

## Sensitivity of surface resistance measurement of HTS thin films by cavity resonator, dielectric resonator and microstrip line resonator

N D KATARIA<sup>1,\*</sup>, MUKUL MISRA<sup>2</sup> and R PINTO<sup>3</sup>

<sup>1</sup>Superconductivity Division, National Physical Laboratory, New Delhi 110 012, India

<sup>2</sup>Research Center for Superconductor Photonics, Osaka University, Osaka 565 0871, Japan

<sup>3</sup>Tata Institute of Fundamental Research, Homi Bhabha Road, Mumbai 400 005, India

\*Email: kataria@csnpl.ren.nic.in

**Abstract.** Microwave surface resistance ( $R_s$ ) of silver-doped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  (YBCO) thin film, deposited by laser ablation technique on  $10\text{ mm} \times 10\text{ mm}$   $\text{LaAlO}_3$  substrate, has been measured by resonant techniques in the frequency range from 5 GHz to 20 GHz. The geometrical factor of the sample and the resonator has been determined theoretically by the knowledge of the electromagnetic field distribution in the resonators. The microwave surface resistance of the superconducting sample is then extracted from the measured  $Q$  value as a function of temperature. The sensitivity of the  $R_s$  measurement, that is, the relative change in the  $Q$  value with the change in the  $R_s$  value is determined for each resonator.

**Keywords.** Microwave surface resistance; high-temperature superconductors.

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### 1. Introduction

The microwave surface resistance of high-temperature superconductor (HTS) thin films is one of the most important parameters to be characterized because the accurate knowledge of  $R_s$  is essential in the design of high frequency superconducting circuits and to assess the usefulness of HTS films. The surface resistance of HTS films is evaluated from the measured unloaded quality factor  $Q_0$  of the microwave resonator structure used for the measurement. The calculation of  $R_s$  is made via an equation, which involves the geometrical constants of the resonator obtained from the mathematical model describing physical phenomena in resonator. Most of the resonant structures so far used in measurements of  $R_s$  of HTS films have the potential for accurate measurements of  $R_s$ , but not all of them provide the same accuracy.

In this paper, we report the measurement of  $R_s$  of laser ablated  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  (YBCO) thin films deposited on  $10\text{ mm} \times 10\text{ mm}$   $\text{LaAlO}_3$  substrates by three resonating techniques, namely cavity resonator, dielectric resonator, and thin film microstrip line resonator. We also discuss the measurement sensitivity of these resonators with respect to the size of the samples.

## 2. Experiment

Ag-doped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  thin films of thickness  $\sim 400$  nm and  $T_c \sim 89$  K were deposited by pulsed laser deposition technique on  $10 \text{ mm} \times 10 \text{ mm}$  single crystal  $\text{LaAlO}_3$  substrate [1]. The  $R_s$  measurement of the un-patterned YBCO thin film was made by cavity partial end-plate substitution technique at 20 GHz and shielded dielectric resonator (SDR) technique at 18 GHz. The films were then patterned to fabricate a planar half wavelength microstrip line resonator providing fundamental resonance at 5 GHz. For the characterization of films, the resonators were mounted in an evacuated cryo-cooler and cooled down to lowest temperature. Microwave power was fed to the resonator through low loss cables and transmitted resonance signal was analyzed using scalar network analyzer (HP-8757D). The temperature is then slowly raised and 3-dB bandwidth,  $\Delta f$  and insertion loss, IL, are measured at resonant frequency  $f_0$  in the temperature range 20 K to superconducting transition temperature  $T_c$  of the thin films. As all the resonators were weakly coupled, the unloaded  $Q$  value,  $Q_0$ , of the resonator was calculated using relation

$$Q_0 = \frac{f_0}{\Delta f} [1 - 10^{-(\text{IL}/20)}]^{-1}. \quad (1)$$

The unloaded  $Q$  value,  $Q_0$ , of the weakly coupled shielded resonators is expressed in terms of conductor losses by the superconducting sample, conduction losses by the copper walls or ground plane and dielectric losses as

$$\frac{1}{Q_0} = \frac{R_s}{G_s} + \frac{R_{\text{scu}}}{G_m} + \rho_e \tan \delta \quad (2)$$

where  $G_s$  and  $G_m$  are respectively, the geometrical factors of the superconducting sample and the metallic conductor. In general, the geometrical factor can be separately evaluated from the knowledge of the electromagnetic field distribution in a resonator.

The conduction losses due to copper background are measured experimentally from all copper resonators with temperature. The change in the temperature influences the superconductor  $Q$  value,  $Q_{\text{sup}}$ , via  $R_s$ , resulting in the change of the unloaded  $Q$  value,  $Q_0$ , of the resonator. Thus, eq. (2) can be generalized as

$$\frac{1}{Q_0} = \frac{1}{Q_{\text{other}}} + \frac{1}{Q_{\text{sup}}}. \quad (3)$$

The surface resistance,  $R_s$ , of the superconducting sample is evaluated using

$$R_s = \frac{G_s}{Q_{\text{sup}}}. \quad (4)$$

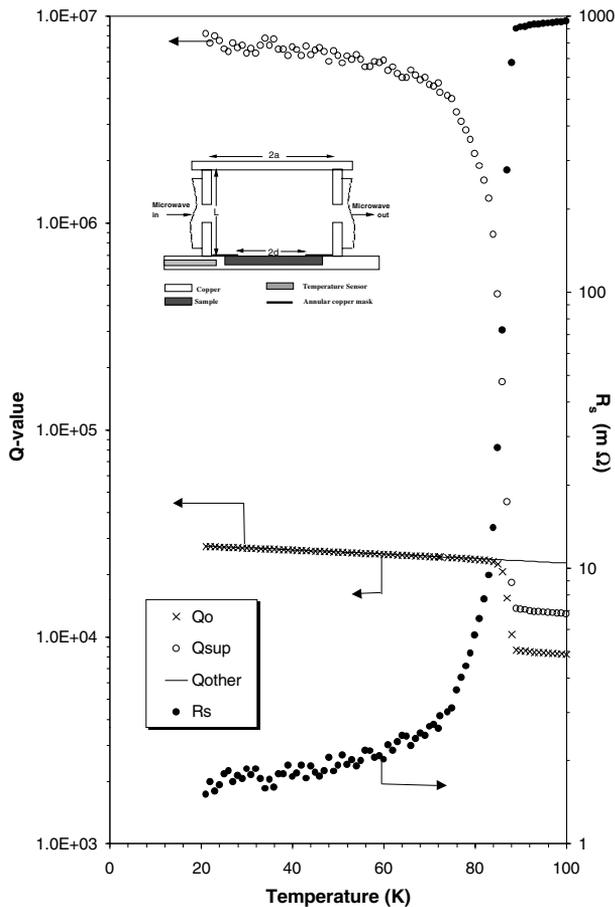
## 3. Cavity resonator technique

The surface resistance of HTS film deposited on  $10 \text{ mm} \times 10 \text{ mm}$  is measured using a  $\text{TE}_{011}$  mode of a cylindrical cavity resonator at 20 GHz by partial end-plate substitution technique (CPEPS) [2]. In this method, the sample is embedded at the center of the end-plate, through annular opening of  $2d = 9.6$  mm, of the copper cavity (diameter  $2a = 22.42$  mm and

length  $L = 12.94$  mm) having surface resistance  $R_{scu}$  of metallic region. The unloaded quality factor  $Q_0$  of the cavity containing sample of surface resistance  $R_s$  is derived using appropriate boundary conditions as [2]

$$\frac{1}{Q_0} = \left[ \left\{ \frac{1}{G_m} - \frac{1}{G_s} \right\} R_{scu} + \frac{1}{G_s} R_s \right] \quad (5)$$

where  $G_m$  and  $G_s$  are the geometrical factors of the metallic cavity and that of the superconducting sample. The geometrical factors were calculated as  $G_m = 716 \Omega$  and  $G_s = 10310 \Omega$  for the sample of 9.6 mm diameter exposed to the microwave signal. The small contribution by the sample area to the total ohmic loss of the cavity can be seen by the ratio  $G_m/G_s = 0.069$  and the fact that the  $Q_{other}$  value of cavity is almost the same as the measured  $Q_0$ , whereas the value of  $Q_{sup}$  is very large as shown in figure 1. This suggests that

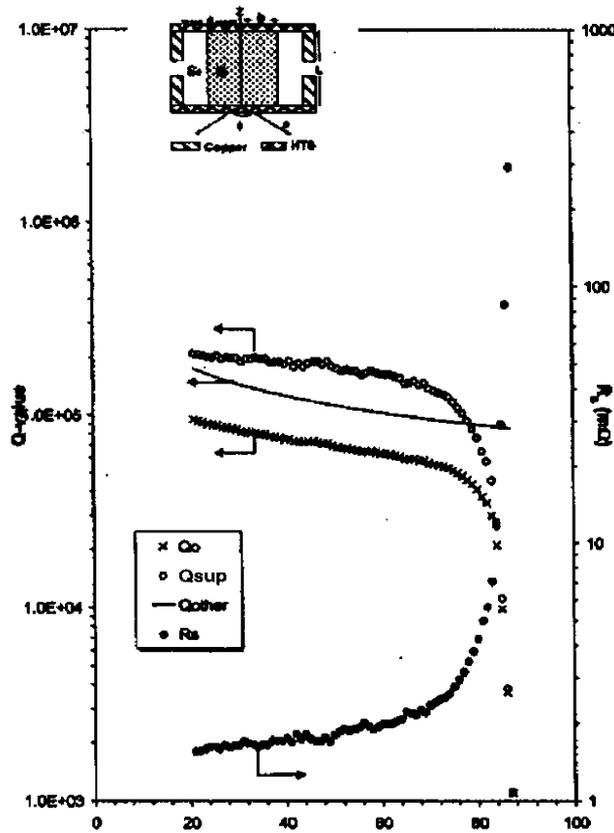


**Figure 1.** Variation of  $Q$  values and  $R_s$  of YBCO thin film with temperature estimated by cavity end-plate substitution at 20 GHz.

the  $Q$  value of the cavity is mainly governed by the ohmic loss in the metallic part of the cavity and that the change in  $R_s$  value of the HTS thin film has negligible influence on  $Q_0$ . The figure also shows the variation in the extracted  $R_s$  value with temperature.

#### 4. Dielectric resonator

The dielectric resonator technique employs the measurement of  $TE_{011}$  mode of a dielectric puck sandwiched between the two test samples and surrounded by a cylindrical metallic shield [3]. A sapphire puck of diameter 7.0 mm and length 4.18 mm was used to fabricate a  $TE_{011}$  mode shielded dielectric resonator (SDR) operating at 18 GHz. The shield diameter of 9.8 mm was kept to ensure grounding of the 10 mm  $\times$  10 mm HTS thin film sample to

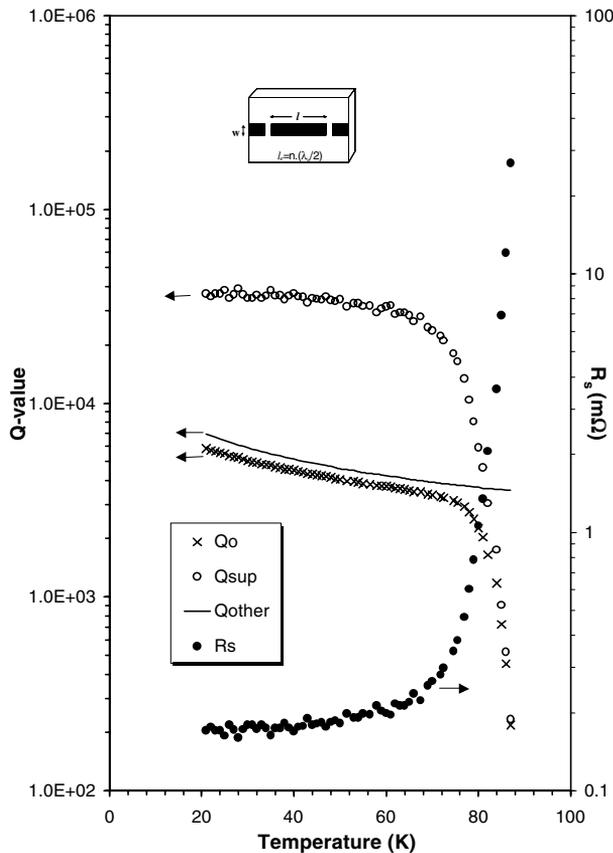


**Figure 2.** Variation of  $Q$  values and estimated  $R_s$  value of the YBCO thin film with temperature measured by dielectric technique at 18 GHz.

the shield. The surface resistance,  $R_s$ , of the YBCO thin film is obtained using eq. (6).

$$\frac{1}{Q_0} = \left[ \left\{ \frac{R_s}{G_s} + \frac{R_{scu}}{G_m} \right\} + p_e \tan \delta \right]. \quad (6)$$

Here  $p_e$  and  $\tan \delta$  are respectively, dielectric filling factor and dielectric loss tangent of the dielectric puck. We have obtained exact expressions for geometrical factors of the superconducting sample  $G_s$  and metallic lateral wall  $G_m$ . The selected dimensions of the SDR provides  $p_e = 0.989$  and the values of geometrical factors  $G_s = 324 \Omega$  and  $G_m = 2105 \Omega$ . Figure 2 shows  $Q$  value of the SDR and average  $R_s$  value as a function of temperature for the two similar HTS YBCO thin films. In this case  $Q_{other}$  and  $Q_{sup}$  are close to each other, suggesting that the  $Q_{sup}$  has rather strong influence on the measured  $Q_0$ .

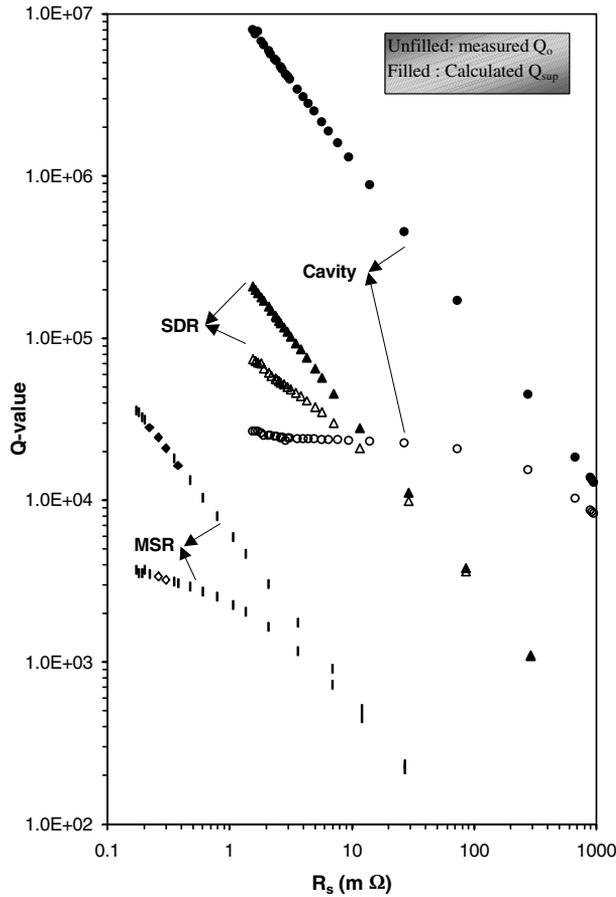


**Figure 3.** Variation of  $Q$  values and estimated  $R_s$  value of the YBCO thin film with temperature measured by microstrip resonator technique at 5 GHz.

### 5. Microstrip resonator technique

The half-wavelength microstrip line resonator is an open-ended transmission line, which supports a standing wave at a frequency for which the effective length  $l_e$  of the line is exactly a half-wavelength. The fundamental resonant mode of the resonator is accompanied by higher order harmonic modes at frequencies approximately integral multiple of the fundamental resonance frequency. We patterned a 5 GHz YBCO half-wavelength microstrip line resonator of length 7.8 mm on LaAlO<sub>3</sub> (LAO) substrate. The surface resistance of the strip material  $R_s$  can be estimated from the measured unloaded  $Q$  value,  $Q_0$ , using relation [4]

$$\frac{1}{Q_0} = \frac{2l_e}{n\pi} \left\{ \left( \frac{G_s R_s + G_m R_{scu}}{2Z_0} \right) + (\rho_e \tan \delta) \right\} \tag{7}$$



**Figure 4.** Variation of  $Q$  value as a function of  $R_s$  value of the YBCO thin film measured by the three resonators.

where  $Z_0$  is the characteristic impedance of the microstrip line,  $G_s$  and  $G_m$  are respectively the geometrical factors of strip and metal ground plane. The geometrical factors for the resonator under consideration are having the values  $G_s = 2187 \Omega^{-1}$  and  $G_m = 298.3 \Omega^{-1}$ . Figure 3 shows the variation of the  $Q$  values and extracted  $R_s$  value of the YBCO thin film with temperature measured by microstrip resonator at 5 GHz. In this case  $Q_{\text{other}}$  of microstrip resonator is much lower than  $Q_{\text{sup}}$  and close to  $Q_0$ . Thus, for this case too, the  $Q_0$  is greatly influenced by  $Q_{\text{other}}$  and reduces the sensitivity of  $R_s$  measurement.

Figure 4 shows measured  $Q$  value,  $Q_0$ , of the three resonators as a function of  $R_s$  value of the HTS YBCO thin film. Figure 4 also shows the plots of  $Q_{\text{sup}}$  vs.  $R_s$  corresponding to the measured  $R_s$  value of the YBCO thin film by these techniques. The  $Q_{\text{sup}}$  value increases monotonically with the decrease in the  $R_s$  value. However, the measured  $Q_0$  tends to saturate at lower  $R_s$  value for CPEPS and microstrip resonator technique. As  $R_s$  value decreases the difference in  $Q_0$  and  $Q_{\text{sup}}$  increases, the difference is minimum for SDR and maximum for CPEPS technique. Also, the slope of the  $Q_0$  for SDR technique is rather steady and higher compared to CPEPS and MSR techniques. It suggests that among those techniques, SDR technique provides the best dynamic range of  $Q$  value for the change in the  $R_s$  value of the sample.

## 6. Conclusion

The sensitivity of SDR for  $R_s$  measurement is maximum. The sensitivity of each technique can be improved: (i) for CPEPS, by increasing the area of sample exposed to microwaves, (ii) in SDR, by taking the shield diameter three times the diameter of sapphire puck, (iii) for MSR, by using double-sided HTS films to form HTS-HTS resonator. However, for CPEPS and SDR the condition of measurement of 10 mm  $\times$  10 mm thin film at low frequencies ( $< 26$  GHz) will be no longer possible in those conditions.

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