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A molecular electron density theory study to understand the interplay of theory and experiment in nitronene-enone cycloaddition

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Abstract. [3 + 2] cycloaddition (32CA) reaction of *C,N*-diaryl nitronene with benzylidene acetone has been studied to analyse the mechanism, selectivity and polar character of this nitronene-enone cycloaddition. Topological analysis of the electron localization function (ELF) shows the absence of *pseudoradical* and carbenoid centre in the nitronene, which allows its classification as a zwitter-ionic (*zw*) *type* three atom component (TAC) and hence participation in *zw-type* cycloadditions is associated with high activation energy barriers. This 32CA reaction follows a *one-step* mechanism with asynchronous TSs. *Endo/meta* product is obtained as the major cycloadduct experimentally, which can be rationalized from its calculated lowest activation energy among the four possible reaction pathways. Global electron density transfer (GEDT) at the TSs predict the non-polar character of this 32CA reaction. Topological analysis of the ELF and QTAIM parameters was performed at the TSs. Finally, non-covalent interaction (NCI) gradient isosurfaces are computed to obtain a visualization of non-covalent interactions at the interatomic bonding regions.

Keywords. ELF; cycloaddition; transition state; QTAIM; MEDT.

1. Introduction

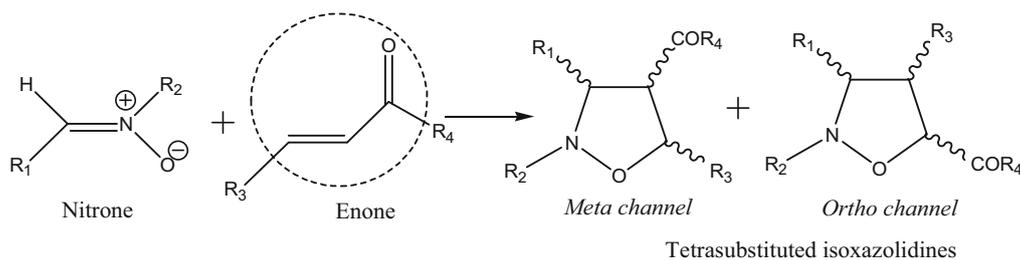
[3 + 2] cycloaddition (32CA) reactions^{1,2} of nitronenes to olefins have remained a versatile protocol for the synthesis of isoxazolidines since the last 40-50 years. Isoxazolidines with three contiguous stereocenters require special mention since they constitute a pivotal structural feature of biologically interesting compounds^{3,4} and are also identified as valuable intermediates in important synthetic routes.^{1,2} Numerous experimental studies devoted to 32CA reactions of nitronenes and enones (Scheme 1) are documented in literature⁵ and this reaction system is still receiving increased attention from synthetic organic chemists.⁶

Frontier Molecular Orbital (FMO) theory proposed by Fukui⁷ in 1952 was considered as the only alternative for interpretation of organic reactions, until

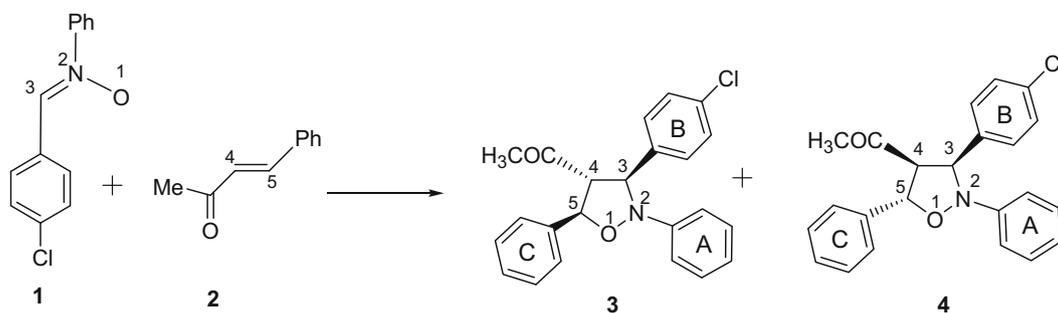
recently in 2016, a new outlook of organic reactivity, named as *Molecular Electron Density Theory* (MEDT) was proposed by Domingo,⁸ stating that the changes in electron density are responsible for molecular reactivity. MEDT^{8,9} has been extensively justified by the use of advanced computing software for the last three years. In 2017, Domingo¹⁰ explained the role of electron density flux between reactants (global electron density transfer¹¹ (GEDT)) in decreasing activation energies of polar cycloadditions and concluded that electron density transfer between reactants facilitates the rupture of C-C double bonds and hence results in lowered activation energy of polar Diels Alder reactions. In a 2018 MEDT study, Domingo¹² explained the underlying reason behind high activation energies of non-polar 32CA reactions of nitronene-alkene systems compared to the corresponding polar 32CA reactions. Non-polar nitronene-alkene 32CA

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Scheme 1. 32CA of the nitron-enone system leading to tetrasubstituted isoxazolidine.



Scheme 2. 32CA reaction of C-(4-chlorophenyl)-N-phenyl nitron (**1**) and Benzylidene acetone (**2**).

reactions involve the formation of new C-C single bond through the coupling of *pseudoradical* centers, while polar 32CA reactions involve the formation of new C-O single bond by donation of the nonbonding electron density by the nitron oxygen. *Pseudoradical* centers are created in non-polar 32CA reactions by the rupture of the olefinic double bond, which requires high energy and hence accounts for the additional energy requirement of non-polar 32CA reactions compared to polar reactions. Now, enone systems (Scheme 1) have conjugated olefin-carbonyl framework which causes depopulation of the olefinic double bond and hence the role of such a framework in the energy requirement of 32CA reactions is worth investigating. With this in mind, the present MEDT study aims to analyse the mechanism and the origin of activation energy in 32CA reactions of enones. MEDT study for nitron-enone system leading to tetrasubstituted isoxazolidine is studied for the first time in this paper. 32CA reaction between C-(4-chlorophenyl)-N-phenyl nitron (**1**) and benzylidene acetone (**2**) is selected as the computational model (Scheme 2) for the present MEDT study.

This report has been divided into four sections. (1) Documentation of experimental findings (2) Electron localization function^{13,14} (ELF) topological study and analysis of conceptual¹⁵ (CDFT) indices at the ground state of the reagents (3) Study of the energy profile and ELF topological study at the TSs (4) Analysis of Quantum Theory of Atoms in Molecules¹⁶⁻¹⁸

(QTAIM) parameters and NCI¹⁹ gradient isosurfaces at the TSs.

2. Computational methods

Density functional theory (DFT) calculations were carried out using B3LYP functional^{20,21} in conjunction with the standard 6-31G(d) basis set, which is identified as a precise computational level to study several 32CA reactions.²²⁻²⁴ Stationary states on the potential energy surface were characterized through frequency calculations at the same level. The intrinsic reaction coordinate (IRC) pathways of the investigated CAs were traced using the second-order Gonzales-Schlegel integration method^{25,26} to check that the energy profiles connect the two associated minima on the potential energy surface. Solvent effects of toluene were taken into account by single-point energy calculations of the gas phase structures using polarised continuum model^{27,28} (PCM) in the framework of SCRf.^{29,30} GEDT¹¹ values were calculated from natural bond orbital (NBO) calculations.^{31,32} CDFT global reactivity indices,^{15,33,34} electronic chemical potential (μ), global hardness (η), global electrophilicity (ω) and relative nucleophilicity N were calculated from the formula cited in reference 15.¹⁵ Computational studies were performed using Gaussian 03 suite of programs (Revision D.01).³⁵ ELF topological studies and calculation of QTAIM parameters

was performed using Multiwfn³⁶ program. Non-covalent interactions¹⁹ (NCIs) were analyzed through evaluation of the B3LYP/6-31G(d) monodeterminantal wave functions of the located transition states by using Multiwfn program.³⁶ ELF basin analysis was performed with a high-quality grid with spacing of 0.06 Bohr. ELF basins and attractors were visualized by using VMD software³⁷ and UCSF Chimera software.³⁸

2.1 Experimental methods

Nitrone **1** was prepared by refluxing phenylhydroxylamine (prepared from nitrobenzene using zinc and ammonium chloride) and 4-chlorobenzaldehyde in ethanol in water bath for 2 h. Nitrone **1** separated as white crystals which were then recrystallized in ethanol. Benzylidene acetone **2** was obtained from the mixed aldol condensation of benzaldehyde and acetone.³⁹ Reactants **1** and **2** were obtained in pure form and confirmed by IR and NMR studies. For the cycloaddition reaction, 0.0044 mol of reactant **1** was allowed to react with 0.0066 mol of reactant **2** in 5 cm³ refluxing dry thiophene-free toluene under a nitrogen atmosphere for 16 h. The cycloaddition was monitored by the examination of reaction aliquots at regular intervals of time by thin-layer chromatography (using benzene-ethyl acetate (4:1) solvent system and silica gel adsorbent) and 300 MHz ¹H spectroscopy. After completion of the run time, excess toluene was removed from the post-reaction mixtures under reduced pressure using a rotary evaporator. Cycloadducts were isolated from the crude reaction mixture by column chromatography over neutral alumina (Activity I-II, Merck) using petroleum ether and benzene mixtures as the eluents. The column was initially eluted with petroleum ether (bpt: 60-80 °C) and then progressively, the proportion of benzene was increased in the eluent. All starting materials and solvents used for reactions and chromatographic separation were distilled before use. IR spectra of the cycloadducts were recorded using a Perkin-Elmer RX-9 FT-IR spectrophotometer. ¹H and ¹³C NMR spectra of the cycloadducts and crude reaction mixtures were recorded by a Bruker AV-300 NMR spectrometer at 300 and 75.5 MHz, respectively. Spectra were recorded in CDCl₃ solvent. Chemical shifts for NMR are reported in ppm, downfield from TMS. Mass spectra are recorded using a JEOL JMS600 H mass spectrometer.

2.1a (3 α ,4 β ,5 α)-3-(4-chlorophenyl)-4-oxomethyl-2,5-Diphenyl-isoxazolidine (**3**, C₂₃H₂₀ClNO₂): White amorphous solid, M.p.: 122 °C, 0.96 gm (58%),

isolated from 10% benzene in petroleum ether (60-80 °C) eluates, R_f = 0.51 (silica gel, petroleum ether (60-80 °C) : benzene = 1:1), IR(cm⁻¹)(KBr): $\bar{\nu}$ = 3077(w), 1670 (s), 1520 (s), 1347(s), 1251 (s), 827 (m), 752 (s), 692(s), ¹H NMR (300MHz, CDCl₃): δ 5.58 (1H,d, *J* = 7.0 Hz, H3), 4.03 (1H,dd, *J* = 7.0, 9.2 Hz, H4), 5.46 (1H,d, *J* = 9.2 Hz, H5), 6.88 (3H, m H2,4,6 (A)), 7.08-7.31 (m, H3,5(A), H2,3,5,6 (B), H2,3,4,5,6 (C)), 2.29 (s, CH₃); ¹³C NMR (75.5MHz, CDCl₃): δ 74.28 (C3), 69.20 (C4), 84.78 (C5), 151.32 (C1(A)), 114.42 (C2,6(A)), 127.92 (C3,5(A)), 122.30 (C4(A)), 136.33, 136.89 (C1(B), C1(C)), 133.15(C4(B), 126.77 (C3,5(C)),128.95 (C4(C)), 128.77, 128.68, 128.43 (C2,6(B), (C3,5(B), C2,6(C)), 196.20 (C=O), 27.42 (-CH₃); MS: *m/z*377 (C₂₃H₂₀NO₂Cl, M⁺), 242 (C₁₅H₁₁OCl), 231 (C₁₃H₁₀NOCl), 216 (C₁₃H₁₁NCl), 131 (C₉H₇O⁺), 111 (C₆H₄Cl⁺), 91 (C₇H₇⁺).

2.1b (3 α ,4 α ,5 β)-3-(4-chlorophenyl)-4-oxomethyl-2,5-Diphenyl-isoxazolidine (**4**, C₂₃H₂₀ClNO₂): White amorphous solid, 0.12 gm (7%), isolated from 20% benzene in petroleum ether (60-80 °C) eluates, R_f = 0.60 (silica gel, petroleum ether (60-80 °C) : benzene = 1:1), IR(cm⁻¹)(KBr): $\bar{\nu}$ = 3045(w), 1677 (s), 1594 (s), 1487 (s), 825 (m), 755 (s), 695(s), ¹H NMR (300MHz, CDCl₃): δ 5.35 (1H,d, *J* = 10.3 Hz, H3), 4.97 (1H,dd, *J* = 10.3, 9.1 Hz, H4), 6.51(1H,d, *J* = 9.1 Hz, H5), 6.93 (3H, m H2,4,6 (A)), 7.10-7.36 (m, H3,5(A), H2,3,5,6 (B), H2,3,4,5,6 (D)), 7.33-7.39 (m, H2,3,4,5,6 (C)), 2.18 (s, CH₃); ¹³C NMR (75.5MHz, CDCl₃): δ 73.48 (C3), 67.30 (C4), 84.75 (C5), 149.07 (C1(A)), 115.58 (C2,6(A)), 127.90 (C3,5(A)),122.30 (C4(A)), 136.13, 136.92 (C1(B), C1(C)), 133.30(C4(B),126.85(C3,5(C)), 128.85(C4(C)), 128.78, 128.68, 128.33 (C2,6(B), (C3,5(B), C2,6(C)), 197.59 (C=O), 27.58 (-CH₃); MS: *m/z*377 (C₂₃H₂₀NO₂Cl, M⁺), 242 (C₁₅H₁₁OCl), 231 (C₁₃H₁₀NOCl), 216 (C₁₃H₁₁NCl), 131 (C₉H₇O⁺), 111 (C₆H₄Cl⁺), 91 (C₇H₇⁺).

3. Results and Discussion

3.1 Experimental findings for 32CA reaction between **1** and **2**

32CA reaction between **1** and **2** afforded a diastereomeric mixture of *meta* cycloadducts **3** and **4** (Scheme 1) in the ratio 87:13 with the total yield of 75%. Structure elucidation was accomplished by spectroscopy (particularly NMR) and mass spectrometry. 300 MHz ¹H NMR spectrum of the major product

3 showed doublets at δ 5.58 ppm ($J = 7.0$ Hz) and δ 5.46 ppm ($J = 9.2$ Hz). A double doublet appeared at δ 4.03 ppm ($J = 7.0, 9.2$ Hz). The double doublet could be assigned to H4 of the isoxazolidine ring. For the minor cycloadduct **4**, two doublets appeared at δ 5.35 ppm ($J = 10.3$ Hz) and δ 6.51 ppm ($J = 9.1$ Hz) and the double doublet appeared at δ 4.97 ppm ($J = 10.3, 9.1$ Hz). Coupling constants of the two doublets rendered their respective assignments to H3 and H5 in **3** & **4** in accordance with our previously reported studies for 32CA reactions of nitrones to benzylidene acetophenone⁴⁰ and cinnamoyl piperidine.⁴¹ The coupling constants supported 3,4-*trans*-4,5-*trans* stereochemistry in cycloadduct **3** [$J_{3,4} = 7.2$ Hz and $J_{4,5} = 9.0$ Hz in 3,4-*trans*-4,5-*trans* cycloadduct obtained from 32CA reaction of nitrone **1** to benzylidene acetophenone]⁴⁰ and 3,4-*cis*-4,5-*trans* stereochemistry in cycloadduct **4** [$J_{3,4} = 10.1$ Hz and $J_{4,5} = 9.5$ Hz in 3,4-*cis*-4,5-*trans* cycloadduct obtained from 32CA reaction of nitrone **1** to benzylidene acetophenone].⁴⁰ ¹³C NMR signals of ring C and mass spectral fragmentation peaks (see experimental section) supported the connectivity of C5 to the oxygen atom of the isoxazolidine ring.

3.2 Analysis of the CDFT reactivity Indices and ELF topological analysis of the reactants

Several theoretical studies devoted to 32CA reactions¹⁵ have reported the analysis of DFT based global indices to characterize the feasibility of the reactions. Consequently, the electronic chemical potentials (μ), chemical hardness (η), electrophilicity (ω) and nucleophilicity (N) indices of nitrone **1** and benzylidene acetone **2** were computed and analyzed (Table 1). The electronic chemical potential μ of benzylidene acetone **2**, $\mu = -4.10$ eV is only slightly lower than that of the nitrone **1**, $\mu = -3.80$ eV, which indicates that transfer of electron density is unlikely to occur in either direction. These values predict a non-polar reaction between **1** and **2**. This is in complete agreement with the calculated global electron density transfer (GEDT¹¹) computed at the transition states (TSs) (see section 3.3). As the reaction is predicted to be non-polar, the regioselectivity could not be predicted by

Table 1. B3LYP/6-31G(d) calculated electronic chemical potentials (μ), chemical hardness (η), electrophilicity (ω) and nucleophilicity (N) indices of the reactants in eV.

	μ	η	ω	N
1	-3.80	3.67	1.96	3.48
2	-4.10	4.49	1.87	2.78

analysis of two-centre or four center interactions by local reactivity indices, such as Fukui⁴² or Parr functions.⁴³ Reagents **1** and **2** show almost similar electrophilicity ω of 1.96 eV(**1**) and 1.87 eV(**2**), which renders their classification as strong electrophiles according to the absolute scale of electrophilicity.³⁴ Nitrone **1** is classified as a strong nucleophile ($N > 3$ eV), while benzylidene acetone **2** as a moderate nucleophile ($N < 3$ eV).¹⁵

The concept of Electron Localization Function (ELF) for atomic and molecular systems was introduced by Becke and Edgecombe,¹³ followed by the outlining contribution of Silvi and Savin¹⁴ in the use of ELF attractors for classification of chemical bonds. Domingo^{8,9} correlated the electronic structures of the simplest three atom components (TACs) and their reactivities in 32CA reactions. Monosynaptic basin V(A) integrating 1e are associated with *pseudoradical center* at A, while V(A) integrating 2e in a neutral molecule is associated with *carbenoid center* at A. TACs are classified as (1) Two *pseudoradical* centers: *Pseudodiradical* TAC (*-pdr* type), (2) One *pseudoradical* center: *Pseudo(mono)radical* TAC (*-pmr* type) (3) One *carbenoid centre*: *Carbenoid* TAC (*cb-* type) (4) No *pseudoradical* or *carbenoid centre*: *Zwitterionic* TAC (*zw-* type)

ELF localization domains and basin attractor positions with the most significant valence basin population of reactants **1** and **2** are given in Figure 1. ELF topological analysis can provide the interpretation of Lewis's bonding model of a molecular system.⁸ The proposed Lewis like structures of **1** and **2** is given in Scheme 3.

ELF topological analysis of nitrone **1** shows the presence of V(C3,N2) and V(N2,O1) disynaptic basins integrating at the populations of 3.93e and 1.30e, respectively which can be associated with underpopulated C3-N2 double bond and underpopulated N2-O1 single bond. V(O1) and V'(O1) monosynaptic basins integrating a total population of 5.95e can be associated with the lone pair electron density at oxygen atom O1 of **1**. Nitrone **1** has neither a *pseudoradical* center nor a *carbenoid centre*, allowing its classification as *zwitterionic* TAC (*zw-* type). TAC reactivity decreases in the order:^{9,12} *pdr*-type > *pmr*-type \approx *cb*-type > *zw*-type. *zw* type 32CA reactions are associated with high activation energies, which is also observed in the present study (see section 3.3). ELF topological analysis of **2** shows V(C4,C5) and V'(C4,C5) disynaptic basins integrating at a total population of 3.38e which can be associated with the underpopulated C4-C5 double bond. For styrene, V(C4,C5) and V'(C4,C5) disynaptic basins integrate at a total population of 3.50e.

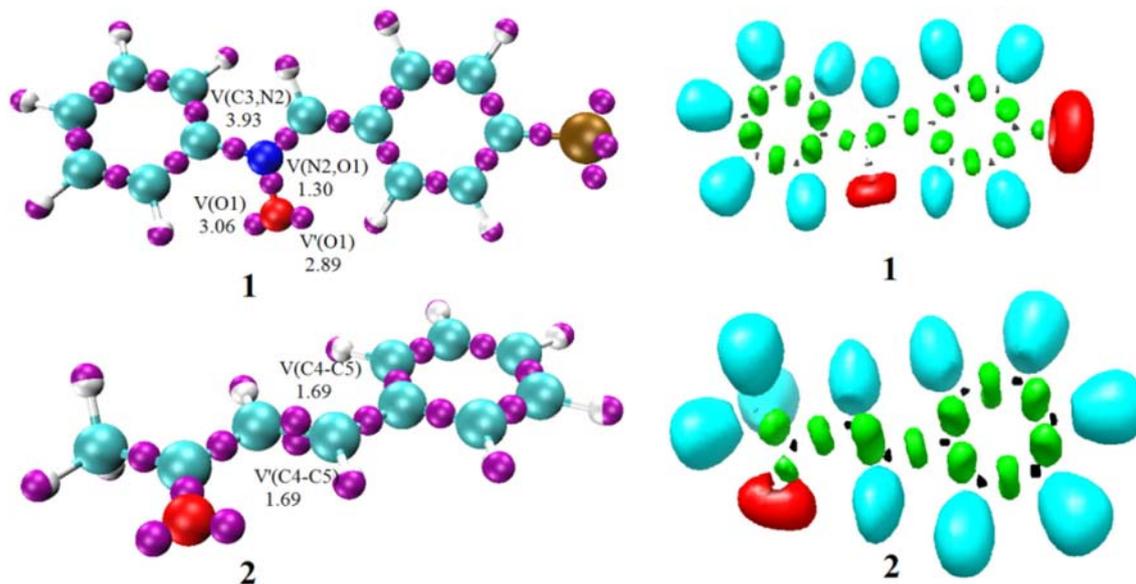
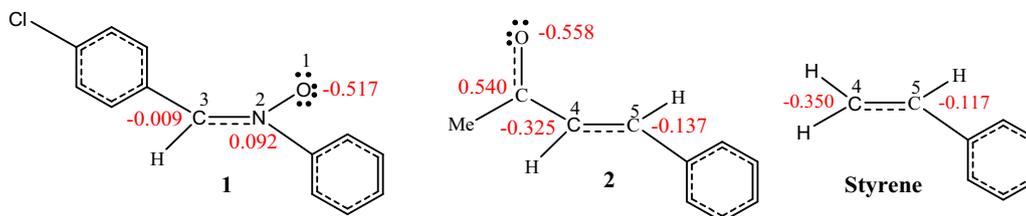


Figure 1. ELF localization domains [Isovalue: 0.79] and Basin attractor positions together with the most significant ELF valence basin populations for the reactant molecules. Attractors are shown by purple spheres, ELF valence basin population are given in average number of electrons, e. Protonated basins are shown in blue, disynaptic basins are shown in green, monosynaptic basins are shown in red and core basins are shown in black colours.



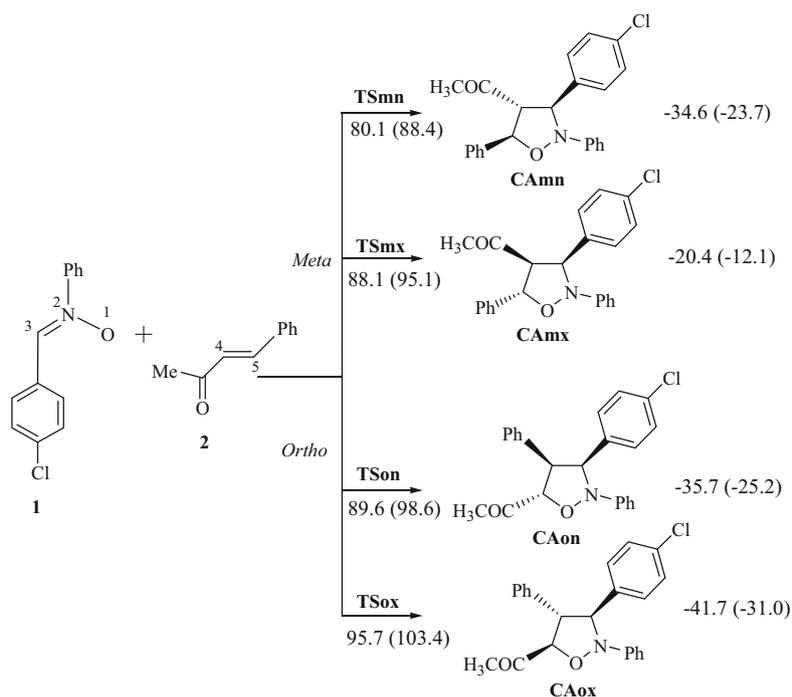
Scheme 3. Proposed Lewis-like structure of the reactants (based on ELF basin population) and calculated natural atomic charges (shown in red) are given in an average number of electrons, e.

Charge distribution of the reactants was analyzed through natural population analysis^{31,32} (NPA). O1 of nitron **1** is negatively charged by 0.517e, while nitrogen N2 and carbon C3 show negligible charges of 0.092e and 0.009e (Scheme 3). This framework of natural charges supports charge separation in TAC **1**, however, the charge separation is not in line with the Lewis bonding model. This indicates that the charge separation is not the outcome of resonance Lewis structure, but asymmetric electron density delocalization in the molecule due to the presence of different nuclei. C4 of Benzylidene acetone **2** and styrene shows the higher magnitude of negative charge than C5, owing to the presence of C5 phenyl substituent.

3.3 Study of the energy profile associated with the 32CA reactions

There are two possible regioisomeric channels, *ortho* and *meta* for 32CA reaction of nitron **1** and

benzylidene acetone **2**. *Ortho* approach is associated with the formation of O1-C4 and C3-C5 bonds, while the *meta channel* is associated with the formation of O1-C5 and C3-C4 bonds (Scheme 4). The *endo* and *exo* stereochemical approaches along these two regioisomeric channels can lead to four possible cycloadducts. The search for stationary points along these four reaction paths allowed locating and characterizing the reagents **1** and **2**, four TSs **TSmn**, **TSmx**, **TSON** and **TSox** along with the *endolmeta*, *exolmeta*, *endolortho* and *exolortho* approach modes and the corresponding cycloadducts **CAMn**, **CAMx**, **CAon** and **CAox** (Scheme 4). This 32CA reaction follows a *one-step* mechanism. The activation energies range from 80.1 (**TSmn**) to 95.7 (**TSox**) kJ mol⁻¹ in the gas phase and from 88.4 (**TSmn**) to 103.4 (**TSox**) kJ mol⁻¹ in toluene, with the reaction being exothermic in the range -20.4 to -41.7 kJ mol⁻¹ in the gas phase and -12.1 to -31.0 kJ mol⁻¹ in toluene. The most favorable reaction path of this kinetically controlled reaction is associated with the *meta/endo* approach



Scheme 4. Possible regio- and stereoisomeric pathways for 32CA reaction between **1** and **2**. Activation energies are given in kJ/mol. Activation energies in parenthesis are calculated in toluene solvent.

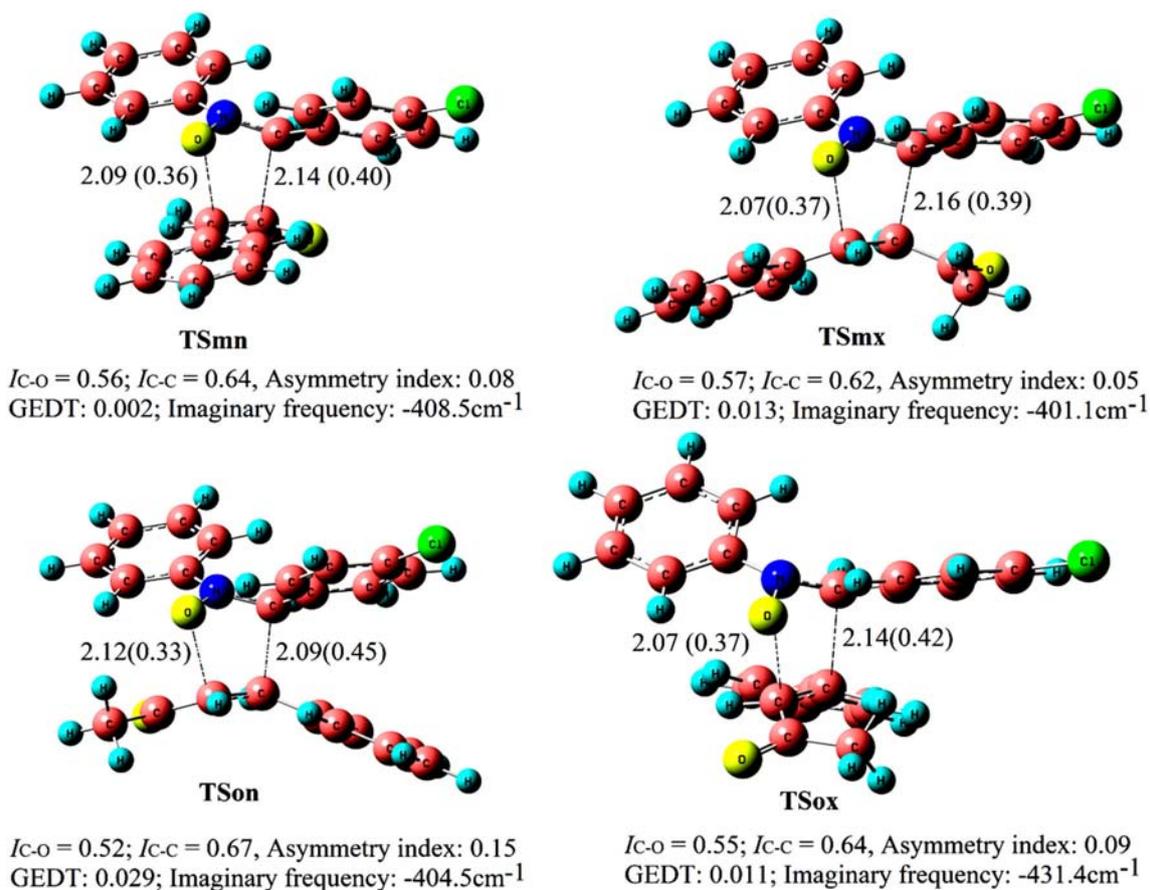


Figure 2. B3LYP/6-31G(d) optimized transition states for 32CA reaction of **1** and **2**. $I_{\text{C-C}} = 1 - ((r_{\text{C-C}}^{\text{TS}} - r_{\text{C-C}}^{\text{P}})/r_{\text{C-C}}^{\text{P}})$; $I_{\text{C-O}} = 1 - ((r_{\text{C-O}}^{\text{TS}} - r_{\text{C-O}}^{\text{P}})/r_{\text{C-O}}^{\text{P}})$; r^{TS} and r^{P} are the bond distances of TSs and cycloadducts; Asymmetry index,⁴⁶ $\Delta a = I_{\text{C-C}} - I_{\text{C-O}}$.

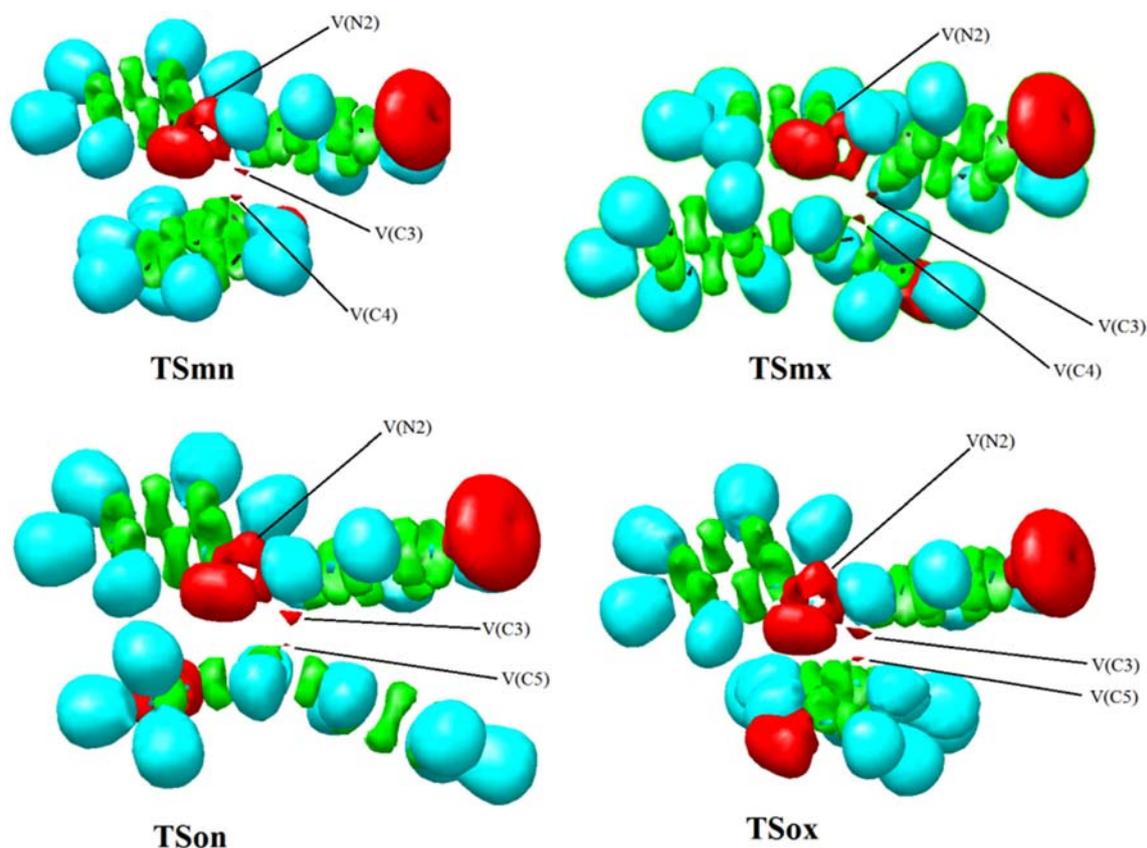


Figure 3. ELF localization domains [Isovalue: 0.79] the TSs. Protonated basins are shown in blue, disynaptic basins are shown in green, monosynaptic basins are shown in red and core basins are shown in black colours.

Table 2. ELF topological analysis at the TSs.

	V(O1)	V'(O1)	V(C3,N2)	V(N2,O1)	V(C4,C5)	V(N2)	V(C3)	V(C4)	V(C5)
TSmn	2.93	2.94	2.36	1.11	2.72	1.33	0.47	0.43	–
TSmx	2.93	2.95	2.31	1.10	2.69	1.32	0.45	0.45	–
TSon	2.91	2.92	2.18	1.14	2.66	1.24	0.60	–	0.39
TSox	2.89	2.94	2.27	1.13	2.71	1.34	0.56	–	0.40

Table 3. QTAIM parameters in [au] of (3,-1) critical points at the transition states in the regions associated with the generation of new C-C (CP1) and C-O (CP2) single bonds.

TS	CP1 (C3-C4)			CP2 (C5-O1)		
	ρ	$\nabla^2_{\rho(r_c)}$	$E_{\rho(r_c)}$	ρ	$\nabla^2_{\rho(r_c)}$	$E_{\rho(r_c)}$
TS1	0.068	0.029	-0.018	0.062	0.117	-0.007
TS2	0.066	0.032	-0.017	0.064	0.117	-0.008
TS3	0.076	0.014	-0.023	0.059	0.117	-0.006
TS4	0.069	0.025	-0.019	0.065	0.121	-0.008

mode, yielding the experimental isoxazolidine **3** via **TSmn**. The high activation energy of 80.1 kJ mol^{-1} is in agreement with the *zw-type* character. This reaction

is completely regioselective with relative energy of **TSmn** less than the *ortho* TSs by 9.5 and 15.6 kJ/mol in the gas phase and 10.2 and 15.0 kJ/mol in toluene. In our previous studies,^{44,45} we have observed that 32CA reaction of *C,N*-disubstituted nitrones to ethyl vinyl ketone and methyl crotonate also follow *one-step* mechanism and show energy barriers of 40.6 kJ/mol and 57.8 kJ/mol, respectively along with the favoured *ortho/exo* and *meta/endo* pathways, which are lower than that calculated for the present study.

Optimized geometries of the TSs are given in Figure 2. The calculated bond orders of the forming C-C bonds are higher than that of C-O bonds in each case. Finally, the polar character was evaluated by GEDT calculations at the TSs. GEDT values at the

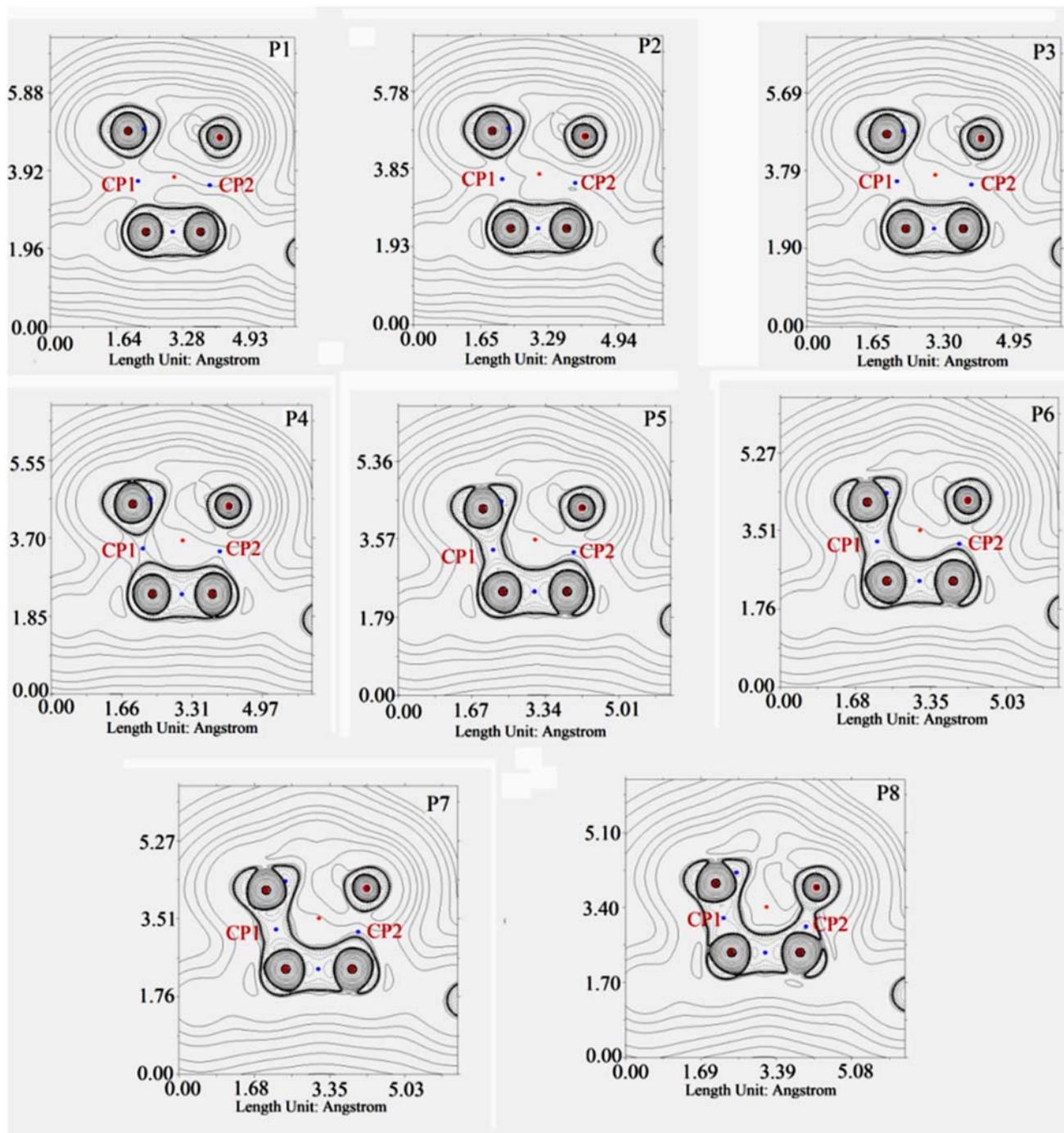


Figure 4. Representations of the contour line maps of the Laplacian of the electron density along *endolmeta* pathway of 32CA reaction between **1** and **2** at selected IRC coordinate points along the reaction pathway on the molecular plane defined by atoms for C3-C4 (C-C) and C5-O1 (C-O) bond formation, CP1 (3,-1) and CP2 (3,-1) critical points respectively are marked in the representation.

TSs vary from 0.002e to 0.029e. This is indicative of the non-polar character, which is supported by the minimal difference between electronic chemical potentials of **1** and **2** (Table 1). Generally speaking, non-polar 32CA reactions are associated with high activation energies, which is also observed in the present study with the enone system.

3.4 ELF topological analysis at the transition states

ELF localization domains at the TSs are given in Figure 3, with the most significant valence basin populations listed in Table 2. Topological analysis of the ELF of TSs **TS_{mn}**, **TS_{mx}**, **TS_{on}** and **TS_{ox}** show

the presence of V(O1) and V'(O1) monosynaptic basins with total integrating population of 5.83-5.88 e (Table 2), which can be associated with the non-bonding electron density at the oxygen atom. Disynaptic V(C3,N2) basin integrating at 2.18-2.36 e can be associated with the C3-N2 bond that has experienced depopulation and hence ruptures along the reaction course while proceeding from the reactants to the TSs. V(N2) monosynaptic basin can be associated with the lone pair electron density at N2 nitrogen.

C4-C5 bond rupture is also evident from the disynaptic V(C4,C5) basin integrating at 2.66-2.72e. TSs also show the presence of monosynaptic V(C3) basin less than 1e which can be associated with the formation of *pseudoradical* centre at C3 carbon. *Meta* TSs, **TS_{mn}** & **TS_{mx}** show the presence of monosynaptic basins at C4, while *ortho* TSs, **TS_{on}** & **TS_{ox}** show the presence of monosynaptic basins at C5, which can be associated respectively with the formation of *pseudoradical* centers at C4 and C5.

3.5 Identification of the atomic interactions at the interatomic bonding regions

Bader's Quantum Theory of Atoms in Molecules¹⁶⁻¹⁸ (QTAIM) has been widely used to unravel the covalent and non-covalent interactions in molecular systems. The Laplacian of electron density ∇^2 plays a significant role to characterize the covalent/non-covalent interactions present in molecular systems. We have recently applied⁴⁴ this QTAIM concept to characterize the nature of bonding in 32CA reactions of nitrene to ethyl vinyl ether. The calculated QTAIM parameters at the (3,-1) bond critical point (BCP) at the TSs are given in Table 3 with contour line map of the Laplacian of electron density at the selected IRC points along the *endolmeta* pathway represented in Figure 4. Positive Laplacian at the BCPs (Table 3) indicate that the formed bond at the TSs is non-covalent in nature and a small amount of electron density ρ is involved in the bonding.

NCI plot program was introduced in 2011 by Yang and co-workers¹⁹ to plot and visualize the bonded and non-bonded non-covalent gradient isosurfaces, defined by the sign of λ_2 ,¹⁶⁻¹⁸ a component of the Laplacian of electron density.¹⁶⁻¹⁸ NCI plots of **TS_{mn}** is given in Figure 5. For **TS_{mn}**, the non-covalent attractive bonded overlap (blue portions) and non-bonded overlap (red portions) are present between O1 & C5, and also between C3 & C4. This indicates the presence of non-covalent interaction at the C3-C5 & C5-O1

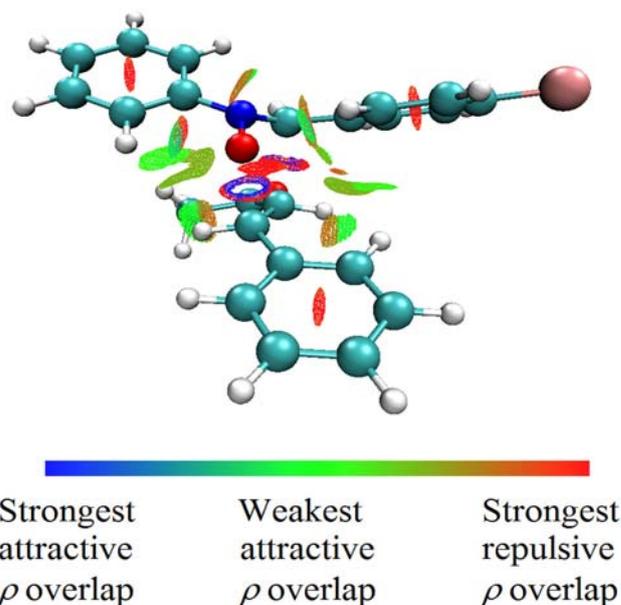


Figure 5. B3LYP/6-31G(d) calculated Non-covalent interactions (NCI) gradient isosurfaces of reduced density gradient [as values of sign(λ_2) ρ] at **TS_{mn}**. Surfaces are coloured in the [-0.04 (blue), 0.02 (red)] a.u. (Isosurfaces = 0.5 a.u.).

interatomic bonding region, which agrees with the calculated positive Laplacian of electron density (Table 3).

4. Conclusions

[3 + 2] cycloaddition reaction of *C*-(4-chlorophenyl)-*N*-phenyl nitrene to benzylidene acetone is non-polar zwitter-ionic (*zw*) type and proceeds through *one-step* mechanism with asynchronous TSs. The reaction is regioselective with *endolmeta* pathway predicted as the favored mode of approach with a high activation energy barrier of 80.1 kJ/mole, in line with its *zw-type* character. The origin of high activation energy barrier is the energy required for the rupture of C-C double bond to form *pseudoradical* centers and new C-C and C-O single bonds of the isoxazolidine adduct are generated through the coupling of these *pseudoradical* centers. This 32CA reaction involves non-covalent interactions between the reacting nuclei at the TSs, as evident from the positive Laplacian of electron density and visualization of gradient isosurfaces in the non-covalent interaction (NCI) plot.

Supplementary Information (SI)

- (1) 300 MHz ¹H NMR spectra of the crude reaction mixture
- (2) 300 MHz ¹H NMR spectrum of cycloadducts **3** and **4** (3)
- 75.5 MHz ¹³C NMR spectrum of cycloadducts **3** and **4** (4)

Mass spectrum of cycloadduct **3** (5) Cartesian Coordinates and optimized energies of all reactants, products and transition states (6) ELF basin populations along *endo/meta* pathway are available at www.ias.ac.in/chemsci.

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