

Microscopic order parameter of two nematogenic compounds using X-rays

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MS received 28 October 1998; revised 12 January 1999

Abstract. X-ray Laue type diffraction patterns were recorded using the image plate system at different temperatures in the nematic phase for two nematogenic compounds. Micro-orientational order parameters have been computed using different methods. These are compared with the microscopic orientational order parameters obtained from refractive index data. Higher order parameters have also been computed and compared. Distribution function at various temperatures for the two nematogenic compounds from Deutsch method has been reported.

Keywords. Nematic; orientational order; liquid crystal.

1. Introduction

The orientational order parameter of any nematic liquid crystal determines its applicability in electro-optic displays and hence the continued interest amongst various investigators to compute the order parameter. This can be evaluated by various methods viz. optical, NMR, X-rays etc. The earlier works of the determination of the OP using X-rays are due to Falgueirettes (1959), Delord and Falgueirettes (1965), de Vries (1972), Leadbetter and Norris (1979), and Baumann *et al* (1989). The simplest approach is that of Leadbetter (1979) which leads to the classical formula:

$$I(\phi) = \int_0^{\pi/2} f(\beta) \sec^2(\phi) (\tan^2 \beta - \tan^2 \phi)^{-1/2} \sin \beta \, d\beta, \quad (1)$$

which relates the scattered intensities at an angle ϕ to the orientational distribution function $f(\beta)$ of the molecular axes. To evaluate the orientational distribution function $f(\beta)$ and the order parameter, various numerical and series expansion methods (see for e.g. Leadbetter and Wrighton 1979; Haase *et al* 1988; Fan *et al* 1990; Kelkar and Paranjape 1987; Bhattacharjee *et al* 1981) had been employed. Deutsch (1991) has shown that (1) can be analytically inverted which leads to general expressions for the order and higher order parameters. Davidson *et al* (1995) (here afterwards called Levelut method) have developed simple analytical calculation of (1) which leads to a series expression. Also, they have shown that single intensity measurement can lead to the

evaluation of $f(\beta)$. We have computed the order parameter by these methods for two nematogenic compounds viz. octylbenzoic acid (OBA) and nonylbenzoic acid (NBA) using good quality X-ray intensity data. These results are compared with the order parameter obtained from refractive index data which have been already reported (Divya *et al* 1997).

2. Experimental

2.1 Samples

OBA and NBA were obtained from M/s Merck Ltd, UK which were purified by recrystallization in benzene. These compounds exhibit nematic phase and the nematic-isotropic transition temperatures are 112 and 115°C for OBA and NBA, respectively. The transition temperatures were determined by using a polarizing microscope in conjunction with a specially constructed hot stage. The observed values are in good agreement with the reported values.

2.2 Collection of X-ray intensity data

The samples were taken in capillary tubes and oriented by an external magnetic field (6 kilogauss). The X-ray intensity data from the sample was collected using Laue method at different temperatures in the nematic phase, the temperature being controlled to an accuracy of $\pm 0.01^\circ\text{C}$. Using the supplied X-ray software, the X-ray intensity data were sorted as a function of the arc angle. The wavelength of the X-rays used was 1.5418 Å (Cu K α). No monochromator was used in this experiment. An image plate with a plate diameter of 18 cm was used

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as the detector to collect the intensity data. The intensity versus arc angle data were obtained by integrating the diffused reflections over an annular ring centred on these reflections. These recordings for OBA and NBA are given in figure 1 for a temperature in the nematic phase.

3. Analysis of X-ray data

Deutsch (1991) has derived an exact analytical solution to (1) and has obtained the expressions for the two lowest order parameters $\langle P_2 \rangle$ and $\langle P_4 \rangle$ as

$$\langle P_2 \rangle = 1 - (3/2N) \int_0^{\pi/2} I(\phi) [\sin^2 \phi + \sin \phi \cos \phi \ln \{(1 + \sin \phi)/\cos \phi\}] d\phi, \quad (2)$$

and

$$\langle P_4 \rangle = 1 - (1/N) \int_0^{\pi/2} I(\phi) [\sin^2 \phi [(105/16) \cos^2 \phi + 15/24] + \sin \phi \ln \{(1 + \sin \phi)/\cos \phi\} ((105/16) \cos^4 \phi - (15/4) \cos^2 \phi)] d\phi, \quad (3)$$

where $N = \int_0^{\pi/2} I(\phi) d\phi$.

The Leadbetter expression for $I(\phi)$ in terms of a series can be written as

$$I(\phi) = f_0 + 2/3 f_2 \cos^2 \phi + 8/15 f_4 \cos^4 \phi + 14/35 f_6 \cos^6 \phi + 128/315 f_8 \cos^8 \phi + 256/693 f_{10} \cos^{10} \phi + \dots \quad (4)$$

Within the framework of Maier–Saupe model, Levelut group have come up with a novel method wherein there is only one independent parameter and the expression for $I(\phi)$ is given by

$$I(\phi) = 1/Z [1 + 2/3 m \cos^2 \phi + 4/15 m^2 \cos^4 \phi + 8/105 m^3 \cos^6 \phi + 16/945 m^4 \cos^8 \phi + \dots], \quad (5)$$

where $Z = 4\pi \int_0^1 \exp(mx^2) dx$ is the normalization constant. The constants f 's in Leadbetter approach and the constant 'm' in Levelut approach are related to the order parameter via the orientational distribution function via the relations

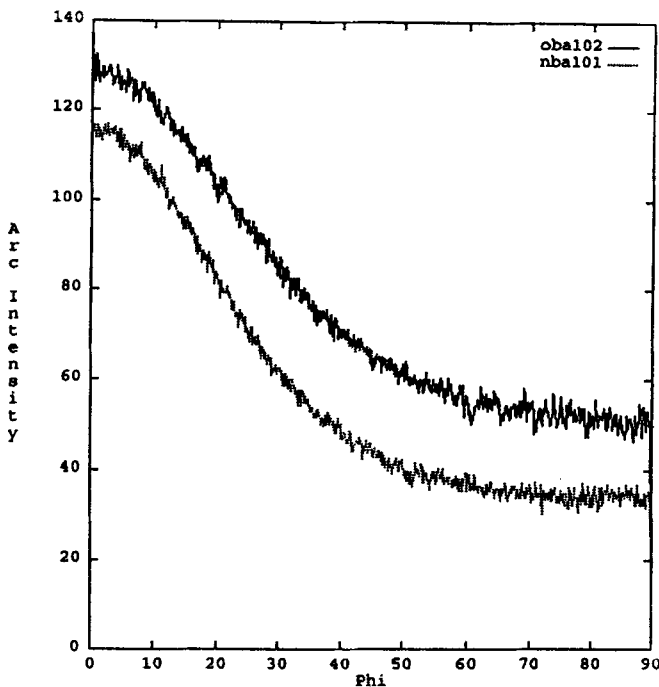


Figure 1. X-ray recordings for OBA and NBA at 101 and 102°C, respectively.

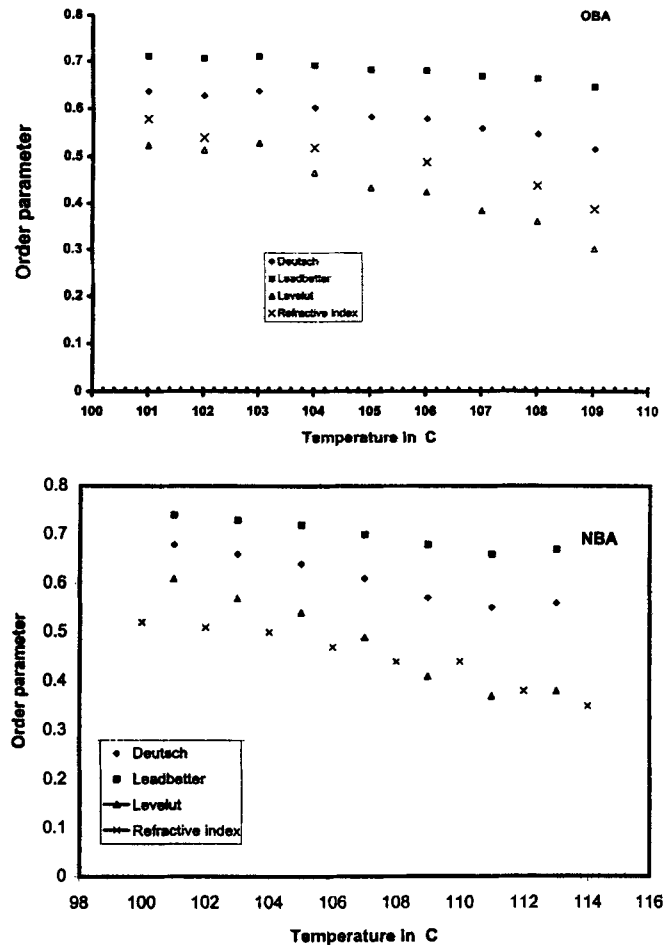


Figure 2. Variation of orientational order parameter $\langle P_2 \rangle$ with temperature for OBA and NBA.

$$\langle \cos^2 \beta \rangle = J_2(m)/J_0(m)$$

and

$$S = (3\langle \cos^2 \beta \rangle - 1)/2.$$

The relation involving 'f' is given by

$$\langle \cos^2 \beta \rangle = \sum f_{2i}/(2i+3)/\sum f_{2i}/2i+1.$$

We have written suitable Fortran programmes for the different methods described above to compute the order parameter $\langle P_2 \rangle$ using the intensity corresponding to various arc angles. The higher order parameter $\langle P_4 \rangle$ has also been computed. The computed values of $\langle P_2 \rangle$ at different temperatures are shown in figure 2 along with the order parameter obtained from refractive index data.

4. Results and discussion

It is evident from figure 2 that the trend in the variation of $\langle P_2 \rangle$ computed from the different methods is the same. However, the values computed by the Deutsch method lies in between the values computed by the Leadbetter *et al* and Levelut methods. This is due to the truncation of the series to a finite number of terms whereas the solution is exact in Deutsch method. The values obtained from the refractive index data are lower compared to the results from X-ray method. This difference between the X-ray and optical methods arise primarily due to averaging procedure of the orientational distribution function. In X-ray method, it is the local averaging, whereas, it is the local and macroscopic averaging in the optical method. Hence the difference is basically due to the distinction between the microscopic and macroscopic orientational order as observed by Davidson *et al* (1995), and de Vries (1972). Deutsch method is more reliable because of the fact that it involves computation of orientational order parameter using analytically obtained solutions. Hence under these circumstances, we have used the Deutsch method (3) to estimate the higher order

Table 1. Higher order parameter $\langle P_4 \rangle$ for OBA and NBA.

$T_c - T$	OBA		NBA	
	Deutsch	Refractive index	Deutsch	Refractive index
12	—	0.161	0.278	—
11	0.220	—	0.233	0.098
10	0.210	0.127	0.259	—
8	0.182	0.112	0.227	—
7	0.163	—	0.117	0.071
6	0.160	0.092	0.134	—
5	0.141	—	0.114	0.064
4	0.131	0.064	0.104	—
3	0.106	—	0.092	0.039

parameter $\langle P_4 \rangle$ and compared with the values of $\langle P_4 \rangle$ from the refractive index data (table 1). The necessary distribution functions for OBA and NBA are given in figure 3. It is observed from table 1 that there is broad agreement between the two methods indicating that the skewness of the distribution function is independent of the type of averaging (local or macroscopic) whereas the variance (width) of the $f(\beta)$ depends on the averaging procedures (de Gennes 1974).

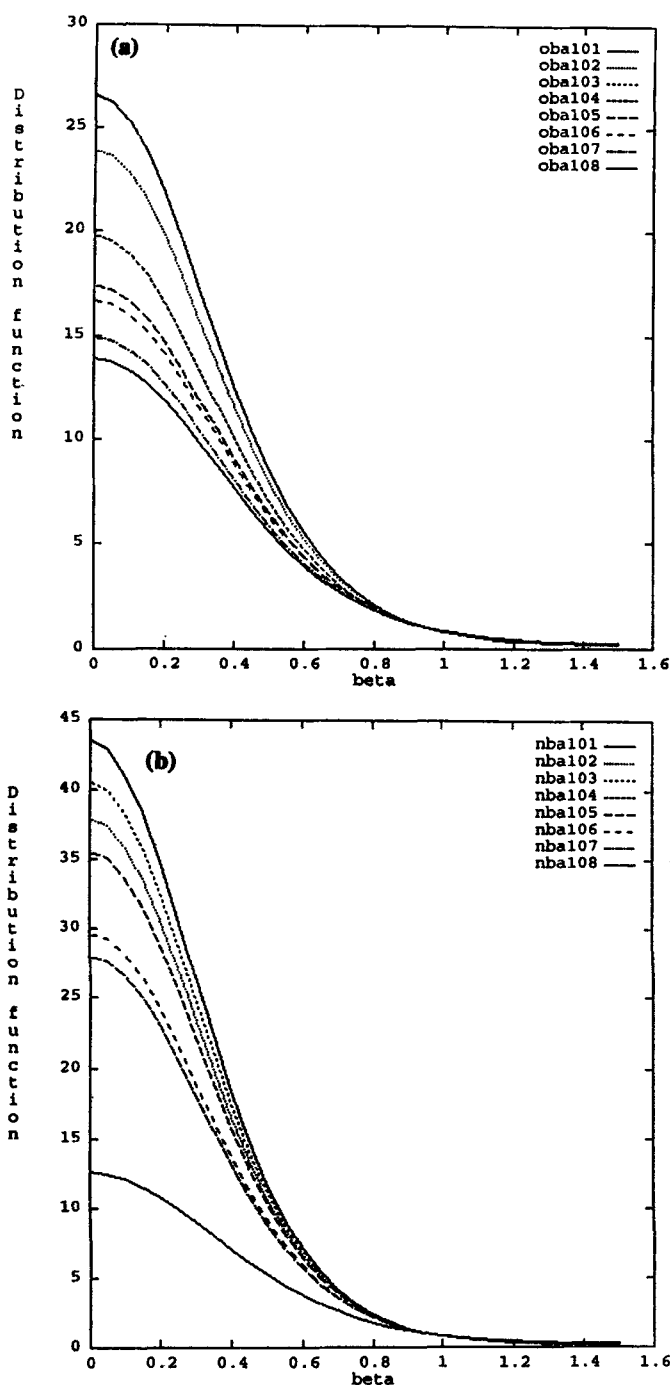


Figure 3. Distribution functions obtained from Deutsch method at various temperatures for (a) OBA and (b) NBA.

5. Conclusion

The orientational order parameters have been estimated from X-ray method using various approaches and compared with the values obtained from the refractive index method for OBA and NBA. The observed differences in orientational parameters have been explained in terms of averaging procedures of $f(\beta)$. It has been pointed out here that the skewness of the $f(\beta)$ is independent of the type of averaging.

Acknowledgements

Authors thank CSIR, New Delhi for the Project. They also thank Prof. N V Madhusudana and Dr K A Raghunathan, Raman Research Institute, Bangalore for the collection of the X-ray intensity data using the imaging plate system. Authors thank the referees for suggestions to improve the presentation of the paper.

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