

Calculation of geometrical coupling coefficients for the hyperspherical harmonics approach

TAPAN K DAS and TUSHAR BARAN DE

Physics Department, University of Burdwan, Burdwan 713 104, India

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Abstract. An elegant and fast method for the calculation of geometrical structure coefficients needed for an expansion of a few-body wavefunction and interaction in hyperspherical harmonics has been proposed. A sum rule for the GSC has also been derived, which is useful for an independent check of the coefficients. The proposed method of computation is many orders of magnitude faster than conventional methods.

Keywords. Nuclear structure; few-body problem; hyperspherical harmonics method; geometrical structure coefficients.

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Introduction

An exact solution of the few-body Schrödinger equation is of great interest in many branches of physics. Apart from the inherent interest in the precise structure and physics of few-body systems, such systems are very good testing grounds for few-particle interactions as well as for approximation methods. For exact calculations of the few body systems the methods of Faddeev (Faddeev 1960; Schmid and Ziegelmann 1974) or Yakubowski (1967) equations and hyperspherical harmonics (Ballot and Fabre 1980; Simonov 1966, 1972) (also called K harmonics) have been widely used. Among these a particularly powerful method is the hyperspherical harmonics expansion (HHE) method, which has been extensively used to investigate trinucleons (Erens *et al* 1971; Demin *et al* 1973; Ballot and Navarro 1975; Das *et al* 1982; Das and Coelho 1982; Coelho *et al* 1983) as well as other three- and four-body problems (Gallieres *et al* 1976a, b; Ballot *et al* 1972). The hyperspherical harmonics (HH) are the multidimensional analog of the ordinary spherical harmonics, which are used as a complete basis set for expansion of the hyperangular part of the few-body space wavefunction. The HHE method (Ballot and Fabre 1980) deals directly with wave function in configuration space and this provides a clear insight into the physics of the problem. Inclusion of long-range, hard-core or many-body (Erens *et al* 1971; Demin *et al* 1973; Ballot and Navarro 1975; Das and Coelho 1982; Das *et al* 1982; Coelho *et al* 1983; Fabre 1979) interactions is straightforward in this method and the structure of the equations in the HHE method remains unaltered due to the inclusion of such interactions.

In the standard HHE approach (Ballot and Fabre 1980) both the space wavefunction and the interaction potential are expanded in terms of suitable HH basis. Substitution