

## Analysis of fission excitation functions and the determination of shell effects at the saddle point

V S RAMAMURTHY and S S KAPOOR

Nuclear Physics Division, Bhabha Atomic Research Centre, Bombay 400 085

MS received 22 July 1977

**Abstract.** A method is proposed to deduce the shell correction energy corresponding to the fission transition state shape of nuclei in the mass region around 200, from an analysis of the first chance fission values of the ratio of fission to neutron widths,  $(\Gamma_f/\Gamma_n)_1$ . The method is applied to the typical case of the fissioning nucleus  $^{213}\text{Po}$ , formed by alpha bombardment of  $^{208}\text{Pb}$ . For the calculation of the neutron width, the level densities of the daughter nucleus after neutron emission were obtained from a numerical calculation starting from shell model single particle energy level scheme. It is shown that with the use of standard Fermi gas expression for the level densities of the fission transition state nucleus in the calculation of the fission width, an apparent energy dependence of the fission barrier height is required to fit the experimental data. This energy dependence, which arises from the excitation energy dependence of shell effects on level densities, can be used to deduce the shell correction energy at the fission transition state point. It is found that in the case of  $^{213}\text{Po}$ , the energy of the actual transition state point is higher than the energy of the liquid drop model (LDM) saddle point by  $(3 \pm 1)$  MeV, implying significant positive shell correction energy at the fission transition state. Further, the liquid drop model value of level density parameter  $a$  is found to be a few per cent smaller for the saddle point shape as compared to its spherical shape.

**Keywords.** Fission excitation function,  $^{213}\text{Po}$ ; shell effects at saddle point.

### 1. Introduction

It is now well known that shell corrections to the liquid drop model (LDM) potential energy of a nucleus are, in general, present at all deformations. It is in fact this feature which leads to a double-humped fission barrier for nuclei in the actinide region. In the region of nuclei with mass numbers around 200, although single particle effects do not lead to any significant secondary minimum in the nuclear deformation potential energy due to a much steeper variation of the LDM energy with deformation, a significant shell correction to the LDM energy may be present at the saddle point deformations of these nuclei, as indicated by some calculations (Bolsterli *et al* 1972, Mosel and Schmitt 1971, Pauli *et al* 1971). In this work it is shown that experimental information regarding the shell correction energy at the saddle point deformation of nuclei with mass numbers around 200 can be deduced from an analysis of their measured fission excitation functions.

Fission excitation functions for a number of nuclei with mass numbers around 200 have been measured by Thompson and his collaborators (Burnett *et al* 1964, Khodai Joopari 1966, Thompson 1966) over a wide excitation energy range of the compound nuclei. In earlier studies (Huizenga *et al* 1962, Burnett *et al* 1964, Thompson 1966)

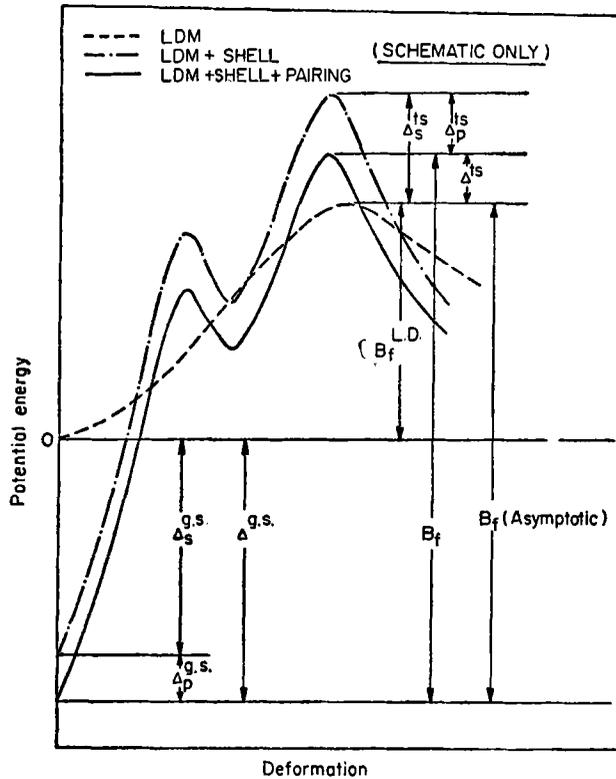
analysis of the fission excitation functions was made with the standard Fermi gas model expressions for the level densities of the fission transition state nucleus and the residual nucleus after neutron emission, on which the magnitudes of the fission width,  $\Gamma_f$  and the neutron width,  $\Gamma_n$  are sensitively dependent. In these studies, theoretical expressions based on Fermi gas model level densities were fitted to the experimental data by treating the level density parameters  $a_f$  and  $a_n$  corresponding to the transition state nucleus and the nucleus after neutron emission as free parameters. Good fits to the data then required a value significantly greater than unity for the ratio  $a_f/a_n$  and it was also found necessary (Thompson 1966) to treat this ratio as energy dependent in order to find a good fit over a wide energy range. These results on  $a_n$  and  $a_f$  were qualitatively understood earlier in terms of shell effects on level densities.

In recent years, numerical calculations of nuclear level densities starting from shell model single particle energy level schemes have become possible (Huizenga and Moretto 1972, Ramamurthy *et al* 1970). Although calculations of single particle levels for both spherical and deformed shapes of nuclei have been carried out, uncertainties associated with these calculations for the highly deformed saddle point shapes can be much larger particularly due to the problems of shape parametrization. The numerical calculations of  $\Gamma_f$ , based on single particle levels of highly deformed saddle shapes may, therefore, have much larger uncertainties than the numerical calculations of  $\Gamma_n$  for spherical shapes. In fact some of the recently reported analysis, while using the numerically calculated level densities for the calculations of  $\Gamma_n$ , retain the standard Fermi gas expression for  $\Gamma_f$  (Moretto *et al* 1972). This simple procedure is justified only if there are no shell effects at the saddle point shape, which may not be true. In this work, we suggest a method of analysis of the experimental  $\Gamma_f/\Gamma_n$  data, which is valid even if there is significant shell correction at the saddle point shape. In fact the present method deduces not only the fission barrier height, but also the contribution of shell correction energy to it. In the following sections, after a brief description of the method, the available data on  $\Gamma_f/\Gamma_n$  for a typical compound nucleus  $^{212}\text{Po}$  formed by alpha bombardment on  $^{208}\text{Pb}$  are analysed with the present method and the results of analysis are discussed.

## 2. Outline of the present method of analysis

The deformation energy curve for a nucleus with mass number around 200 is shown schematically in figure 1 for the general case where shell effects are present at the saddle point. The standard theoretical expressions for the calculation of  $\Gamma_f$  and  $\Gamma_n$  are given in the Appendix. In the present method, the values of  $\Gamma_n$  are computed from a numerical calculation of the level densities of the residual nucleus. From these values of  $\Gamma_n$ , and the experimental  $\Gamma_f/\Gamma_n$  data, we then determine the excitation energy variation of  $\Gamma_f$ . As is described below, an analysis of this deduced  $\Gamma_f$  vs excitation energy can give not only the fission barrier height but also the shell correction energy and the value of LDM  $a$  parameter at the saddle point shape.

It has been shown earlier (Ramamurthy *et al* 1970) that for a calculation of the entropy at the deformed saddle shape with the inclusion of shell and pairing effects, one can use a modified Fermi gas expression  $S^2 = 4a_f E_x^{s'} = 4a_f (E_x^s + \delta)$ , where  $a_f$  is the LDM value of the level density parameter at the saddle point,  $E_x^s$  is the excitation energy at the saddle point and  $\delta$  is an excitation energy dependent correction term. It



**Figure 1.** A schematic representation of potential energy of deformation of a nucleus with residual single particle effects at the fission barrier.  $\Delta_s^{g.s.}$ ,  $\Delta_p^{g.s.}$  and  $\Delta^{g.s.}$  represent the shell, pairing and shell plus pairing energy corrections respectively in the ground state, while  $\Delta_s^{ts}$ ,  $\Delta_p^{ts}$  and  $\Delta^{ts}$  are the corresponding quantities for the transition state nucleus.

is also known from earlier studies (Ramamurthy *et al* 1970, Kapoor and Ramamurthy 1973) that the transition state point is to be identified as the point of minimum entropy along the fission path, and the effective excitation energy  $E_x^{s'}$  is to be measured from a reference energy surface which coincides with the actual potential energy surface at low excitation energies and from the LDM surface at higher excitation energies where shell effects have disappeared. It then follows that  $\delta$  asymptotically approaches the value  $\Delta^{ts}$  at these higher excitation energies, where  $\Delta^{ts}$  is the energy difference between the maximum of the actual potential energy surface and the LDM energy surface (figure 1). Since the quantity  $\Delta^{ts}$  can be identified with the sum of shell and pairing correction energies at the LDM saddle shape if the maximum of the actual potential energy surface coincides with the LDM saddle shape, we shall, refer to the quantity  $\Delta^{ts}$  as the shell and pairing correction energy at the fission transition point shape. One can, therefore, write

$$E_x^{s'} = E_x^s + \delta = (E_x - B_f + \delta) = E_x - B_f'$$

where, at sufficiently higher excitation energies.

$$B_f' = (B_f - \Delta^{ts}) = (B_f^{LDM} + \Delta^{gs}) = \text{constant.}$$

This implies that if an analysis of  $\Gamma_f$  is carried out on the basis of the standard Fermi gas expression for  $\rho^*(X)$  it would necessitate the use of an apparent fission barrier  $B'_f$  which changes with energy in such a way that at higher excitation energies, it asymptotically approaches a constant value equal to  $(B_f - \Delta^{ts})$ . It may be stressed here that  $B'_f$  will reach this constant value only if the chosen value  $a_f$  corresponds to the correct LDM value for the transition state shape of the nucleus. For nuclei with no single particle effects at the saddle point, this constant value of  $B'_f$  will be realised starting from zero excitation energy of the transition state nucleus, and in this case, one can treat  $a_f$  as a free parameter to search for this single constant value of  $B'_f$  by a least square fit to the data. However, as shown earlier, for a nucleus with single particle effects at the saddle point one expects a constant value of  $B'_f$  only at excitation energies, sufficiently large to wipe out shell effects. The expected constancy of  $B'_f$  at higher excitation energies can also be used as a criterion to obtain the correct value of  $a_f$ . Figure 2 shows schematically the expected energy dependence of the apparent fission barrier  $B'_f$  for different values of  $a_f$  for a nucleus having a positive value for the shell plus pairing energy correction to its LDM deformation energy near the saddle point deformation. It can be seen that  $B'_f$  reaches a constant value only for a single value of  $a_f$  which is to be identified as the correct LDM value for the transition state shape of the nucleus. It is, therefore, clear that such an analysis

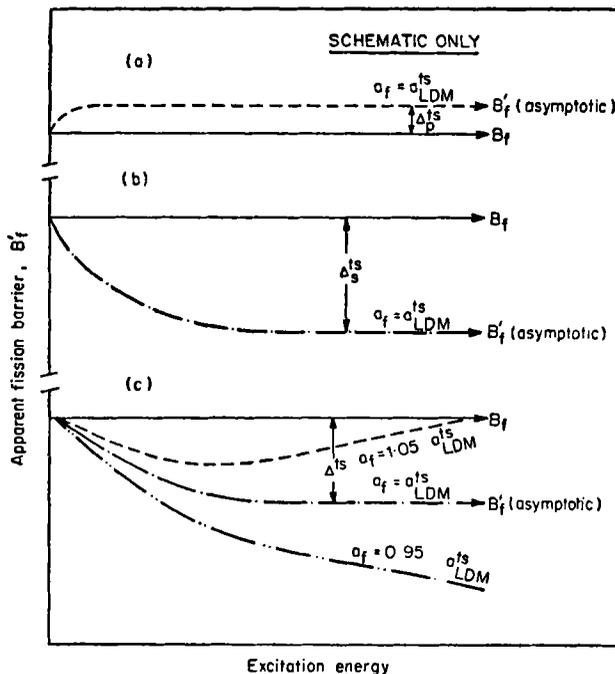


Figure 2. Expected variation of the apparent fission barrier height  $B'_f$  for a nucleus considering (a) pairing energy correction  $\Delta_p^{ts}$  alone (b) a positive shell energy correction  $\Delta_s^{ts}$  alone and (c) pairing plus shell energy correction  $\Delta^{ts}$  respectively. In 2(c), the apparent fission barrier  $B'_f$  versus excitation energy is shown for three values of  $a_f$ , and it can be seen that a constant value of  $B'_f$  is reached asymptotically only if  $a_f = a_{LDM}^{ts}$ .

provides the saddle point shell plus pairing energy correction which is simply equal to the actual fission barrier  $B_f$  minus the asymptotic value of the apparent fission barrier  $B'_f$  at high excitation energies.

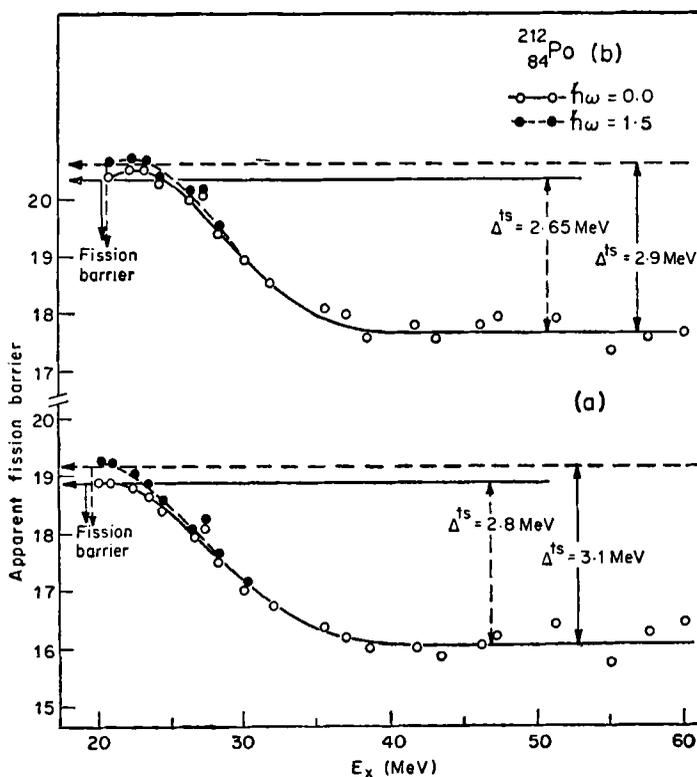
### 3. Results for $^{212}\text{Po}$

The present method was used to analyse the data of Thompson (1966) on  $\Gamma_f/\Gamma_n$  for the nucleus  $^{212}\text{Po}$ . The values of  $\Gamma_f/\Gamma_n$  as deduced by Thompson (1966) from their measurements of alpha induced fission cross-sections of  $^{208}\text{Pb}$  and the reaction cross sections calculated from optical model formed the input data. In order to compare with the calculated first chance fission values of  $(\Gamma_f/\Gamma_n)$ , the above measured values need corrections for multiple chance fissions. The first chance fission values  $(\Gamma_f/\Gamma_T)_1$  for  $^{212}\text{Po}$  were obtained from the measured  $(\Gamma_f/\Gamma_T)$  ( $\Gamma_T = \Gamma_f + \Gamma_n$ ) for  $^{212}\text{Po}$  and  $^{211}\text{Po}$  on the assumption that  $(\Gamma_f/\Gamma_T)_{2+3+\dots}$  for  $^{212}\text{Po}$  at excitation energy  $E_x$  is equal to the measured  $(\Gamma_f/\Gamma_T)$  for  $^{211}\text{Po}$  at excitation energy  $E_x - B_n - 2T$ , where  $B_n$  is the neutron binding energy for  $^{212}\text{Po}$  and  $T$  is the average nuclear temperature for the daughter nucleus after neutron emission. It is seen that the magnitude of this correction is negligibly small below 40 MeV and increases rapidly with increase in the excitation energy. For example, at an excitation energy of 60 MeV, the second chance correction is found to be 70% of the measured value pointing out the importance of correction of the data for multiple chance fission, if the analysis is extended to the data points up to 60 MeV or more. In the present procedure the data might be undercorrection by a few percent due to the angular momentum differences for  $^{212}\text{Po}$  and  $^{211}\text{Po}$  at the same excitation energies, but this residual error is expected to cancel the effect of any small direct interaction effects, if present. In order to keep to a minimum the uncertainties associated with the multiple chance corrections and possible direct interaction effects at higher bombarding energies, the data points for excitation energies only up to 60 MeV were used in the present analysis.

The values of  $\Gamma_n$  vs excitation energies were computed with eq. (A2) with the values of neutron binding energies obtained from the known ground state masses, and taking  $r_0 = 1.2 \times 10^{-13}$  cm. The nuclear level densities  $\rho^{**}(E_x)$  for the residual nucleus were computed by a numerical calculation of both the entropy and the pre-exponential factor starting from a shell model single particle level scheme as described earlier (Ramamurthy 1971). Calculations were carried out for two sets of single particle levels, one given by Seeger and Perisho (1967) for a modified harmonic oscillator potential and the other given by Bolsterli *et al* (1972) for a folded-Yukawa potential. The nuclear pairing effects on level densities were taken into account by replacing the excitation energy  $E_x$  by  $(E_x - \Delta_p^{gs})$ , where  $\Delta_p^{gs}$  is the ground state pairing energy<sup>†</sup> of the residual nucleus. Since the level densities which enter into the calculation of  $\Gamma_n$  are mainly for the residual nucleus excitation energies exceeding about 10 MeV, this procedure for including pairing interactions is justified, (Ramamurthy 1971) since the pairing effects quickly disappear with excitation energy and the level density of a nucleus corresponds to the excitation energy measured from the ground state stripped off its pairing energy  $\Delta_p^{gs}$ . The calculations for  $\Gamma_f$  were carried out with a Fermi gas expression for the level densities and involved two adjustable parameters,  $a_f$  and

<sup>†</sup>Throughout this text, the pairing energy correction refers to the difference in the total potential energy with and without pairing interaction.

$\hbar\omega$ . It was found that the experimental data on  $(\Gamma_f/\Gamma_n)_1$ , cannot be satisfactorily fitted to the calculations with a single value of  $B_f$  over the entire energy range for any value of  $a_f$  implying the existence of shell effects at the saddle point. The values of the apparent fission barrier  $B_f'$  at any excitation energy was then deduced from a fit to the experimental first chance fission  $(\Gamma_f/\Gamma_n)_1$  data. The values of  $B_f'$  vs excitation energy were thus deduced for a range of values of  $a_f$ , and that value of  $a_f$  which led to the expected constancy of  $B_f'$  at higher excitation energies was obtained from these calculations. Figure 3 shows the deduced values of  $B_f'$  for various compound nucleus excitation energies and for values of barrier penetration parameter  $\hbar\omega$  equal to zero and 1.5 MeV and for that value of  $a_f$  which led to a constant value of  $B_f'$  at higher excitation energies. These values of fission barriers have been corrected for a small effective decrease in the fission barrier heights due to the angular momentum brought in by the incident alpha particles using the tabulated (Plasil 1963) Pick-Pichak energies. The results of the analysis are summarized in table 1.



**Figure 3.** The apparent fission barrier height  $B_f'$  as a function of compound nucleus excitation energy  $E_x$  for the fissioning nucleus  $^{212}\text{Po}$  obtained from the analysis of first chance  $(\Gamma_f/\Gamma_n)_1$  data. The calculation of  $\Gamma_n$  with the modified harmonic oscillator levels of Seeger and Perisho (1967), and the folded Yukawa potential levels of Bolsterli *et al* (1972), yields the results shown in figures 3 (a) and (b) respectively. The results of analysis based on the assumptions of barrier penetration factor  $\hbar\omega = 0.0$  and 1.5 MeV are shown for comparison with each other. It can be seen that with the correct value of  $a_f$  chosen, the apparent fission barrier reaches a constant value asymptotically with increasing excitation energies and in all the cases the pairing plus shell energy correction at the transition state is found to have a significant positive value of about 3 MeV.

**Table 1.** Summary of the results of analysis of first chance  $(\Gamma_f/\Gamma_n)_1$  data of  $^{212}\text{Po}$  fissioning nuclei.

Fissioning nucleus	Fission barrier, (MeV) $B_f$		$B_f'$ MeV (asymptotic)	$\Delta^{ts}$ (MeV)		$a_f, \text{MeV}^{-1}$	Spherical $a_{\text{LDM}}, \text{MeV}^{-1}$	$a_f/a_{\text{LDM}}$	Remarks
	$\hbar\omega =$	$\hbar\omega$		$\hbar\omega$	$\hbar\omega$				
	0.0 MeV	1.5 MeV		0.0 MeV	1.5 MeV				
$^{212}\text{Po}$	18.9	19.2	16.1	2.8	3.1	26.1	27.8	0.94	a
	0.4	20.6	17.7	2.6	2.9	19.21	20.9	0.92	b

(a) Modified harmonic oscillator levels (Seeger and Perisho 1967) for calculation of  $\Gamma_n$ (b) Folded-Yukawa potential single particle levels (Bolsterli *et al* 1972) for calculation of  $\Gamma_n$ .

#### 4. Discussion

It can be seen from figure 3 and table 1 that the asymptotic value of  $B_f'$  is less than the actual fission barrier by a few MeV, irrespective of the details of the single particle level scheme used to calculate  $\Gamma_n$  and the input values of the parameter  $\hbar\omega$ . This implies that  $^{212}\text{Po}$  nucleus has a significant positive value for the sum of the shell and pairing correction energy at the saddle point similar to the cases of actinide nuclei. It is further seen from figure 3 that in the present case where shell correction energy has a positive sign, most of the shell effects have disappeared at a moderate excitation energy  $E_x^s$  of about 20 MeV. It is estimated that the deduced values of  $a_f$  have an uncertainty of less than 3% due to the scatter in the experimental data points and uncertainty in the choice of  $r_0$  used to calculate  $\Gamma_n$ . The corresponding uncertainty in the derived values of  $\Delta^{ts}$  is estimated to be within 1 MeV. It is therefore inferred that for the nucleus  $^{212}\text{Po}$ , the sum of the shell and pairing corrections at the transition state shape is  $+(3 \pm 1)$  MeV. In table 1, the deduced values of  $a_f$  are compared with the LDM value of the parameter  $a$  for the *spherical shape* of the nucleus  $^{212}\text{Po}$ . These LDM  $a$  values corresponding to each single particle level scheme were obtained by generating its corresponding uniform level scheme with a value of 1.0 for the Strutinsky parameter  $\gamma$ , and correction terms up to sixth order, and then by determining the single particle level density at the Fermi level for the uniform level schemes. It is seen that the derived values of  $a_f$  are less by 6.8% than the corresponding LDM values for the spherical shapes. A reduction of this order in the LDM value of  $a_f$  for the deformed saddle point shape as compared to spherical shape is in fact expected on the basis of the recently found evidence (Kataria *et al* 1977) for the dependence of  $a_f$  on nuclear surface areas.

The existence of shell and pairing energy corrections at the saddle point of the nucleus  $^{212}\text{Po}$ , as shown by the present analysis, implies that the LDM fission barrier for this nucleus is appreciably lower than the values deduced earlier (Thompson 1966) with the neglect of shell effects at the saddle point. Consequently the Myer-Swiatecki semiempirical mass formula (Myers and Swiatecki 1966) whose coefficients are determined by a fit to the fission barriers deduced earlier with the neglect of shell effects at the saddle point is expected to overestimate the LDM fission barrier heights. Indications to the effect that LDM fission barriers are smaller than those obtained from

the calculations have recently come from other investigations (Shelino *et al* 1972, Methasiri and Johansson 1971, Beckerman and Blann 1977).

In conclusion, the present work has shown that the magnitude of the single particle effects at the fission transition state deformation of nuclei in the region of masses around 200 can be deduced from an analysis of the first chance fission values,  $(\Gamma_f/\Gamma_t)_1$ . The analysis carried out for the case of a typical nucleus  $^{212}\text{Po}$  has shown that appreciable single particle effects exist at its transition state shape. The maximum in the actual potential energy surface is found to be  $(3 \pm 1)$  MeV higher than the LDM saddle point energy. It is also found that the LDM value of the level density parameter  $a$ , is lesser by a few per cent at the deformed saddle shape as compared to spherical shape indicating the dependence of the parameter  $a$  on nuclear surface.

### Acknowledgement

We gratefully acknowledge several useful discussions with Dr S K Kataria, Mr R K Choudhury and Mr M Prakash on several aspects of this work.

### Appendix

#### *Theoretical expressions for the fission and neutron widths*

Analysis of fission excitation functions is based on the Bohr-Wheeler transition state theory for the evaluation of fission width  $\Gamma_f$  and the statistical theory of neutron evaporation for the evaluation of neutron width  $\Gamma_n$ . The theoretical expressions for the fission and neutron widths used in the present investigations are the same as those earlier (Khodai Joopari 1966). The neutron width  $\Gamma_n$  is given by

$$\Gamma_n = \hbar \int_0^{E_x - B_n} W_n(t) dt \quad (\text{A1})$$

where

$$W_n(t) = \frac{\sigma(E_x, t) g m t \rho^{**}(X)}{\pi^2 \hbar^3 \rho(E_x)}$$

Here  $\sigma(E_x, t)$  is the cross section for the inverse process,  $g$  is the statistical weight which applies to the spin states of the neutrons, namely 2, and  $m$  is the neutron mass. The level density of the residual nucleus following neutron emission at excitation  $X$  is  $\rho^{**}(X)$  and  $\rho(E_x)$  is the level density of the compound nucleus at excitation energy  $E_x$ . The neutron kinetic energy  $t$  is related to the total excitation energy  $E_x$ , the neutron binding energy  $B_n$  and the excitation energy of the residual nucleus  $X$ , by

$$t = E_x - B_n - X.$$

By taking the geometric cross section for  $\sigma(E_x, t)$  one gets

$$\Gamma_n = \frac{1}{\pi \rho(E_x)} \int_0^{E_x - B_n} \rho^{**}(X) \frac{t}{t_0} dX \quad (\text{A2})$$

where

$$t_0 = \frac{\hbar^2}{2mr_0 A^{2/3}}$$

For the fission width, the Bohr-Wheeler expression obtained on the basis of the standard theory of reaction rates applied to fission, with the fissioning nucleus at the saddle point configuration, is given by

$$\Gamma_f = \frac{1}{2\pi\rho(E_x)} \int_0^{E_x - B_f} \rho^*(X) dX$$

where  $\rho^*(X)$  is the level density of the saddle point configuration at the excitation energy  $X$  which is the energy in the non-fission degree of freedom. The relation of  $X$  to the total excitation energy  $E_x$  and the potential and kinetic energies in the fission degree of freedom is given by

$$E_x = B_f + T + X$$

where  $B_f$  is the fission barrier and  $T$  is the kinetic energy in the fission degree of freedom. At excitation energies close to the fission barrier, one has to take into account the quantum mechanical penetrability of the barrier. Including this effect, one gets

$$\Gamma_f = \frac{1}{2\pi\rho(E_x)} \int_0^{E_x} \frac{\rho^*(X) dX}{[1 + \exp\{-2\pi(E_x - B_f - X)/\hbar\omega\}]} \quad (\text{A3})$$

where the quantity  $\hbar\omega$  is a measure of the thickness of the barrier, which is assumed to be parabolic.

## References

- Beckerman M and Blann M 1977 *Phys. Rev. Lett.* **38** 272  
 Bolsterli M, Fiset E O, Nix J R and Norton J L 1972 *Phys. Rev.* **C5** 1050  
 Burnett D B *et al* 1964 *Phys. Rev.* **B134** 952  
 Huizenga J R, Choudhry R and Vandebosch R 1962 *Phys. Rev.* **126** 210  
 Huizenga J R and Moretto L G 1972 *Ann. Rev. Nucl. Sci.* **22** 427  
 Kapoor S S and Ramamurthy V S 1973 *Physics and Chemistry of Fission* (IAEA: Vienna) Vol. 1 375  
 Kataria S K, Ramamurthy V S and Kapoor S S 1977 *Phys. Rev. C* (in press)  
 Khodai Joopari A 1966 Univ. of Calif. Lawrence Radiation Lab. Rep. UCRL 16489  
 Methasiri T and Johansson S A E 1971 *Nucl. Phys.* **A167** 97  
 Moretto L G, Thompson S G, Routti J and Gatti R C 1972 *Phys. Lett.* **B38** 471  
 Mosel U and Schmitt H W 1971 *Phys. Rev.* **C4** 2185  
 Myers W D and Swiatecki W J 1966 *Nucl. Phys.* **81** 1; *Ark. Fys.* **36** 343  
 Pauli H C, Ledergerber T and Brack M 1971 *Phys. Lett.* **B34** 264  
 Plasil F 1963 Univ. of Calif. Lawrence Radiation Lab. Rep. UCRL 11193  
 Ramamurthy V S, Kapoor S S and Kataria S K 1970 *Phys. Rev. Lett.* **25** 386  
 Ramamurthy V S 1971 Ph. D. Thesis, Bombay University  
 Seeger R P and Perisho R C 1967 Los Alamos Sci. Lab. Rep. LA 3751  
 Shelino R K, Ragnarsson I and Nilsson S G 1972 *Phys. Lett.* **B41** 115  
 Thompson S G 1966 *Ark. Fys.* **36** 267