

# Model-based remote sensing algorithms for particulate organic carbon (POC) in the Northeastern Gulf of Mexico

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Hydrographic data, including particulate organic carbon (POC) from the Northeastern Gulf of Mexico (NEGOM) study, were combined with remotely-sensed SeaWiFS data to estimate POC concentration using principal component analysis (PCA). The spectral radiance was extracted at each NEGOM station, digitized, and averaged. The mean value and spurious trends were removed from each spectrum. De-trended data included six wavelengths at 58 stations. The correlation between the weighting factors of the first six eigenvectors and POC concentration were applied using multiple linear regression. PCA algorithms based on the first three, four, and five modes accounted for 90, 95, and 98% of total variance and yielded significant correlations with POC with  $R^2 = 0.89, 0.92,$  and  $0.93$ . These full waveband approaches provided robust estimates of POC in various water types.

Three different analyses (root mean square error, mean ratio and standard deviation) showed similar error estimates, and suggest that spectral variations in the modes defined by just the first four characteristic vectors are closely correlated with POC concentration, resulting in only negligible loss of spectral information from additional modes. The use of POC algorithms greatly increases the spatial and temporal resolution for interpreting POC cycling and can be extrapolated throughout and perhaps beyond the area of shipboard sampling.

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## 1. Introduction

The Gulf of Mexico, a semi-enclosed basin with passages at the Yucatan Channel and the Florida Straits, is biologically productive in the continental shelf regions and has a physically complex regional and mesoscale circulation system (Vastano *et al* 1995; Walker 1996; Ohlmann and Niiler 2005). Several river systems on the surrounding land provide a large mass of fresh water to the shelf along with suspended sediments, organic and inorganic matter, and pollutants. Higher levels of materials in the Gulf of Mexico have a different spatial and temporal variability influenced by the seasonal

and inter-annual variations of the local shelf and mesoscale circulations (Lohrenz *et al* 1990; Redalje *et al* 1994; Rabalais *et al* 1996; Walker 1996). These conditions can sometimes cause negative impacts resulting from high productivity and subsequent carbon export, which may contribute to the formation of 'dead zones' of hypoxia such as along the Gulf Coast. The Northeastern Gulf of Mexico (NEGOM), Louisiana–Texas Shelf Physical Oceanography Program (LATEX), and hypoxia studies have provided useful information for characterizing the oceanic environment of the northern Gulf of Mexico region (Redalje *et al* 1994; Cho *et al* 1998; DiMarco and Reid 1998). These studies have

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greatly expanded our knowledge on many parameters of the carbon pool as well as hydrography. However, carbon measurements have been made in a limited number of programs.

Particulate organic carbon (POC) plays a key role in the transport of carbon in the ocean through the biological pump. While  $\text{CO}_2$  and dissolved organic carbon (DOC) move with the water, POC can settle through the water column, across isopycnals, scavenging or aggregating other particles and transporting carbon and associated elements to deeper waters. Thus POC is a key component in the ocean's role in sequestering and isolating carbon from the atmosphere. Because POC is produced/cycled on day-to-week time scales, a synoptic picture of POC changes can only be obtained by employing remote sensing techniques. To investigate more components of the carbon cycle, empirical approaches have been developed recently based on the optical closure relationships using single or multiple spectral wavelengths and provide a reasonable assessment of POC distribution on regional to global scales (Stramski *et al* 1999, 2008; Loisel *et al* 2001; Mishonov *et al* 2003; Stramska and Stramski 2005; Gardner *et al* 2006; Son 2006; Son *et al* 2009). Several empirical approaches have been used for estimating chlorophyll concentration in ocean color studies, as well as using model-based approaches based on orthogonal vector analyses, using remote sensing data (Mueller 1976; Gower *et al* 1984; Fischer *et al* 1986; Sathyendranath *et al* 1989; Neumann *et al* 1995) but the latter approaches have not been studied sufficiently for POC concentration.

The principal component analysis (PCA), one of the model-based approaches to estimate water constituents, is generally used to produce a reduced variance for the analysis of information in multi-dimensional datasets. PCA is used to analyze information from empirical or modeled datasets and to separate the signal from noise (Mueller 1976; Neumann *et al* 1995; IOCCG 2000). In ocean color studies a characteristic vector analysis method using multiple wavelengths has been introduced to determine the relationship between chlorophyll concentrations and spectral wavelengths, and enhance the potential discrimination and reconstruction accuracy of constituents present (Mueller 1976; Gower *et al* 1984; Fischer *et al* 1986; Sathyendranath *et al* 1989; Neumann *et al* 1995; IOCCG 2000). In this study, the main idea is to develop accurate and efficient POC algorithms using a model-based approach employing multiple wavelengths and *in situ* measurements. This method can be optimized to take into account regional or seasonal variations by applying regional optical models to derive the weighting coefficients for the estimator. It is important for quantifying

the time-varying evolution of POC in surface waters to monitor, and eventually model, the impact of climate change on surface water biomass and productivity (Son 2006).

## 2. Data and methods

### 2.1 *In situ* shipboard data

In order to understand the spatial and temporal physical processes in the northern Gulf of Mexico, the Northeastern Gulf of Mexico (NEGOM) project conducted nine cruises from November 1997 to August 2000 along the same eleven track lines. Each seasonal cruise was completed along lines normal to the coastline between mid-Florida and the Mississippi River, starting from about 20 m water depth on the shelf and moving out to the 1000 m isobath (figure 1). This area spans a wide range of particle concentrations and types, from turbid river runoff to clear and open-ocean waters.

POC samples were collected from rosette water bottles at about half of the stations ( $\sim 60$  sampling points). Prior to each cruise, 25-mm diameter GF-75 (approximately  $0.7\ \mu\text{m}$  pore size) glass-fiber filters were combusted in a thermolyne type 1300 furnace along with aluminum foil squares to oxidize any organic traces on the filters and foil (Gordon 1969; Sharp 1974; JGOFS 1996). During each cruise, water samples (1  $\sim$  3 liters) including all organic particles were filtered to determine concentrations of POC at each of the  $\sim 60$  stations. The filters were then wrapped in aluminum foil and placed in a drying oven under low heat, approximately  $30^\circ\text{C}$ , for 3–4 hours (Bernal 2001). After each cruise the filters were acidified to remove the carbonates and combusted, converting the organic carbon to  $\text{CO}_2$ , which was then measured by thermal conductivity (JGOFS 1996). Blank (unused and pre-combusted filters) corrections were applied and results were given in concentration of  $\text{mg}/\text{m}^3$ .

### 2.2 *Satellite* data

Daily SeaWiFS satellite images (Level 1A) covering the Gulf of Mexico were obtained from the NASA Goddard Space Flight Center DAAC archives (<http://oceancolor.gsfc.nasa.gov/>). L1A images were processed to Level 2 using the SeaWiFS Data Analysis System (SeaDAS) (Baith *et al* 2001; McClain *et al* 2004) software. The spectral normalized water-leaving radiance ( $L_{wn}$ ) were derived from the SeaWiFS Level 2 (geolocated, geophysical values, L2) data using the SeaDAS standard correction algorithm for all eight

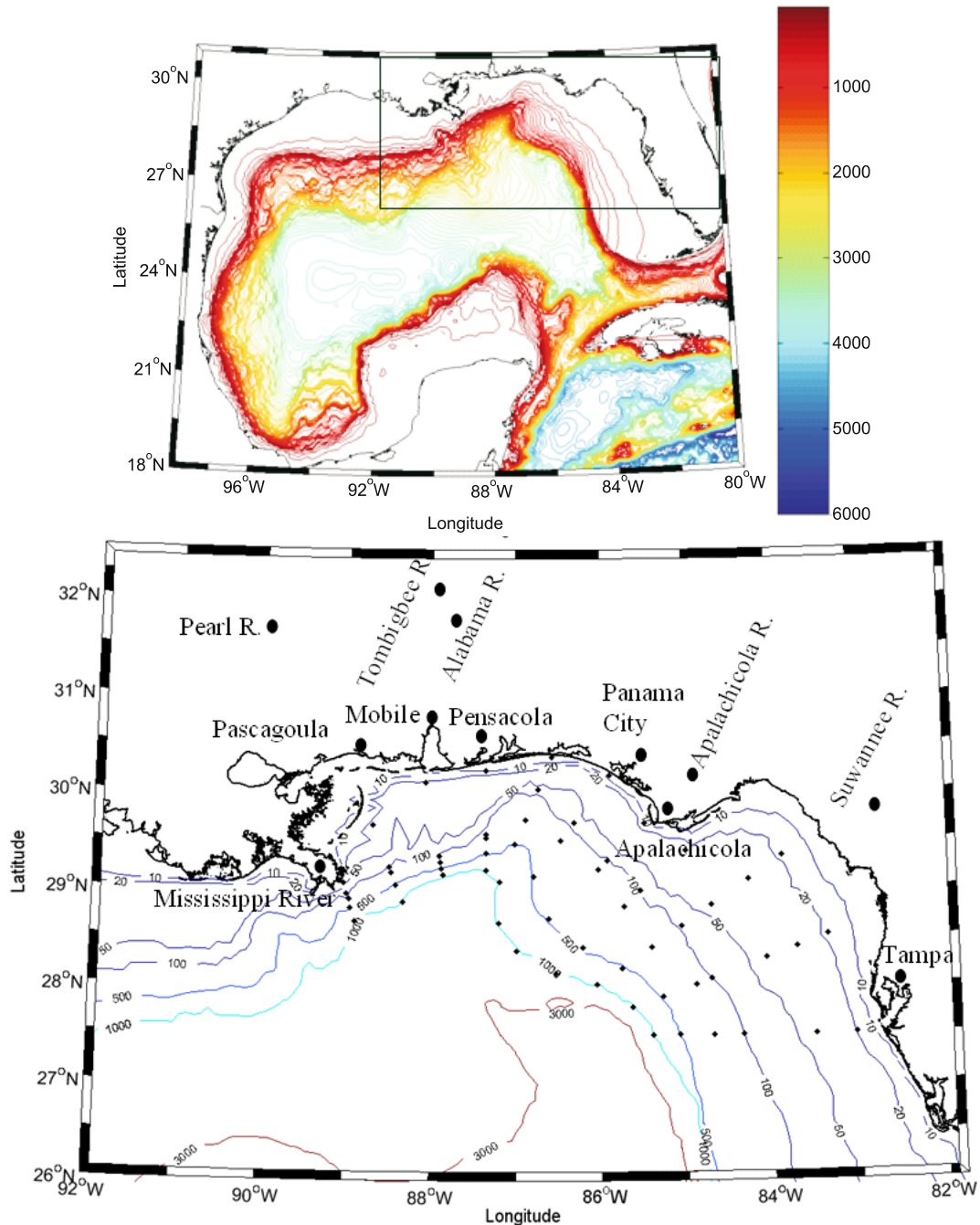


Figure 1. Bathymetry and sampling stations in the Northeastern Gulf of Mexico (NEGOM) occupied during 9 cruises from November 1997 to August 2000 (11 sampling transects and 60 POC sampling stations).

spectral channels. The derived six visible wavelengths (412, 443, 490, 510, 555, and 670 nm) data were used to develop an algorithm to estimate POC.

### 2.3 Model-based approach

A match-up dataset between *in situ* measurements and satellite data synchronously obtained from the same cruise time was generated. The empirical match-up analysis adopted the NASA Ocean

Biology Processing Group's (OBPG) approach (Bailey *et al* 2000, 2006). In our study, we used  $3 \times 3$  pixel grid (*i.e.*,  $>4$  valid pixels) instead of a  $5 \times 5$  pixel grid. The 58 POC sub-samples, which totaled about 11% of the total 526 POC samples, were matched with the SeaWiFS spectral data within  $\pm 3$  hours of POC sampling and within  $\pm 3$  hours of local noon.

In this study, PCA was used to determine the information from empirical datasets, to transform the data in a manner suitable for analysis, and

to separate a useful signal from noise in the data. This correlated dataset was used to determine the spectral dimensionality of the data, and the weighting of each spectral channel required to estimate the variables of interest (Gower *et al* 1984; Sathyendranath *et al* 1989; IOCCG 2000).

We first removed the calculated mean value  $\mu(\lambda)$  from each normalized water leaving radiance ( $\lambda$ ). We also computed and removed any linear trend existing in the record deemed to be spurious. The resulting de-measured series of  $D(\lambda)$  are termed standardized as:

$$D_n(\lambda) = \sum_{i=1}^n \sum_{j=1}^m [L_i(\lambda_j) - \mu(\lambda_j)], \quad (1)$$

where  $L$  is the spectral remote sensing dataset of original  $N \times M$  matrix,  $i$  is the observation number and  $j$  is the measurement at the given spectral wavelength.

The computationally efficient singular value decomposition (SVD) of a matrix is applied to calculate eigenvectors and eigenvalues. SVD is based on the concept that any rectangular  $N \times M$  matrix  $D_n(\lambda)$  can be written as the product of three matrices: an  $N \times N$  matrix  $U$ , a  $N \times M$  diagonal matrix  $\Gamma$  with positive or zero elements, and the transposition ( $V^\dagger$ ) of the  $M \times M$  matrix  $V$ .

$$D_n(\lambda) = U \times \Gamma \times V^\dagger. \quad (2)$$

Matrix  $\Gamma$  is a rectangular  $N \times M$  matrix with zero elements outside the diagonal and positive or zero elements on the diagonal. The scalars on the diagonal,  $\gamma_k$ , are called the singular values and are typically placed in decreasing order of magnitude. Again, there is a maximum of  $k \leq \min(N, M)$  non-zero singular values, which defines the maximum number of PCA modes we can determine, so that the effective dimension of matrix  $\Gamma$  is  $k \times k$ .

An original observation vector,  $L$ , may be transformed into its characteristic system representation through the  $k$  equations.

$$\text{PC}_i = \sum_{j=1}^n e_{ij} \times D_j; \quad (3)$$

$$i = 1, 2, \dots, k \quad \text{and} \quad j = 1, 2, \dots, N,$$

where  $\text{PC}_i$  is called the  $i$ th principal component of  $D_i$  and characteristic vector  $e_{ij}$  is the

$i$ th characteristic vector. Thus, we effect the transformation

$$(D_1, D_2, \dots, D_N) \rightarrow (\text{PC}_1, \text{PC}_2, \dots, \text{PC}_k),$$

where  $k$  is less than or equal to  $N$  to retain the desired proportion of sample variance.

### 3. Results and discussions

#### 3.1 A model-based approach (principal component analysis)

The spectral normalized water-leaving radiances at six wavelengths for 58 stations were analyzed using PCA analysis to obtain the eigenvalues and eigenvectors of the dimensionally reduced data. The principal components (PCs) of the first six characteristic vectors were calculated. The correlation between these PCs and POC concentrations was determined using multiple linear regression and added weighting factors. This approach reduced the data to a small number of orthogonal vectors and the corresponding weight factors for each sample. The reduced dataset simplifies the task of information extraction and interpretation (Mueller 1976; Gower *et al* 1984; Sathyendranath *et al* 1989).

In the first approach, we compared discrete POC concentration with averaged radiance data from each NEGOM cruise. Figure 2(a) graphically shows the total variance calculated by PCA. The first and second modes (54 and 27%) were clearly dominant, followed by a steep drop in variance of the third and fourth modes, which accounted for 10 and 4% of the total variance respectively. The first three, four, and five modes accounted for 90, 94, and 98% of total variance.

In figure 2(b), the peak in the mean spectral radiance occurred at the shorter wavelengths and rapidly dropped off in the green and red wavelengths. In examining individual eigenvectors, the first eigenvector showed a small maximum at 555 nm. The maximum in the second eigenvector occurred at the shortest wavelength measured 412 nm, and the third eigenvector maximum was at 490 nm (figure 2c). The other three eigenvectors had double maxima but lower eigenvalues (<4% of total variance, figure 2d).

The first eigenvector shows high values at longer wavelengths, perhaps due to increased scattering from elevated concentrations of nonliving and living organic particles. The maximum of the second vector is shifted to shorter wavelengths,

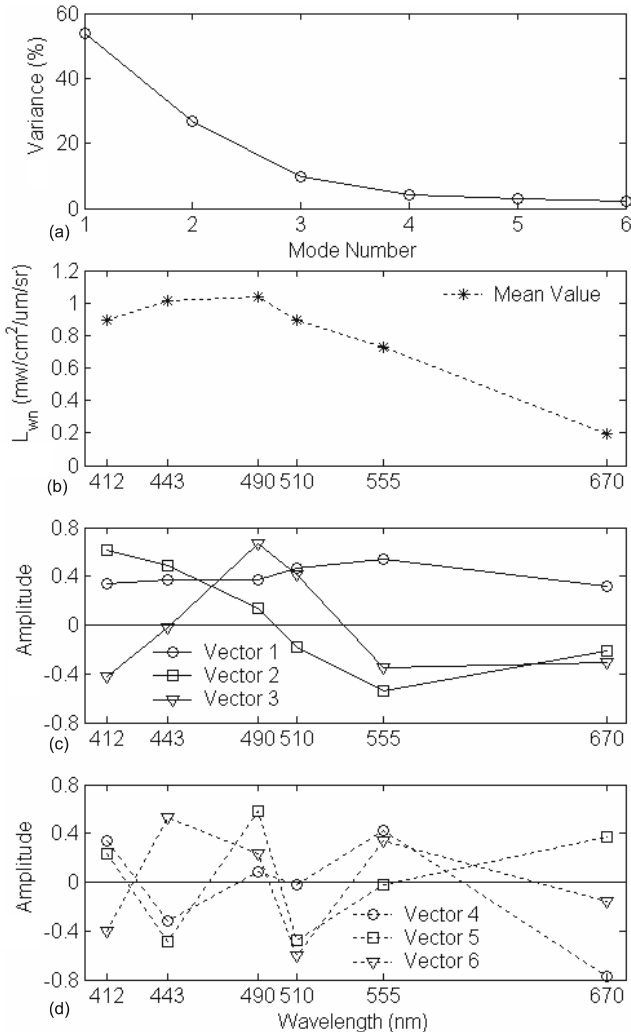


Figure 2. PCA analysis using 58 samples and six wavelengths: (a) Total variance versus PCA mode number, (b) mean spectral radiance versus wavelength, and (c, d) the first six eigenvectors derived from NEGOM data. The first eigenvector showed that the maximum occurred at 555 nm, the second eigenvector shows maximum at 412 nm, and the third at 490 nm. Eigenvectors 4–6 show double maxima.

violet-blue wavelengths, which is the characteristic of increasing radiance due to low absorption. The third vector appears to be a combination of moderate concentrations of nonliving and living organic particles at 490 nm (figure 2c). The fourth and fifth vectors show lower radiance peaks at 670 nm and the sixth vector has a high value at 670 nm. The shapes of vectors reveal that spectral response depends on absorption/scattering of nonliving and living organic particles (Gower *et al* 1984, figures 2c and 2d).

We can observe the patterns of characteristic eigenvectors from the spectral response curve (Son 2006; Son *et al* 2009). When the POC concentration in the surface water increased, the radiance peak shifted from the shorter wavelengths

(412 and 443 nm, violet-blue band) to longer wavelengths (555 nm, green band). Radiance at 510 nm remained at a relatively constant value over a wide range of POC concentrations (< 20 to > 550 mg/m<sup>3</sup>). One would expect that at lower POC concentration, the spectral curve maximum would shift to shorter wavelengths, since blue water-leaving radiance should increase (relative to longer wavelengths where light does not penetrate as deeply). When POC concentration increases, the radiance peak shifts towards longer wavelengths as radiance from particles dominates the signal.

However, a fixed number of spectral radiances in model-based approaches does not yield an equal number of independent constituents affecting the radiance because of the similarity in the spectral response generated by different oceanic constituents (Fischer 1985), i.e., the spectral response of different constituents in the water is not unique. Therefore, only a small number of spectral measurements yield independent information about water constituents of interest. The degree of interdependence between radiances measured at different wavelengths can be determined with an eigenvalue analysis (Twomey 1977). The orthogonality of the radiance signals of the individual components will determine our ability to recover these components from the total radiance spectrum.

A least-squares fit of the principal component (PC) values to POC concentrations using the multiple-linear regression method showed that POC estimates (mg/m<sup>3</sup>) were related to each principal component of the SeaWiFS visible wavelengths by the equation:

$$\text{POC} = 10^{(-0.1 \times \text{PC}_1 + 0.66 \times \text{PC}_2 + 0.474 \times \text{PC}_3 + 2.054)}, \quad (4)$$

where  $\text{PC}_{1,2,3}$  are the principal components of the first three modes using surface POC and averaged radiance data from each NEGOM cruise.

Equation (4) demonstrates that weighting vectors 2 and 3 contributed roughly equally to describing the effects of POC concentration but vector 1 anti-correlated with POC (negative exponent for  $\text{PC}_1$ ). Figure 3(a) and table 1 show the scatter plot between *in situ* surface POC measurements and POC estimates using equation (4). This multiple regression was well correlated with lower POC concentration but scattered at higher POC concentration ( $R^2 = 0.89$ ,  $N = 58$ ). To determine a quantitative algorithm evaluation, Son *et al* (2009) provided a useful method to distinguish between samples dominated by organic and inorganic components based organic percent. Through

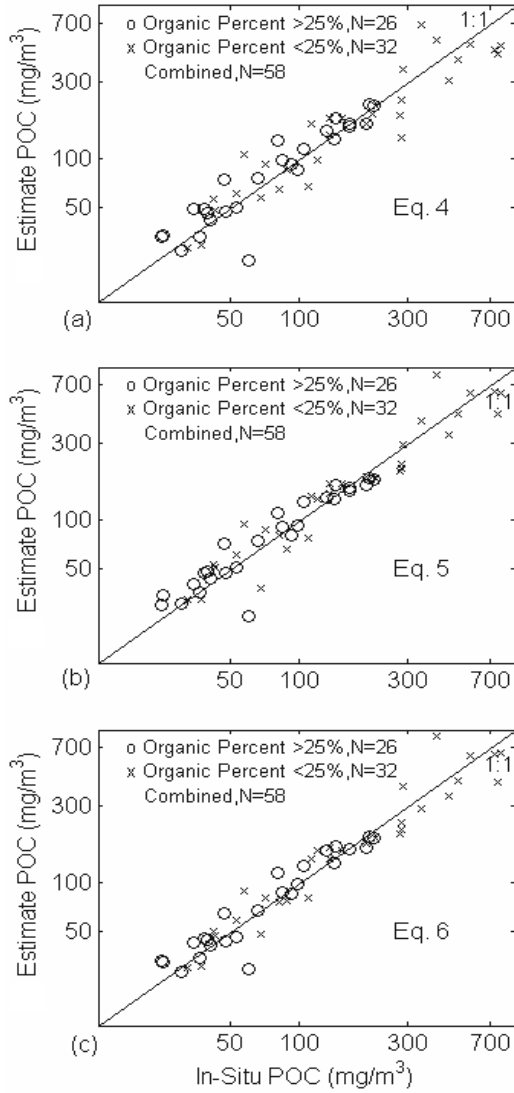


Figure 3. Comparisons between *in situ* POC and estimated POC using three different algorithms based on multiple linear regression and weighted PCA vectors. Data are delineated by percent organic carbon > 25% and < 25%. The lines are 1:1 slopes. All correlation statistics are in table 1.

empirical analysis they found that the 25% value best correlated POC/PM and beam attenuation coefficient due to particles at 660 nm,  $c_p$ . This assessment demonstrated that POC was better related to  $c_p$  when organic matter dominated the total mass of particles, as one would expect (organic matter  $\sim 2 \times$  POC). We applied this relationship between the measured and estimated POC to our study. Figure 3 and table 1 provide correlation plots and statistical data between discrete POC measurements and POC estimates obtained with three different algorithms (equations 4–6) using samples where organic percent > 25%, < 25%, and combined POC samples. The root mean square error (RMSE), mean ratio values between the *in situ* POC and POC estimates,

as well as the corresponding standard deviation were computed and tabulated in table 1. The results of RMSE, mean ratio, and standard deviation where POC > 25%, < 25%, and combined POC samples were not significantly different; the regression slightly overestimated when organic percent > 25% and underestimated when organic percent < 25% (table 1).

Equation (5) reveals that weighting vectors 2, 3, and 4 contributed similarly to describe the effects of POC concentration but vector 1 anti-correlated with POC. Figure 3(b) shows the scatter plot between *in situ* surface POC measurements and POC estimates obtained with equation (5). The correlation revealed a good relationship between POC measurements and weighted spectral data ( $R^2 = 0.92$ ,  $N = 58$ ). The results of error analysis where > 25%, < 25%, and combined POC samples provided a closer correlation between *in situ* and estimated POC than the previous approach (equation 4).

$$\text{POC} = 10^{(-0.1 \times \text{PC}_1 + 0.66 \times \text{PC}_2 + 0.474 \times \text{PC}_3 + 0.84 \times \text{PC}_4 + 2.054)}, \quad (5)$$

where  $\text{PC}_{1,2,3,4}$  are the principal components of the first four modes.

Equation (6) demonstrates that weighting vectors 2, 3, and 4 contributed similarly to describing the effects of POC concentration but vectors 1 and 5 anti-correlated with POC (negative exponents). Figure 3(c) and table 1 show the scatter plot and statistics between *in situ* surface POC measurements and POC estimates using equation (6). This multiple regression reveals a significant correlation between POC measurements and weighted spectral data with  $R^2 = 0.93$  ( $N = 58$ ). Although this approach using equation (3) provided reasonable estimates of POC concentrations regardless of whether organic percent was > 25%, < 25%, or combined, the RMS error was not significantly different than with equation (5).

$$\text{POC} = 10^{(-0.1 \times \text{PC}_1 + 0.66 \times \text{PC}_2 + 0.474 \times \text{PC}_3 + 0.84 \times \text{PC}_4 - 0.693 \times \text{PC}_5 + 2.054)}, \quad (6)$$

where  $\text{PC}_{1,2,3,4,5}$  are the principal components of the first five modes.

In figure 3 and table 1, the first three, four, and five vectors demonstrated different weighting factors with varying POC concentrations showing similar effects of POC concentrations. Although the first three vectors accounted for about 90% of the total variance, the POC concentrations

Table 1. Regression (type II) of in-situ POC versus estimated POC from algorithms:  $RMSE = \sqrt{\sum (\log_{10}(\text{estimate\_POC}) - \log_{10}(\text{in-situ\_POC}))^2 / (N - 1)}$ , mean ratio =  $1/N \sum (\log_{10}(\text{estimate\_POC}) / \log_{10}(\text{in-situ\_POC}))$ , the corresponding standard deviations, bias are calculated with POC > 25%, < 25%, and combined POC samples.

Organic percent	Slope	Intercept	$R^2$	RMSE	Mean ratio	Standard deviation	$N$
Equation (4)							
> 25% POC	0.924	0.166	0.852	0.118	1.016	0.068	26
< 25% POC	0.880	0.244	0.877	0.144	0.994	0.066	32
Combined	0.889	0.228	0.889	0.133	1.004	0.067	58
Equation (5)							
> 25% POC	0.889	0.220	0.880	0.103	1.010	0.059	26
< 25% POC	0.932	0.140	0.916	0.119	0.997	0.056	32
Combined	0.922	0.161	0.922	0.112	1.003	0.058	58
Equation (6)							
> 25% POC	0.930	0.142	0.905	0.092	1.009	0.053	26
< 25% POC	0.934	0.136	0.925	0.112	0.997	0.050	32
Combined	0.933	0.138	0.933	0.103	1.002	0.052	58

estimated using the first three vectors and weighting factors had a slightly higher error (table 1). Adding the fourth or fifth vectors and weighting factors provided a better correlation over a wide range of surface POC concentrations. These higher vectors appear to provide more systematic information about high POC concentrations which are affected by strong absorption and scattering radiances. However, each vector provided reasonable POC estimates for turbid waters. One, or a combination of the weighted eigenvalues reduced the noise levels from an optically complex environment. Although this linear approach does not accurately describe the physical relationship between principal components of the spectral radiance and POC concentration, the results of PCA demonstrate that using the first four vectors rather than all six lost virtually no information about the original constituents and provided a better correlation than using a single-wavelength ratio (Son 2006; Son *et al* 2009). In a previous study (Son 2006; Son *et al* 2009), the empirical POC approach used all wavelengths from blue to green to reduce the scatter of radiance signal. It was demonstrated that to obtain the best POC estimates in complex waters requires complex algorithms using 4–6 wavelengths rather than a single wavelength or the simple blue-to-green ratios typically used for open ocean waters. The empirical and model-based approaches employ full spectral radiance information and are well correlated with a broad range of POC concentrations. Still, further studies are necessary to establish a databank of spectral signatures of different water constituents using multispectral, multivariate data (Gower *et al* 1984; Sathyendranath *et al* 1989; IOCCG 2000).

Figure 4 is the reconstruction of estimated POC using the PCA algorithm (equation 4) and ocean color data collected by SeaWiFS Level 1A (1.1 km resolution). The PCA approach employed full spectral radiance information and was well correlated at lower and higher POC concentration. The most notable difference between maps constructed strictly from field data and POC maps from PCA analysis applied to SeaWiFS data, is the more detailed spatial pattern of POC, especially in coastal areas which were excluded during shipboard sampling. Cruises N1/N4/N7 were completed during fall, N2/N5/N8 – during spring, and N3/N6/N9 – during summer. The range of PCA-POC concentrations within the area circumscribed by the bottle samples was 17–889 mg/m<sup>3</sup>. The geometric mean based on the PCA algorithm was  $121 \pm 39$  mg/m<sup>3</sup> for the fall seasons,  $124 \pm 50$  mg/m<sup>3</sup> for the spring seasons, and  $200 \pm 41$  mg/m<sup>3</sup> for the summer seasons. During the fall and early spring, elevated POC concentrations were confined to the inner shelf. During the late spring and summer, elevated POC concentrations extended out to the outer shelf and the upper slope. During those summer cruises the Loop Current and eddies, drew water from the Mississippi area out beyond the shelf into the open Gulf of Mexico. However, the close fit between POC estimates for PCA and measured POC suggests that spectral variations in the modes defined by the first four characteristic vectors are more closely related to POC concentration than with other optically important properties of sea water such as phytoplankton, suspended inorganic matter or CDOM. Thus, this algorithm should be valid in waters with

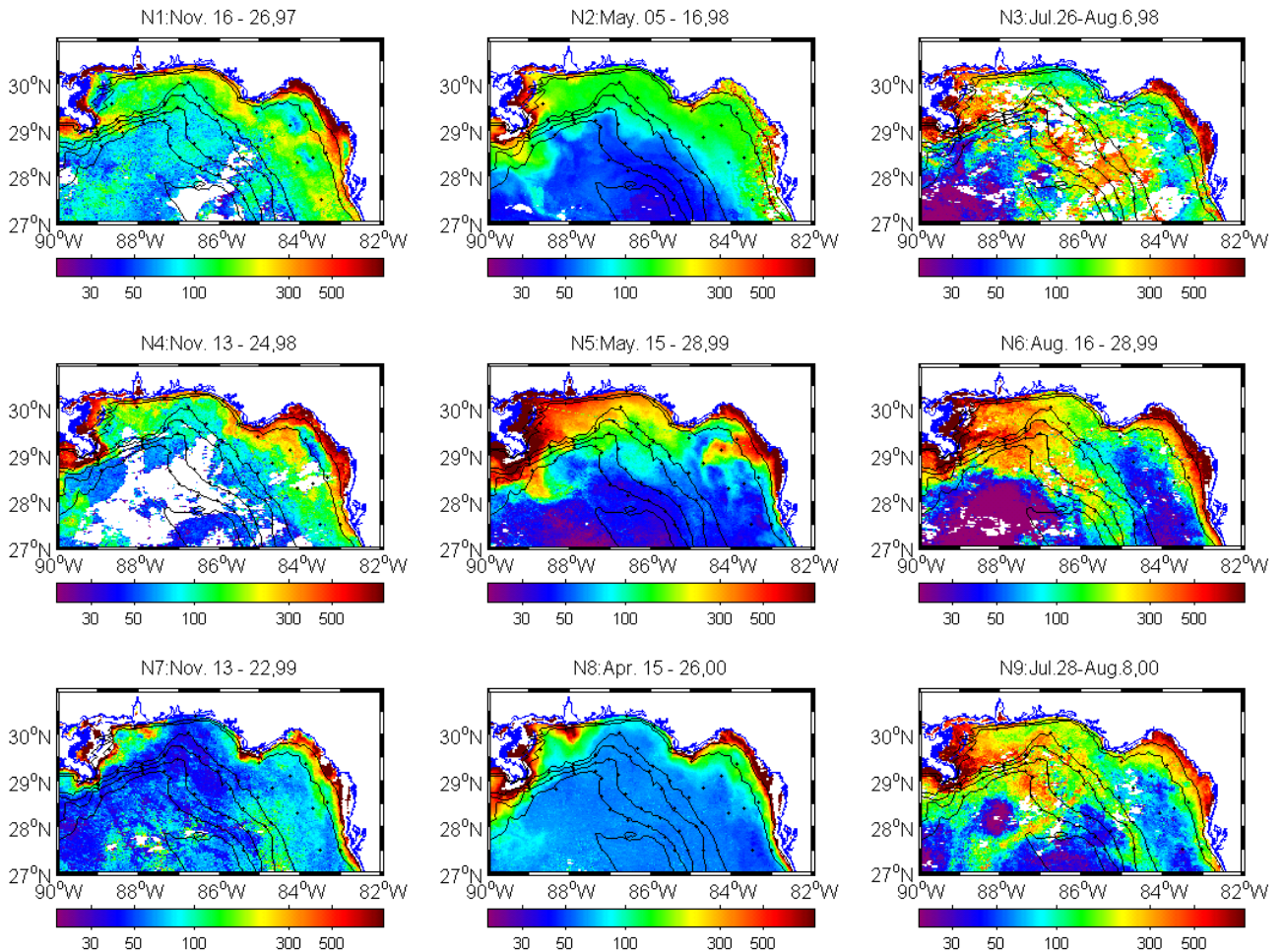


Figure 4. Estimated POC concentration ( $\text{mg}/\text{m}^3$ ) in the Northeastern Gulf of Mexico. Each map is compiled using PCA equation (5). POC estimates are well correlated with *in situ* data at both low and high POC concentrations.

both high and low %POC (*i.e.*, coastal and open-ocean waters). Since the accuracy of the PCA was similar in high and low %POC waters, it opens the question whether this algorithm could be applied to larger regions or even globally. We tested the PCA using a few samples from other oceans with promising results, but more data and testing are required.

Son *et al* (2009) presented more detailed information about the difference between the bottle measurements and estimated POC. A later paper will use multivariate analysis to examine the distribution of POC and many other environmental factors (wind, temperature, chlorophyll, river runoff, etc.) that influence those distributions based on the work of Son (2006).

#### 4. Conclusions

Using large datasets that include *in situ* measurements and ocean color products, the classical approach for estimating POC with high

spatial resolution over wide areas is to develop empirical or model-based algorithms. From our analysis of the spectral response curve, we found that the peak spectral radiance was significantly dependent on POC concentration (Gower *et al* 1984; Sathyendranath *et al* 1989). Three different model-based PCA approaches using the spectral dependence were developed for POC estimates from normalized water-leaving radiances at six wavelengths. The characteristic eigenvalues and eigenvectors were derived from the reduced dimension of the spectral radiances. Nearly the entire variability of spectral radiances for POC estimates could be explained by the first three, four, or five modes (90, 95, and 98% of total variances). The first vector yielded information about higher POC concentrations. The second vector yielded information about lower POC concentrations. The third vector provided information about moderate POC concentrations. Other vectors did not yield further information about POC concentration, most likely because of the optically complex conditions due to one or more influences of scattering

and absorption conditions by phytoplankton, suspended inorganic matter or CDOM.

Although the results of PCA algorithms tested by three different approaches reveal a significant relationship between *in situ* measurements and estimated POC, the POC algorithm which employed the first four modes showed that the derived relations were most sensitive when using all SeaWiFS wavelengths over the entire range of *in situ* POC concentrations. These algorithms are promising for mapping POC concentration regionally based on remote sensing data as it clearly reproduces the spatial distribution and seasonal cycles in the Gulf of Mexico. This approach for developing algorithms appears useful for estimating and monitoring POC concentrations at least on regional scales, and should be tested on even broader spatial scales.

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