounds on  $g_R$  and  $g_L$ .

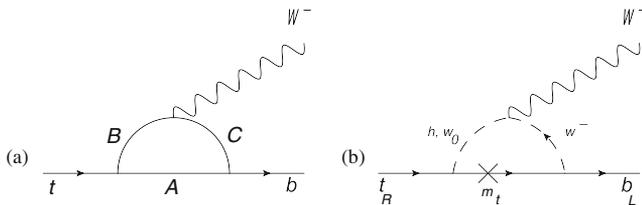
| Reference                     |           | $g_R$ Bound   | $g_L$ Bound  |
|-------------------------------|-----------|---|--|
| $bs\gamma$                    | 95% CL    | $-0.15 < g_R < 0.57$  | $-0.0015 < g_L < 0.0004$   |
| Future LHC data               | $2\sigma$ | $-0.026 \leq g_R \leq 0.031$  | $-0.058 \leq g_L \leq 0.026$   |
| Future LHC data               | $1\sigma$ | $-0.012 \leq g_R \leq 0.024$  | $-0.16 \leq g_L \leq 0.16$   |
|                               |           | $g_R$ Discovery limit   | $g_L$ Discovery limit  |
| Helicity fractions of the $W$ | $3\sigma$ | $ \text{Re}(g_R)  \geq 0.056$   | $\text{Re}(g_L) \geq 0.051$ or<br>$\text{Re}(g_L) \leq -0.083$   |
| $bs\gamma$                    | $3\sigma$ | $ \text{Im}(g_R)  \geq 0.115$<br>$\text{Re}(g_R) \geq 0.76$ or<br>$\text{Re}(g_R) \leq -0.33$ | $ \text{Im}(g_L)  \geq 0.065$<br>$\text{Re}(g_L) \geq 0.0009$ or<br>$\text{Re}(g_L) \leq -0.0019$<br><br>$ \text{Im}(g_L)  \geq 0.006$ |

helicity fractions for polarized  $W$  were defined for polarized top decays; the exclusion intervals derived from these observables are shown in the fourth line of table 1. As a reference for the comparison with the LHC, they also derived as  $3\sigma$  discovery limits from  $b \rightarrow s\gamma$  in ref. [9]; this is shown in the last line of table 1.

At one loop in the SM, there is only one topology for the diagrams that contribute to the anomalous  $g_R$  and  $g_L$ : this is shown in figure 1a. For  $g_R$  there are two diagrams that have a leading  $m_t$ -mass. They are the ones in figure 1b with  $thW$  and  $tw_0W$  circulating in the loop, where  $h$  is the Higgs boson and  $w_0$  is the unphysical  $Z$ -boson. These two diagrams have top mass insertions that give a mass dependence which is of the order  $1/r_W^2 = 1/(m_W/m_t)^2$  with respect to the other diagrams. Some diagrams, like  $bWZ$  for example, contribute to the imaginary part of  $g_R$ .

The result for each contribution of the diagrams to  $g_R$  and  $g_L$  is given in table 2, with  $m_h = 150$  GeV. The final result for the one-loop electroweak correction is

$$g_R^{\text{EW}} = -(0.56 + 1.23i) \times 10^{-3}, \quad g_L^{\text{EW}} = -(0.92 + 0.14i) \times 10^{-4}. \quad (2)$$



**Figure 1.** (a) Topology of the one-loop SM Feynman diagrams for the quantum correction to the  $t \rightarrow bW^+$  decay. (b) Leading order diagrams for  $g_R$  in the large  $m_t$  limit.

**Table 2.** Electroweak contributions to  $g_R$  and  $g_L$ .

| Diagram                   | $g_R \times 10^3$              | $g_L \times 10^3$     |
|---------------------------|--------------------------------|-----------------------|
| $tZW$                     | -1.176                         | -0.0141               |
| $thW$                     | 0.220                          | 0                     |
| $tw^0w^-$                 | 0.344                          | 0.0051                |
| $hw^-$                    | 0.462                          | -0.0088               |
| $tZw^-$                   | -0.050                         | -0.0012               |
| $t\gamma W + t\gamma w^-$ | 0.572                          | -0.0094               |
| $bWZ$                     | $-0.623 - 0.664i$              | $-0.0201 - 0.0214i$   |
| $bWh$                     | 0                              | $0.0086 - 0.0120i$    |
| $bw^+w^0$                 | $(1.5 + 11.0i) \times 10^{-4}$ | $-0.0029 - 0.0167i$   |
| $bw^+h$                   | $(-4.3 + 8.6i) \times 10^{-4}$ | $-0.0019 + 0.0111i$   |
| $bw^+Z$                   | $-0.088 - 0.062i$              | $-0.00039 - 0.00028i$ |
| $bW\gamma + bw^+\gamma$   | $0.114 - 0.509i$               | $-0.0270 + 0.0250i$   |
| $Ztb$                     | -0.397                         | -0.0067               |
| $\gamma tb$               | 0.068                          | 0.0115                |
| $w^0tb$                   | $-6.8 \times 10^{-4}$          | -0.0109               |
| $htb$                     | $-6.2 \times 10^{-4}$          | -0.0135               |
| $\Sigma(EW)$              | $-0.56 - 1.23i$                | $-(0.092 + 0.014i)$   |
| $gtb$                     | -6.61                          | -1.12                 |

We note that for  $g_L^{\text{EW}}$  is 8% of  $g_L^g$ , and also that the CP violation has its origin in the electroweak diagrams. These values are to be compared with the gluon contribution that is the dominant one:

$$g_R^g = -6.61 \times 10^{-3}, \quad g_L^g = -1.12 \times 10^{-3}. \quad (3)$$

The final result for the one-loop computation in the SM is the sum of eqs (2) and (3):

$$g_R^{\text{SM}} = -(7.17 + 1.23i) \times 10^{-3}, \quad g_L^{\text{SM}} = -(1.21 + 0.01i) \times 10^{-3}. \quad (4)$$

The real part for the one-loop electroweak quantum correction for  $g_R$  is 8% of the leading gluon-exchange contribution. Note that the imaginary part is 17% of the one-loop  $\text{Re}(g_R^{\text{SM}})$ .

### Acknowledgements

This work was supported by ANII-FCE-2986-Uruguay, COLCIENCIAS-Colombia, the Spanish Ministry of Science and Innovation, under grants FPA2008-03373, FPA2008-02878, and by Generalitat Valenciana under grant PROMETEO 2009/128.

### References

- [1] M Beneke *et al*, hep-ph/0003033
- [2] W Bernreuther, *J. Phys.* **GG35**, 083001 (2008)  
E Boos, L Dudko and T Ohl, *Eur. Phys. J.* **C11**, 473 (1999)  
J A Aguilar-Saavedra, *Nucl. Phys.* **B804**, 160 (2008)

- [3] H S Do *et al*, *Phys. Rev.* **D67**, 091501 (2003)
- [4] C R Chen, F Larios and C P Yuan, *Phys. Lett.* **B631**, 126 (2005)  
Gabriel A Gonzalez-Sprinberg, Roberto Martínez and Jorge Vidal, *J. High Energy Phys.* **1107**, 094 (2011)
- [5] F del Águila and J A Aguilar-Saavedra, *Phys. Rev.* **D67**, 014009 (2003)  
J A Aguilar-Saavedra *et al*, *Eur. Phys. J.* **C804**, 160 (2008)  
J A Aguilar-Saavedra *et al*, *Eur. Phys. J.* **C53**, 689 (2008)  
J Bernabéu and J A Aguilar-Saavedra, *Nucl. Phys.* **B840**, 349 (2010)
- [6] C S Li, R J Oakes and T C Yuan, *Phys. Rev.* **D43**, 3759 (1991)
- [7] M Jezabek and J H Kuhn, *Phys. Rev.* **D48**, 1910 (1993)  
A Czarnecki, *Phys. Lett.* **B252**, 467 (1990)  
C S Li, R J Oakes and T C Yuan, *Phys. Rev.* **D43**, 3759 (1991)
- [8] J Alwall *et al*, *Eur. Phys. J.* **C49**, 791 (2007)
- [9] B Grzadkowski and M Misiak, *Phys. Rev.* **D78**, 077501 (2008)
- [10] J Bernabéu, G A González-Sprinberg and J Vidal, *Phys. Lett.* **B326**, 168 (1994)  
J Bernabéu *et al*, *Nucl. Phys.* **B436**, 474 (1995)